

Solved Paper 2021*

Instructions

 There are 150 questions in all. The number of questions in each part is as given below. No. 	of Questions
Part I Physics	1-40
Part II Chemistry	41-80
Part III a. English Proficiency	81-95
b. Logical Reasoning	96-105
Part IV Mathematics	106-150
* All questions are Multiple Choice Questions bouing four entires out of which anti- and is correct	

PART I

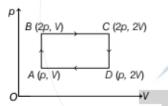
All questions are Multiple Choice Questions having four options out of which only one is correct.

d. zero

- Each correct answer fetches 3 marks while incorrect answer has a penalty of 1 mark.
- Time allotted to complete this paper is 3 hrs.

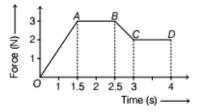
Physics

1. An ideal monoatomic gas is taken round the cycle *ABCDA* as shown in the *p*-V diagram.



The work done during the cycle is a. pV b. 2pV c. pV/2

 The initial speed of a body of mass 2.0 kg is 5 m/s. A force acts for 4 s in the direction of motion of the body, as shown in force-time graph. The impulse of force is



a. 8.50 Ns	b. 8 Ns
c. 5.5 Ns	d. 6 Ns

3. For a constant hydraulic stress on an object, the fractional change in the object's volume $\left(\frac{\Delta V}{V}\right)$

and its bulk modulus B are related as

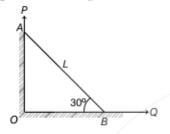
$$a. \frac{\Delta V}{V} \propto B$$
 $b. \frac{\Delta V}{V} \propto B^2$ $c. \frac{\Delta V}{V} \propto \frac{1}{B}$ $d. \frac{\Delta V}{V} \propto \frac{1}{B^2}$

4. A shunt is connected in parallel with a galvanometer. Why?
a. To prevent galvanometer from strong current
b. To convert galvanometer into ammeter
c. To increase the range of ammeter

- d. All of the above
- The phase difference between the V_{out} and V_{in} of CE-amplifier circuit is

 a. 90°
 b. 180°
 c. 0°
 d. 270°

- If nth division of main scale coincides with (n + 1)th divisions of vernier scale. The least count of the vernier is (Given, one main scale division is equal to a units)
 - a. $\frac{a+1}{n+1}$ b. $\frac{a}{n}$ c. $\frac{a}{n+1}$ d. $\frac{a+1}{n}$
- A uniform rod AB of length L = 1 m is sliding along two mutually perpendicular surfaces OP and OQ as shown in figure.



When the rod subtends an angle $\theta = 30^{\circ}$ with OQ, then the end *B* has a velocity $\sqrt{3}$ m/s. The velocity of end *A* at that time is

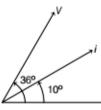
b. 0.5 m/s **d.** $\frac{1}{\sqrt{2}}$ m/s

- **a.** 1 m/s
- **c.** √3 m/s
- **8.** A tray of mass (*M*) 12 kg is supported by a spring as shown in figure.



When the tray is pressed down and released, it executes SHM with a period of 1.5 s. When a block of mass *m* placed on the tray, then the period of SHM changes to 3.0 s. The mass of block is **a.** 36 kg **b.** 48 kg **c.** 12 kg **d.** 24 kg

9. The phasor diagram of a load represents which circuit?



- a. Purely capacitive
- b. Purely inductive
- **c.** R-L-C circuit with X_L more than X_C
- d. R-L-C circuit with X_L less than X_C

10. The equation of progressive wave is given by $y = ric \left[x \left(\frac{t}{x} - \frac{x}{x} \right) + \frac{\pi}{x} \right]$ cm. Which one of the

$$I = \sin \left[x \left(\frac{5}{5} - \frac{9}{9} \right)^{+} \frac{6}{6} \right] \text{ cm. which one of the following is correct?}$$

$$a, v = 5 \text{ cm/s}$$

$$b, \lambda = 18 \text{ cm}$$

c. A = 0.04 cm **d.** f = 50 Hz

- The property of light used in optical fibre cables is
 - a. total internal reflection
 - refraction
 - c. interference
 - d. polarisation
- 12. A man walks in a straight line for 5 min with a velocity of 45 m/s. What is the speed with which he has to move in order to comeback to its original position in 1.5 min?
 - *a*. 90 m/s *b*. 150 m/s
 - *c.* 135 m/s *d.* 115 m/s
- **13.** From a solid sphere of mass *M* and radius *R*, a spherical portion of radius $\frac{R}{2}$ is removed as

shown in the figure.



Taking gravitational potential V = 0 at $r = \infty$, the potential at the centre of the cavity thus formed is

- $a. -\frac{GM}{2R} \qquad b. -\frac{GM}{R}$ $c. -\frac{2GM}{3R} \qquad d. -\frac{2GM}{R}$
- **14.** Four charges equal to +Q are placed at the four corners of a square and a charge (-q) is at its centre. If the system is in equilibrium, then the value of -q is

a.
$$-\frac{Q}{4}(1+2\sqrt{2})$$

b. $\frac{Q}{2}(2\sqrt{2}+1)$
c. $\frac{Q}{4}(1+2\sqrt{2})$
d. $\frac{Q}{4}(1+\sqrt{2})$

15. A force F = a + bx acts on a particle in the x-direction, where a and b are constants. The work done by this force during a displacement from x = 0 to x = d is

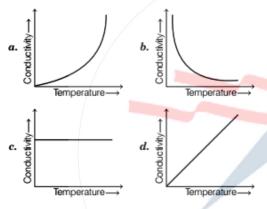
$$a. \left(a + \frac{bd}{2}\right)d \qquad b. \left(ad + \frac{bd}{2}\right)$$
$$c. \left(\frac{ad + bd}{2}\right) \qquad d. (ad + b)\frac{d}{2}$$

16. A proton has kinetic energy E = 100 eV which is equal to that of a photon. The wavelength of photon is λ_2 and that of proton is λ_1 . The ratio

$$\frac{\lambda_2}{\lambda_1}$$
 is proportional to

- **a**. E^2 **b**. $E^{\frac{1}{2}}$ **c**. E^{-1} **d**. $E^{-\frac{1}{2}}$
- 17. A block of mass 10 kg rests on a rough inclined plane making an angle of 30° with the horizontal. The coefficient of static friction between the block and the plane is 0.1. The friction force on the block is

 a. 4.9 N
 b. 49√3 N
 c. 49 N
 d. 0.1 × 49√3 N
- **18.** Which of the following graphs show the correct relation between conductivity and temperature for a metallic conductor?



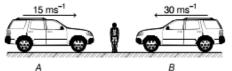
- **19.** The radius of a muonic hydrogen atom is 25×10^{-13} m. The total atomic volume (in m³) of a mole of such hydrogen atoms is (Take, $\pi = 3.14$) **a.** 3.94×10^{-14} **b.** 3.09×10^{-14} **c.** 4×10^{-14} **d.** 3.9×10^{-14}
- 20. The angular momentum of a body placed at origin of mass 1 kg and having position vector r = 3t î + 4j is

 a. time dependent 	b. 3 k J-s
c. − 12 k J-s	d. 0

21. If the earth stops rotating about its axis, then what will be the change in the value of g at a place in the equatorial plane? (Radius of earth = 6400 km) a. 3.7 cm/s² b. 9.8 m/s^2

an on anyo	01 010 1140
c. 0	d. 3.4 cm/s ²

22. Two cars approach a stationary observer from opposite sides as shown in the figure.



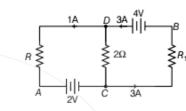
The observer hears no beats. If the frequency of the horn of the car *B* is 504 Hz, then the frequency of the horn of the car *A* will be **a.** 529.2 Hz **b.** 440.5 Hz

d. None of these

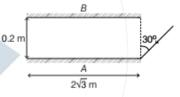


23.





- In the following circuit, assuming point A to be at zero potential, then what is the potential at point B? a. 1 V b. 2 V c. 4 V d. 3 V
- **24.** Two plane mirrors *A* and *B* are aligned parallel to each other as shown in the figure.



A ray of light is incident at an angle 30° at a point just inside one end of A. The plane of incidence coincides with the plane of the figure. The maximum number of times, the ray undergoes reflection (excluding the first one) before it emerges out is

25. A projectile is given an initial velocity of $(\hat{i} + \hat{j})$ m/s, where \hat{i} is along the ground and \hat{j} is along the vertical. If $g = 10 \text{ m/s}^2$, then the equation of its trajectory is

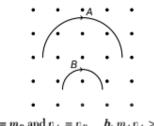
its trajectory is	
a. $y = x + 5x^2$	b. $y = x - 5x^2$
c. $y = x^2 + 5x$	$d. y = x^2 - 5x$

26. Two drops of equal radius R coalesce to form a bigger drop. What is the ratio of surface energy of bigger drop to smaller one?

$a. 2^{-1/3}: 1$	b. 2 ^{2/3} : 1
c. 1 : 1	$d. 2^{1/2}:1$

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27. Two particles A and B of masses m_A and m_B respectively, are having same charge and moving on same plane. A uniform magnetic field exists perpendicular to this plane. The speeds of the particles are v_A and v_B respectively and the trajectories are as shown in figure. Then,



a. $m_A = m_B$ and $v_A = v_B$ **b.** $m_A v_A > m_B v_B$ **c.** $m_A < m_B$ and $v_A < v_B$ **d.** $m_A v_A < m_B v_B$

- **28.** The potential difference applied to an X-ray tube is decreased. As a result, in the emitted radiation,
 - a. the intensity increases
 - b. the intensity decreases
 - c. the minimum wavelength increases
 - d. the minimum wavelength decreases

29. The ratio of the specific heats
$$\frac{C_V}{C_p} = \frac{1}{\gamma}$$
 in terms

of degrees of freedom n is given by

$$a. \left(1 + \frac{n}{3}\right) \qquad b. \left(1 + \frac{2}{n}\right)$$
$$c. \left(1 + \frac{n}{2}\right) \qquad d. \left(1 + \frac{1}{n}\right)$$

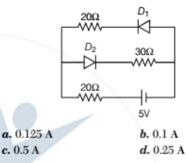
- **30.** A cyclist speeding at 6 m/s in a circle of 18 m radius makes an angle θ with the vertical. The minimum possible value of coefficient of friction between the tyres and the ground is

 a. 12.041
 b. 0.2041
 c. 11.32
 d. 10.020
- **31.** Three particles each of mass *m* are kept at the vertices of an equilateral triangle of side *b*. Moment of inertia of the system about an axis passing through the centroid and perpendicular to its plane is

a.
$$3 mb^2$$
 b. mb^2 **c.** $\frac{mb^2}{3}$ **d.** $\frac{2}{3}mb^2$

- **32.** An electric dipole is placed at an angle of 30° in a non-uniform electric field. The dipole will experience
 - a. torque only
 - b. translational force only in the direction of the field

- c. translational force only in a direction normal to the direction of the field
- d. torque as well as a translational force
- **33.** Two coils *A* and *B* have a mutual inductance 0.001 H. The current changes in the first coil according to the equation $i = i_0 \sin \omega t$, where $i_0 = 10$ A and $\omega = 10\pi$ rads⁻¹. The maximum value of emf in the second coil is **a**. 0.01 π V **b**. 1 π V **c**. 0.1 π V **d**. 0.05 π V
- 34. The current in the circuit will be



35. The bob of a pendulum of length 2m lies at *P*, when it reaches *Q*, it loses 10% of its total energy due to air resistance.

 The velocity of bob at Q is

 a. 6 m/s
 b. 1 m/s

 c. 2 m/s_____
 d. 8 m/s

36. A particle executes SHM with a frequency *f*. The frequency with which its kinetic energy oscillates is

a.
$$\frac{f}{2}$$
 b. f **c.** 2f

37. A radioactive sample at any instant has its disintegration rate 5000 disintegrations per min. After 5 min, the rate is 1250 disintegrations per min. Then, the disintegration constant (per min) is

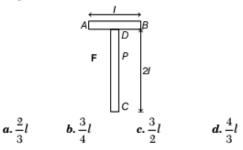
d. 4f

a. 0.4 log _e 2	b. 0.2 log _e 2
c. 0.1 log _e 2	d. 0.8 log _e 2

38. The separation between two parallel plates of capacitor is 1 mm. What is the electric potential generates between the plates of capacitor, when electric field of 2000 N/C is applied on it?

a. 2 v	0. 2000 V
c. 0.2 V	d. 200 V

- Choose the correct statement.
 - a. The speed of light in the meta-material is v = c |n|.
 - **b.** The speed of light in the meta-material is v =
 - c. The speed of light in the meta-material is v = c.
 - d. The wavelength of the light in the meta-material (λ_m) is given by $\lambda_m = \lambda_{air} |n|$.
- 40. A T-shaped object with dimensions shown in figure, is lying on a smooth floor. A force F is applied at the point P parallel to AB, such that the object has only the translational motion
- without rotation. Find the location of P with respect to C.



PART II

Chemistry

41. The most volatile compound among the given option is a. o-nitrophenol b. p-nitrophenol

d. can't say

d. √9

- c. m-nitrophenol
- 42. What is the magnetic moment of Ti²⁺? (Given : Atomic number = 22) c. √6
 - **a**. √8 b. √10
- 43. Why only Xe can form compounds with fluorine among noble gases?
 - a. Large size
 - b. Low electronegativity
 - c. High ionisation energy
 - d. Low electron gain enthalpy
- 44. Which of the following inert gas is used as cryogenic agent? **d.** Kr
 - **a**. He **b**. Ne c. Ar

For the following reaction,

 $2A + 3B \longrightarrow 3C + 4D$

expression for rate	of reaction is
$a, \frac{d[A]}{d}$	h 1 d[B]
$\frac{dt}{dt}$	$\frac{0}{2} \frac{1}{dt}$
1 d[C]	$\int 1 d[D]$
c	$a. \frac{-}{4}$

 Cyclohexanol on reacting with H₂SO₄ and then heating gives a. cyclohexene b. cyclohexanone **c**. c

one of these

- The major product obtained on reaction of 3-methylbutene with HCl is a. 2-chloro-2-methylbutane b. 3-chloro-2-methylbutane
 - c. 1-chloro-2-methylbutane
 - d. 3-chloro-3-methylbutane

- **48.** If Rydberg constant is same for all elements, the angular momentum and energy of Li2+ of which orbital is equal to angular momentum and energy of 1s-orbital of hydrogen atom? a. 3s b. 4s **d.** 3d c. 2p
- 49. Sodium iodide reacts with ammonia to give a. [Na(NH3)4] I b. [Na(NH₃)₄] I₃ c. [Na(NH₃) I₃] I d. [Na(NH₃)₃I]
- 50. In photography, which compound is used as a fixing agent a. sodium thiosulphate b. ammonium thiosulphate

c. sodium chloride d. Both (a) and (b)

- The compound formed on reaction of epoxy ethane with NH3 and H2O is a. mono-ethanol amines b. di-ethanol amines c. tri-ethanol amines d. All of these
- 52. The process of removal of excess electrolyte from colloidal solution is a. coagulation b. dialysis
- c. ultra-filtration d. peptisation **53.** Maltase converts maltose into
- a. glucose b. sucrose c. fructose d. starch 54. Starch is a polymer of
 - a. glucose b. fructose d. None of these c. Both (a) and (b)
- Methyl alcohol can be distinguished from ethyl alcohol using a. Fehling solution
 - b. Schiff's reagent
 - c. Sodium hydroxide and iodine
 - d. Phthalein fusion test

a. anionic soap b. cationic detergent c. anionic detergent d. Non-ionic soap 57. Which is not an anti-fluorite structure a. Rb₂S b. BaF₂ c. K₂O d. Li₂O The structure of ClF₃ is a. T-shape b. bent shape c. linear d. trigonal planar 59. Which of the following is diamagnetic in nature? b. 02a. 02 c. N²⁺₂ **d**. B₂ The correct order of bond order in SO2, SO3, SO2-, SO2- is $a. SO_3^{2-} > SO_4^{2-} > SO_3 = SO_3$ **b.** $SO_4^{2-} > SO_3 > SO_2 > SO_3^{2-}$ $c. SO_2 = SO_3 > SO_4^{2-} > SO_3^{2-}$ d. Can't say 61. Ionisation energy for H⁺ ion is proportional to r^n , then value of *n* is b. -1 d. −2 a. 1 c. 2 62. Role of BHA in food industries a. prevent oxidation b. prevent reduction c. add sweeteners d. None of these Permanganate ion (MnO⁻₄) is dark purple coloured though Mn is in + 7 oxidation state with d^0 configuration. This is due to a. d - d transition b. charge transfer from metal to ligand c. charge transfer from ligand to metal d. All of the above 64. Rutherford model could not explain a. electronic structure of an atom b. stability of an atom c. Both (a) and (b) d. None of the above 65. Which is true in case of [Ni(CO)₄]? a. Hybridisation of Ni is sp³ b. Hybridisation of Ni is dsp² c. Paramagnetic d. Square planar SI unit of Boltzmann's constant is

56. Sodium stearate (C₁₇H₃₅COO⁻Na⁺) is

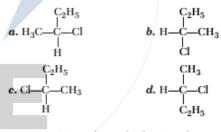
a. JK⁻¹ b. eVK⁻¹ c. erg K⁻¹ d. JK

reaction? a. Substitution reaction b. Polymerisation reaction c. Condensation reaction d. Addition reaction 68. Magnetic moment of Co in [CoF₆]²⁻ of unpaired electron is **b**. √45 **d**. √30 a. √35 c. $\sqrt{40}$ Some statements about heavy water are given below 1. Heavy water is used as a moderator in nuclear reactors. 2. Heavy water is more associated than ordinary water. 3. Heavy water is more effective solvent than ordinary water.

Acetone does not undergo which type of

Which of the above statements are correct? *a*. 1 and 2 *b*. 1, 2 and 3

- c. 2 and 3 d. 1 and 3
- 70. CH₃—CHCl—CH₂—CH₃ has a chiral centre, which of the following represents its R configurations?



- 71. In Victor Meyer's method 0.2 g of an organic substance displaced 56 mL of air at STP the molecular weight of the compound is
 a. 56
 b. 112
 c. 80
 d. 28
- **72.** For the complete combustion of ethanol, $C_2H_5OH(l) + 3O_2(g) \longrightarrow 2CO_2(g) + 3H_2O(l)$, the amount of heat produced as measured in bomb calorimeter is 1364.47 kJ mol⁻¹ at 25°C. Assuming ideality the enthalpy of combustion, ΔH_C , for the reaction will be $(R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1})$
 - a. 1366.95 kJ mol⁻¹
 - **b.** 1361.95 kJ mol⁻¹
 - c. 1460.50 kJ mol⁻¹
 - d. 1350.50 kJ mol⁻¹

73. The incorrect expression among the following is $a. \frac{\Delta G_{\text{system}}}{\Delta S_{\text{total}}} = -T$

b. In isothermal process, $W_{\text{reversible}} = -nRT \ln \frac{V_f}{V}$

$$c. \ln K = \frac{\Delta H^{\circ} - T\Delta S^{\circ}}{RT}$$
$$d. K = e^{-\Delta G^{\circ}/RT}$$

74. The solubility of Pb(OH)2 in water is 6.7×10^{-6} M. Its solubility in a buffer solution of pH=8 would be a. 1.2×10^{-2} **b.** 1.6×10^{-3}

c. 1.6×	10 ⁻²	d.	$1.2 \times$	10-3

75. The density (in g mL⁻¹) of a 3.60 M sulphuric acid solution that is 29% H2SO4 (molar mass = 98 g mol⁻¹) by mass will $\overline{b}e$

a. 1.64	b. 1.88
c. 1.22	d. 1.45

- 76. The relative lowering of vapour pressure of a dilute aqueous solution containing non-volatile solute is 0.0125. The molality of the solution is about a. 0.70 d. 0.80
 - c. 0.90 **b**. 0.50

a. English Proficiency

Directions (Q. Nos. 81-83) Choose the word which best expresses the meaning of the underlined word in the sentence.

- 81. Decay is an immutable factor of human life. a. important b. unique c. unchangeable d. awful
- 82. It was an ignominious defect for the team. a. shameful b. admirable d. worthv c. unaccountable
- **83.** His <u>conjecture</u> was the better than mine. a. guess b. fact c. surprise d. doubt

Directions (Q. Nos. 84-86) Fill in the blanks.

84. Freedom and equality are the rights of every human. a. inalienable b. inscrutable

c. incalculable	d. institutional	
Pradoon's face encke	of the bar	

85. Pradeep's face spoke of the happiness he was feeling. a. elegantly b. tons c. volumes d. much

77. Equal masses of methane and oxygen are mixed in an empty container at 25°C. The fraction of the total pressure exerted by oxygen is

a.
$$\frac{2}{3}$$
 b. $\frac{1}{3} \times \frac{273}{298}$ **c.** $\frac{1}{3}$ **d.** $\frac{1}{2}$

78. The molar conductivities of KCl, NaCl and KNO₃ are 152, 128 and 111 S cm² mol⁻¹ respectively. What is the molar conductivity of NaNO₃? a. 101 S cm² mol⁻¹ $b. 87 \, \mathrm{S} \, \mathrm{cm}^2 \, \mathrm{mol}^{-1}$

$$-101 \text{ S cm}^2 \text{ mol}^{-1} \qquad d. -391 \text{ S cm}^2 \text{ mol}^{-1}$$

- 79. The approximate time duration in hours to electroplate 30 g of calcium from molten calcium chloride using a current of 5 A is (Atomic mass of Ca = 40) a. 80 **b.** 10 c. 16 d. 8
- Given, the reduction potential of Na⁺, Mg²⁺, Al³⁺ and Ag⁺ as $E^{\circ}_{Na^+/Na} = -2.17 \text{ V};$

 $E^{\circ}_{Mg^{2+}/Mg} = -2.37 \text{ V}; E^{\circ}_{Ag^{+}/Ag} = -0.08 \text{ V};$ $E^{\circ}_{Al^{3+}/Al} = -1.66 V$

The least stable oxide is **b.** Al₂O₃ c. MgO

- d. Na₂O
- 86. His speech was disappointing : it all the major issues.
 - a. projected
 - b. revealed

a. Ag₂O

PART III

c.

- c. skirted
- d. analysed

Directions (Q. Nos. 87-89) Choose the word which is closest to the opposite in meaning of the given italicised word.

- Hydra is biologically believed to be immortal. a. undving b. perishable d. eternal c. ancient
- 88. The Gupta rulers *patronised* all cultural activities and thus Gupta period was called the golden era in Indian History. a. criticised b. rejected c. opposed d. spurned
- 89. This is a barbarous act. a. bad b. good c. civilised d. exemplary

Directions (Q. Nos. 90-92) In each of the following questions, out of the four alternatives, choose the one which can be substituted for the given words/sentence.

90. A person who doe	es not believe in any religion
a. Philatelist	b. Rationalist

c. Atheist	d. Pagan

 A person who believes that pleasure is the chief good

a. Stoic	b. Hedonist	c. Epicure	d. Sensual

One who loves manking	
a. Anthropologist	b. Philanthropist
c. Seismologist	d. Optometrist

Directions (Q. Nos. 93-95) Choose the order of the sentences marked A, B, C, D and E to form a logical paragraph.

- **93.** A. Tasty and healthy food can help you bring out their best.
 - B. One minute they are toddlers and next you see them in their next adventure.
 - C. Your young ones seem to be growing so fast.
 - D. Being their loving custodians, you always want to see them doing well.
 - E. Their eyes sparkle with curiosity and endless questions on their tongues. Codes

a. DBCEA	b. CADEB
c. CBEDA	d. ECABD

b. Logical Reasoning

96. Choose the correct answer figure which will make a complete square on joining with the problem figure.

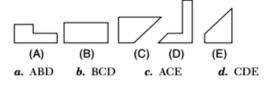
Problem figure

Answer figures

d



97. In the following question, five figures are given. Out of them, find the three figures that can be joined to form a square.



- 94. A. It is hoping that overseas friends will bring in big money and lift the morale of the people.
 - B. But a lot needs to be done to kick start industrial revival.
 - C. People had big hopes from the new government.
 - D. So far government has only given an incremental push to existing policies and programmes.
 - E. Government is to go for big time reforms, which it promised.

Codes

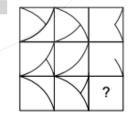
a. BCDAE	b. EADCB
c. DABEC	d. CDEAB

- **95.** A. However, women hiring is catching up at a slow and steady rate in the recent times.
 - B. Gender ratio has been inclined more towards male employees.
 - C. As a result, recent reports have highlighted the rise in demand for women employees.
 - D. Women constitute a little over half of world's total population.
 - E. But, their contribution to measured economic activity is far below the potential. Codes

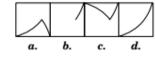
Codes

- a. DEBACb. CDAEBc. BCDEAd. AEDBC
- **98.** Choose the answer figure which completes the problem figure matrix.

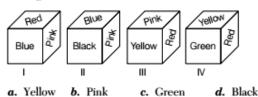
Problem Figure



Answer Figures

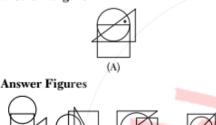


99. From the given four positions of a single dice, find the colour at the face opposite to the face having red colour.



100. In the following questions, one or more dots are placed in the figure marked as (A). The figure is followed by four alternatives marked as (a), (b), (c) and (d). One out of these four options contains region(s) common to the circle, square, triangle, similar to that marked by the dot in figure (A).

Problem Figure



- 101. Complete the series by replacing '?' mark. G4T, J9R, M20P, P43N, S90L, ? a. S90L b. V185J c. M20P d. P43N
- 102. Neeraj starts walking towards South. After walking 15 m, he turns towards North. After walking 20 m, he turns towards East and walks 10 m. He then turns towards South and walks 5 m. How far is he from his original position and in which direction?

a. 10 m, East	b. 10 m, South-East
c. 10 m, West	d. 10 m, North-East

- 103. The average age of 8 men is increased by 2 yrs. when one of them whose age is 20 yr is replaced by a new man. What is the age of the new man? a. 28 yr b. 36 yr c. 34 yr d. 35 yr
- 104. Shikha is mother-in-law of Ekta who is sister-in-law of Ankit. Pankaj is father of Sanjay, the only brother of Ankit. How is Shikha related to Ankit?

a. Mother-in-law b. Aunt c. Wife d. Mother

105. In a row of forty children, P is thirteenth from the left end and Q is ninth from the right end. How many children are there between P and R, if R is fourth to the left of Q?

a. 12 **b**. 13 c. 14 **d**. 15

Mathematics

- **106.** If Re(z + 2) = |z 2|, then the locus of z is a. parabola b. circle c. ellipse d. hyperbola
- **107.** If $a \in R$, $b \in R$, then the equation $x^2 - abx - a^2 = 0$ has a. one positive root and one negative root b. Both positive roots
 - c. Both negative roots
 - d. Non-real roots
- **108.** If a + 2b + 3c = 12, $(a, b, c \in R^+)$, then the maximum value of ab^2c^3 is d. 2⁵

$$a. 2^{\circ}$$
 $b. 2^{\circ}$ $c. 2^{\circ}$

109. Sum of *n* terms of the infinite series ~ 2 a - 2

$$1.3^2 + 25^2 + 3.7^2 + ... \infty$$
 is
a. $\frac{n}{2}(n+1)(6n^2 + 14n + 7)$

$$b \cdot \frac{n}{6}(n+1)(6n^2+14n+5)$$

c.
$$\frac{n}{6}(n+1)(2n+1)(3n+1)$$

d. $4n^3 + 4n^2 + n$

110. If $\log_7 5 = a$, $\log_5 3 = b$ and $\log_3 2 = c$, then the logarithm of the number 70 to the base 225 is

$a.\frac{1-a+abc}{2a(1+b)}$	$b.\frac{1-a-abc}{2a(1+b)}$
$c. \frac{1+a-abc}{2a(1+b)}$	$d.\frac{1+a+abc}{2a(1+b)}$

111. The maximum number of points of intersection of 10 circles is

A 90

a. 80
b. 90
c. 85
d. 95
112.
$$\frac{C_1}{C_0} + 2\frac{C_2}{C_1} + 3\frac{C_3}{C_2} + 4\frac{C_4}{C_3} + \dots 20\frac{C_{20}}{C_{19}} =$$

a. 120
b. 260
c. 210
d. 180

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PART IV

 $0 \quad x-p \quad x-q$ **113.** If $p \neq q \neq r$ and x + p = 0x - r = 0, then the x+q x-rvalue of x which satisfy the equation is a. x = p**b**. x = qc. x = r $d_x = 0$ x 3 2] **114.** Matrix $A = \begin{bmatrix} 1 & y & 4 \end{bmatrix}$, if xyz = 60 and $2 \ 2 \ z$ 8x + 4y + 3z = 20, then A(adj A) is equal to
 a. $\begin{bmatrix} 64 & 0 & 0 \\ 0 & 64 & 0 \\ 0 & 0 & 64 \end{bmatrix}$ b. $\begin{bmatrix} 68 & 0 & 0 \\ 0 & 88 & 0 \\ 0 & 0 & 88 \end{bmatrix}$ $d.\begin{bmatrix} 34 & 0 & 0 \\ 0 & 34 & 0 \end{bmatrix}$ [68 0 0] c. 0 68 0 **115.** If $f(x) = 4x - x^2$, $x \in R$, and f(a+1) - f(a-1) = 0, then a is equal to **a.** 0 **b**. 2 c. 1 d. 3 **116.** Which of the following is not an equivalence relation in z? **a**. $aRb \Leftrightarrow a + b$ is an even integer **b.** $aRb \Leftrightarrow a - b$ is an even integer c. aRb $\Leftrightarrow a < b$ $d. aRb \Leftrightarrow a = b$ 117. Which of the following is always true? $a.(\sim p \lor \sim q) \equiv (p \land q)$ **b.** $(p \rightarrow q) \equiv (\sim q \rightarrow \sim p)$ c. $\sim (p \rightarrow \sim q) \equiv (p \land \sim q)$ **d.** $\sim (p \leftrightarrow q) \equiv (p \rightarrow q) \rightarrow (q \rightarrow p)$ **118.** The solution of the inequation $4^{-x+0.5} - 7.2^{-x} < 4, x \in R$ is $a(-2, \infty)$ **b**. (2, ∞) $c.\left(2,\frac{7}{2}\right)$ d. None of these **119.** If $\cos^3 x \cdot \sin 2x = \sum_{m=1}^n a_m \sin mx$ is identity in *x*, then **a.** $a_3 = \frac{3}{8}, a_2 = 0$ **b.** $n = 6, a_1 = \frac{1}{2}$ c. $n = 5, a_1 = \frac{3}{4}$ d. $\Sigma a_m = \frac{1}{4}$ 120. Total number of solutions of $|\cot x| = \cot x + \frac{1}{\sin x}, x \in [0, 3\pi]$ is equal to

b. 2

a. 1

c. 3

d. 0

121. The minimum value of $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$ is equal to

a.
$$\frac{\pi^3}{32}$$
 b. $\frac{5\pi^3}{32}$ **c.** $\frac{9\pi^3}{32}$ **d.** $\frac{11\pi^3}{32}$

- **122.** The origin is shifted to (1, 2). The equation $y^2 - 8x - 4y + 12 = 0$ changes to $y^2 = 4ax$, then *a* is equal to *a*. 1 *b*. 2 *c*. -2 *d*. -1
- **123.** The equations of the bisector of the angles between the straight lines 3x + 4y + 7 = 0 and 12x + 5y - 8 = 0 are *a.* 7x + 9y + 17 = 0, 99x + 77y + 51 = 0*b.* 7x - 9y - 17 = 0, 99x + 77y - 51 = 0*c.* 7x - 9y + 17 = 0, 99x + 77y + 51 = 0*d.* None of the above
- **124.** Equation of circle which passes through the points (1, -2) and (3, -4) and touch the *X*-axis is **a.** $x^2 + y^2 + 6x + 2y + 9 = 0$ **b.** $x^2 + y^2 + 10x + 20y + 25 = 0$ **c.** $x^2 + y^2 + 6x + 4y + 9 = 0$

d. None of the above

- **125.** If x = 9 is the chord of contact of the hyperbola $x^2 y^2 = 9$, then the equation of the corresponding pair of tangent is **a**. $9x^2 - 8y^2 + 18x - 9 = 0$ **b**. $9x^2 - 8y^2 - 18x + 9 = 0$ **c**. $9x^2 - 8y^2 - 18x - 9 = 0$ **d**. $9x^2 - 8y^2 + 18x - 9 = 0$
- **126.** The points with position vectors $10\hat{i} + 3\hat{j}$, $12\hat{i} - 15\hat{j}$ and $a\hat{i} + 11\hat{j}$ are collinear, if a is **a.** -8 **b.** 4 **c.** 2 **d.** $\frac{82}{9}$
- **127.** Let a, b, c be vectors of lengths 3, 4, 5 respectively and a be perpendicular to $(\mathbf{b} + \mathbf{c})$, b to $(\mathbf{c} + \mathbf{a})$ and c to $(\mathbf{a} + \mathbf{b})$, then the value of $(\mathbf{a} + \mathbf{b} + \mathbf{c})$ is **a**. $2\sqrt{5}$ **b**. $2\sqrt{2}$ **c**. $10\sqrt{5}$ **d**. $5\sqrt{2}$
- **128.** For non-zero vectors $\mathbf{a}, \mathbf{b}, \mathbf{c}; |(\mathbf{a} \times \mathbf{b}) \cdot \mathbf{c}| = |\mathbf{a}||\mathbf{b}||\mathbf{c}|$ holds if and only if $\mathbf{a}, \mathbf{a} \cdot \mathbf{b} = 0, \ \mathbf{b} \cdot \mathbf{c} = 0$ $\mathbf{c}, \mathbf{c} \cdot \mathbf{a} = 0, \ \mathbf{a} \cdot \mathbf{b} = 0$ $\mathbf{b}, \mathbf{b} \cdot \mathbf{c} = 0, \ \mathbf{c} \cdot \mathbf{a} = 0$ $\mathbf{c}, \mathbf{c} \cdot \mathbf{a} = 0, \ \mathbf{a} \cdot \mathbf{b} = 0$ $\mathbf{c}, \mathbf{c} \cdot \mathbf{a} = 0, \ \mathbf{c} \cdot \mathbf{a} = 0$
- **129.** Angle between the diagonals of a cube is **a.** $\pi/3$ **b.** $\pi/2$ **c.** $\cos^{-1}(1/3)$ **d.** $\cos^{-1}(1/\sqrt{3})$

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130.Consider the two lines

$$L_1: \frac{x+1}{3} = \frac{y+2}{1} = \frac{z+1}{2}$$

and $L_2: \frac{x-2}{1} = \frac{y+2}{2} = \frac{z-3}{3}$

The unit vector perpendicular to both the lines L_1 and L_2 is

a.
$$\frac{-\hat{i}+7\hat{j}+7\hat{k}}{\sqrt{99}}$$
 b. $\frac{-\hat{i}-7\hat{j}+5\hat{k}}{5\sqrt{3}}$
c. $\frac{-\hat{i}+7\hat{j}+5\hat{k}}{5\sqrt{3}}$ d. $\frac{7\hat{i}-7\hat{j}+\hat{k}}{\sqrt{99}}$

- **131.** The distance between the line $\mathbf{r} = 2\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}} + \lambda(\hat{\mathbf{i}} - \hat{\mathbf{j}} + 4\hat{\mathbf{k}})$ and the plane $\mathbf{a} \cdot (\hat{\mathbf{i}} + 5\hat{\mathbf{j}} + \hat{\mathbf{k}}) = 5$ is $\mathbf{a} \cdot \frac{10}{9} \qquad \mathbf{b} \cdot \frac{10}{3\sqrt{3}} \qquad \mathbf{c} \cdot \frac{10}{3} \qquad \mathbf{d}$. None of these
- **132.** Two cards are drawn from a pack of 52 cards. What is the probability that either both are red or both are kings?
 - a. 7/13 b. 63/221 c. 55/221 d. 3/26
- **133.** If A and B are two independent events such that $P(A) = \frac{1}{2}$ and $P(B) = \frac{1}{5}$, then which of the following is correct? **a.** $P\left(\frac{A}{B}\right) = \frac{1}{2}$ **b.** $P\left(\frac{A}{A \cup B}\right) = \frac{5}{6}$ **c.** $P\left(\frac{A \cap B}{A' \cup B'}\right) = 0$ **d.** All of these
- **134.** Box I contains 5 red and 2 blue balls, while box II contains 2 red and 6 blue balls. A fair coin is tossed. If it turns up head, a ball is drawn from box I, else a ball is drawn from box II. The probability ball drawn is from box I, if it is blue, is
 - a. 27/56 b. 8/29 c. 21/29 d. 29/56
- **135.** For a random variable X, E(X) = 3 and $E(X^2) = 11$. The variable of X is **a**, 8 **b**, 5 **c**, 2 **d**, 1
- **136.** The sum of 10 items is 12 and the sum of their squares is 18, then the standard deviation will be

 a. -3/5
 b. 6/5
 c. 4/5
 d. 3/5
- **137.** The height of the chimney when it is found that on walking towards it 50 m in the horizontal line through its base, the angle of elevation of its

top changes from 30° to 60° is

c.
$$25\sqrt{3}$$
 m d. None of these
138. The value of $\lim_{x\to 0} \frac{\sqrt{1-\cos x^2}}{1-\cos x}$ is
a. $1/2$ b. 2 c. $\sqrt{2}$ d. None of these
139. If $f(x) = \begin{cases} ax^2 + 1, & x \le 1 \\ x^2 + ax + b, x > 1 \end{cases}$ is differentiable at
 $x = 1$, then
a. $a = 1, b = 1$ b. $a = 1, b = 0$
c. $a = 2, b = 0$ d. $a = 2, b = 1$
140. The slope of the tangent to the curve
 $x = t^2 + 3t - 8, y = 2t^2 - 2t - 5$ at the point $t = 2$ is
a. $7/6$ b. $5/6$ c. $6/7$ d. 1
141. $\int \frac{1}{1-2\sin x} dx$ is equal to
a. $\frac{1}{2\sqrt{3}} \log \left| \frac{\tan \frac{x}{2} - 2 - \sqrt{3}}{\tan \frac{x}{2} - 2 + \sqrt{3}} \right| + c$
b. $\frac{\sqrt{3}}{2} \log \left| \frac{\tan \frac{x}{2} - 2 - \sqrt{3}}{\tan \frac{x}{2} - 2 + \sqrt{3}} \right| + c$
d. None of the above
142. $\int_{0}^{1} \frac{\log(1+x)}{1+x^2} dx$ is equal to
a. $\frac{\pi}{8} \log 2$ b. $\frac{\pi}{8} \log \frac{1}{2}$
c. $\frac{\pi}{4} \log 2$ d. None of these

b. 25√2 m

a. 25 m

- **143.** The area of one curvilinear triangle formed by curves $y = \sin x$, $y = \cos x$ and *X*-axis, is *a*. 2 sq units *b*. $(2 + \sqrt{2}) \text{ sq units}$ *c*. $(2 \sqrt{2}) \text{ sq units}$ *d*. None of the above
- **144.** Solution of $\left(\frac{x+y-1}{x+y-2}\right) \frac{dy}{dx} = \left(\frac{x+y+1}{x+y+2}\right)$ given that y = 1 when x = 1 is **a.** $\ln \left| \frac{(x-y)^2 - 2}{2} \right| = 2(x+y)$ **b.** $\ln \left| \frac{(x+y)^2 - 2}{2} \right| = 2(x-y)$

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c.
$$\ln \frac{(x-y)^2 + 2}{2} = 2(x+y)$$

d. $\ln \frac{(x+y)^2 + 2}{2} = 2(x-y)$
145. If $y = \sin\left(2\tan^{-1}\sqrt{\frac{1-x}{1+x}}\right)$, then $\frac{dy}{dx}$ is
a. 1 b. -1 c. $\frac{x}{\sqrt{x^2-1}}$ d. $\frac{-x}{\sqrt{1-x^2}}$

- **146.** The maximum value of the function $y = x(x-1)^2$, is **a**. 0 **b**. 4/27 **c**. -4 **d**. None of these **147.** The solution of $x^3 \frac{dy}{dx} + 4x^2 \tan y = e^x \sec y$
 - satisfying y(1) = 0, is **a.** $\tan y = (x-2)e^x \log x$ **b.** $\sin y = e^x(x-1)x^{-4}$ **c.** $\tan y = (x-1)e^x x^{-3}$ **d.** $\sin y = e^x(x-1)x^{-3}$

148. The runs of two players for 10 innings each are as follows

Α	58	59	60	54	65	66	52	75	69	52
В	94	26	92	65	96	78	14	34	98	13

- The more consistent player is
- a. player A
- **b.** player B
- c. both player A and B
- d. None of the above

149.	The linear program	mming problem minimise
	z = 3x + 2y subjec	t to constraints $x + y \ge 8$,
	$3x + 5y \le 15, x \ge 0$	and $y \ge 0$, has
	a. one solution	b. no feasible solution
	c. two solutions	d. infinitely many solutions

150. Find the area enclosed by the loop in the curve $4y^2 = 4x^2 - x^3$.

a. 128/5 b. 15/128 c. 130/17 d. 17/130

Answers

- 10-1		
- 121	ivs	100
	IVS	

2. (a)	3. (c)	4. (d)	5. (b)	6. (c)	7. (a)	8. (a)	9. (c)	10. (b)
12. (b)	13. (b)	14. (c)	15. (a)	16. (d)	17. (c)	18. (b)	19. (a)	20. (c)
22. (a)	23. (b)	24. (d)	25. (b)	26. (a)	27. (b)	28. (c)	29. (b)	30. (b)
32. (d)	33. (c)	34. (b)	35. (a)	36. (c)	37. (a)	38. (a)	39. (b)	40. (d)
ry		/						
42. (a)	43. (a)	44. (a)	45. (c,d)	46. (a)	47. (a)	48. (a)	49. (a)	50. (d)
52. (b)	53. (a)	54. (a)	55. (c)	56. (a)	57. (b)	58. (a)	59. (b)	60. (c)
62. (a)	63. (c)	64. (c)	65. (a)	66. (a)	67. (a)	68. (a)	69. (a)	70. (c)
72. (a)	73. (c)	74. (d)	75. (c)	76. (a)	77. (c)	78. (b)	79. (d)	80. (a)
Proficienc	ey							
82. (a)	83. (a)	84. (d)	85. (c)	86. (c)	87. (b)	88. (c)	89. (c)	90. (c)
92. (b)	93. (c)	94. (d)	95. (a)					
Reasoning	ç							
97. (c)	98. (b)	99. (d)	100. (c)	101. (b)	102. (a)	103. (b)	104. (d)	105. (c)
atics								
107. (a)	108. (c)	109. (a)	110. (d)	111. (b)	112. (c)	113. (c)	114. (c)	115. (b)
117. (b)	118. (a)	119. (a)	120. (b)	121. (a)	122. (b)	123. (d)	124. (b)	125. (b)
127. (d)	128. (d)	129. (c)	130. (b)	131. (b)	132. (c)	133. (d)	134. (b)	135. (c)
	1.7							
137. (c)	138. (c)	139. (c)	140. (c)	141. (c)	142. (a)	143. (c)	144. (b)	145. (d)
	12. (b) 22. (a) 32. (d) 79 42. (a) 52. (b) 62. (a) 72. (a) Proficience 82. (a) 92. (b) Reasoning 97. (c) atics 107. (a) 117. (b)	12. (b) 13. (b) 22. (a) 23. (b) 32. (d) 33. (c) ry 42. (a) 43. (a) 52. (b) 53. (a) 62. (a) 63. (c) 72. (a) 73. (c) Proficiency 82. (a) 83. (a) 92. (b) 93. (c) Reasoning 97. (c) 98. (b) atics 107. (a) 108. (c) 117. (b) 118. (a)	12. (b) 13. (b) 14. (c) 22. (a) 23. (b) 24. (d) 32. (d) 33. (c) 34. (b) ry 42. (a) 43. (a) 44. (a) 52. (b) 53. (a) 54. (a) 62. (a) 63. (c) 64. (c) 72. (a) 73. (c) 74. (d) Proficiency 82. (a) 83. (a) 84. (d) 92. (b) 93. (c) 94. (d) Reasoning 97. (c) 98. (b) 99. (d) atics 107. (a) 108. (c) 109. (a) 117. (b) 118. (a) 119. (a)	12. (b) 13. (b) 14. (c) 15. (a) 22. (a) 23. (b) 24. (d) 25. (b) 32. (d) 33. (c) 34. (b) 35. (a) ry 42. (a) 43. (a) 44. (a) 45. (c,d) 52. (b) 53. (a) 54. (a) 55. (c) 62. (a) 63. (c) 64. (c) 65. (a) 72. (a) 73. (c) 74. (d) 75. (c) Proficiency 82. (a) 83. (a) 84. (d) 85. (c) 92. (b) 93. (c) 94. (d) 95. (a) Reasoning 97. (c) 98. (b) 99. (d) 100. (c) atics 107. (a) 108. (c) 109. (a) 110. (d) 117. (b) 118. (a) 119. (a) 120. (b) 110. (d)	12. (b) 13. (b) 14. (c) 15. (a) 16. (d) 22. (a) 23. (b) 24. (d) 25. (b) 26. (a) 32. (d) 33. (c) 34. (b) 35. (a) 36. (c) ry 42. (a) 43. (a) 44. (a) 45. (c,d) 46. (a) 52. (b) 53. (a) 54. (a) 55. (c) 56. (a) 62. (a) 63. (c) 64. (c) 65. (a) 66. (a) 72. (a) 73. (c) 74. (d) 75. (c) 76. (a) Proficiency 82. (a) 83. (a) 84. (d) 85. (c) 86. (c) 92. (b) 93. (c) 94. (d) 95. (a) 86. (c) 92. (b) 93. (c) 94. (d) 95. (a) 86. (c) 92. (b) 93. (c) 94. (d) 95. (a) 86. (c) 92. (b) 93. (c) 100. (c) 101. (b) 11. (b) atics 107. (a) 108. (c) 109. (a) 110. (d) 111. (b) 117. (b) 118. (a) 119. (a) 120. (b) 121. (a)	12. (b) 13. (b) 14. (c) 15. (a) 16. (d) 17. (c) 22. (a) 23. (b) 24. (d) 25. (b) 26. (a) 27. (b) 32. (d) 33. (c) 34. (b) 35. (a) 36. (c) 37. (a) ry 42. (a) 43. (a) 44. (a) 45. (c,d) 46. (a) 47. (a) 52. (b) 53. (a) 54. (a) 55. (c) 56. (a) 57. (b) 62. (a) 63. (c) 64. (c) 65. (a) 66. (a) 67. (a) 72. (a) 73. (c) 74. (d) 75. (c) 76. (a) 77. (c) Proficiency S2. (a) S3. (a) 84. (d) 85. (c) 86. (c) 87. (b) 92. (b) 93. (c) 94. (d) 95. (a) <	12. (b) 13. (b) 14. (c) 15. (a) 16. (d) 17. (c) 18. (b) 22. (a) 23. (b) 24. (d) 25. (b) 26. (a) 27. (b) 28. (c) 32. (d) 33. (c) 34. (b) 35. (a) 36. (c) 37. (a) 38. (a) Y 42. (a) 43. (a) 44. (a) 45. (c,d) 46. (a) 47. (a) 48. (a) 52. (b) 53. (a) 54. (a) 55. (c) 56. (a) 57. (b) 58. (a) 62. (a) 63. (c) 64. (c) 65. (a) 66. (a) 67. (a) 68. (a) 72. (a) 73. (c) 74. (d) 75. (c) 76. (a) 77. (c) 78. (b) Proficiency 82. (a) 83. (a) 84. (d) 85. (c) 86. (c) 87. (b) 88. (c) 92. (b) 93. (c) 94. (d) 95. (a) 102. (a) 103. (b) attics 107. (a) 108. (c) 109. (a) 110. (d) 111. (b) 112. (c) 113. (c) 117. (b) 118. (a) 119. (a) 120. (b) 121. (a) 122. (b) 1	12. (b) 13. (b) 14. (c) 15. (a) 16. (d) 17. (c) 18. (b) 19. (a) 22. (a) 23. (b) 24. (d) 25. (b) 26. (a) 27. (b) 28. (c) 29. (b) 32. (d) 33. (c) 34. (b) 35. (a) 36. (c) 37. (a) 38. (a) 39. (b) ry 42. (a) 43. (a) 44. (a) 45. (c,d) 46. (a) 47. (a) 48. (a) 49. (a) 52. (b) 53. (a) 54. (a) 55. (c) 56. (a) 57. (b) 58. (a) 59. (b) 62. (a) 63. (c) 64. (c) 65. (a) 66. (a) 67. (a) 68. (a) 69. (a) 72. (a) 73. (c) 74. (d) 75. (c) 76. (a) 77. (c) 78. (b) 79. (d) Proficiency 82. (a) 83. (a) 84. (d) 85. (c) 86. (c) 87. (b) 88. (c) 89. (c) 92. (b) 93. (c) 94. (d) 95. (a) 104. (d) Interval Interval 100. (c) 101. (b) 102. (a)

Hints & Solutions

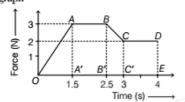
Physics

1. (a) Work done in the cyclic process

= Area of the loop ABCD

 $= (2p - p) \times (2V - V) = pV$

 (a) Impulse of a force = Area between the force-time graph



Hence, impulse of force = area of $\Delta OA'A$ + area of rectangle A'B'BA + area of trapezium BB'C'C + area of rectangle CC'ED

$$= \frac{1}{2} \times 15 \times 3 + 1 \times 3 + \frac{1}{2}(3+2)(3-25) + 2 \times 1$$

= 2.25 + 3 + 1.25 + 2
= 850 Ns

 $B = \frac{\text{Hydraulic stress}}{\Delta V}$

3. (c) Bulk modulus = $\frac{\text{Hydraulic stress}}{\text{Volumetric strain}}$

or
$$\frac{\Delta V}{V} =$$
 Hydraulic stress $\times \frac{1}{B}$
 \therefore For constant hydraulic stress, $\frac{\Delta V}{V} \propto \frac{1}{B}$

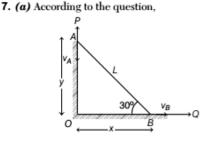
- 4. (d) A shunt is a low resistance which is connected in parallel with a galvanometer (or ammeter) to protect it from large current and to increase the range of ammeter.
- (b) There is a phase difference of 180° between the signal voltage and output voltage in a common emitter amplifier. It is also known as phase reversal.
- (c) (n + 1)th divisions of vernier scale = n division of main scale

$$\therefore$$
 1 VSD = $\frac{n}{n+1}$ MSD

Least count = 1 MSD - 1 VSD

$$= 1 \text{ MSD} - \frac{n}{n+1} \text{ MSD} = \frac{1}{n+1} \text{ MSD}$$
$$= \frac{1}{n+1} \times a \text{ units} = \frac{a}{n+1} \text{ units}$$

[:: given, 1MSD= a units]



Let OB = x, OA = y and $x = L \cos \theta$ So, by Pythagoras theorem,

$$\Rightarrow \qquad x^2 + y^2 = L^2$$

Differentiating w.r.t. t, we get

$$2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$$

$$2x v_B + 2y v_A = 0 \quad \left[\because \frac{dx}{dt} = v_B \text{ and } \frac{dy}{dt} = v_A \right]$$

$$\Rightarrow \quad v_A = -\frac{x}{y} v_B$$

$$\Rightarrow \quad |v_A| = \frac{x}{y} v_B = v_B \cot\theta \quad \left[\because \frac{x}{y} = \cot\theta \right]$$

$$= \sqrt{3} \times \cot 30^\circ$$

$$= \sqrt{3} \times \frac{1}{\sqrt{3}} = 1 \text{ m/s}$$

8. (a) Let k be the force constant of spring.

Time period,
$$T = 2\pi \sqrt{\frac{M}{k}}$$
 ...(i)

When block of mass *m* is placed in the tray, the time period of oscillations becomes

$$T' = 2\pi \sqrt{\frac{M+m}{k}} \qquad \dots (ii)$$

On dividing Eq. (ii) by Eq. (i), we get

$$\Rightarrow \qquad \frac{T'}{T} = \frac{\sqrt{M} + m}{\sqrt{M}}$$

$$\Rightarrow \qquad \frac{3}{15} = \sqrt{\frac{12 + m}{12}} \qquad \begin{bmatrix} \text{where, } M = 12 \text{ kg,} \\ T = 1.5 \text{ s} \\ \text{and } T' = 3 \text{ s,} \end{bmatrix}$$

$$\Rightarrow \qquad \sqrt{\frac{12 + m}{12}} = 2$$

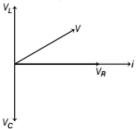
$$\Rightarrow \qquad 12 + m = 48$$

$$\Rightarrow \qquad m = 36 \text{ kg}$$

9. (c) As shown in phasor diagram, voltage leads the current.

As in purely inductive circuit, current lags behind the voltage by an angle of 90°, here angle is not 90° but it is lesser than that.

So, this type of case arise in *R-L-C* circuit when *R-L-C* load with inductive reactance X_L is more than the capacitive reactance X_C as shown below.



10. (b) Given,

$$Y = \sin\left[\pi\left(\frac{t}{5} - \frac{x}{9}\right) + \frac{\pi}{6}\right] \text{cm} \qquad \dots(i)$$

The general equation of progressive wave is

$$Y = A \sin \left[2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) + \phi \right] \operatorname{cm} \qquad \dots \text{(ii)}$$

On comparing Eq. (i) with Eq. (ii), we get

$$A = 1 \text{ cm}, f = \frac{1}{T} = \frac{1}{10} = 0.1 \text{ Hz}$$

and
$$\frac{2\pi}{\lambda} = \frac{\pi}{9}$$

 $\Rightarrow \lambda = 18 \text{ cm}$

$$v = f\lambda = 0.1 \times 18 = 1.8 \text{ m/s}$$

- 11. (a) In fibre optic communication, signals are transmitted through an optical fibre. The property of light used in transmission through optical fibre cables is total internal reflection.
- 12. (b) Distance moved by man in 5 min with velocity of 45 m/s is

Distance = Speed × Time

= 45 m/s
$$\times$$
 (5 \times 60) s

= 13500 m

When he move back, it covers the same distance to come back to its original position. Now, time taken = 15 min

 $= 15 \times 60 \text{ s} = 90 \text{ s}$

Distance travelled = 13500 m

$$\therefore \text{ Speed} = \frac{\text{Distance}}{\text{Time}} = \frac{13500}{90} = 150 \text{ m/s}$$

13. (b) Potential at point P due to the solid sphere,

$$V_1 = -\frac{GM}{2R^3} \left[3R^2 - \left(\frac{R}{2}\right)^2 \right]$$

$$=-\frac{11 GM}{8B}$$

Potential at point P due to the cavity part,

$$V_2 = -\frac{3}{2} \frac{G\left(\frac{M}{8}\right)}{\frac{R}{2}} = -\frac{3GM}{8R}$$

Potential due to the remaining part at point *P*,

⇒

$$V = V_1 - V_2 = \frac{-11GM}{8R} + \frac{3GM}{8R}$$
$$V = -\frac{GM}{R}$$

14. (c) Consider the equilibrium of charge Q at corner A

$$F_{O} = \frac{kQ^{2}}{(\sqrt{2}a)^{2}}$$

$$F_{O} = \frac{kQ^{2}}{(\sqrt{2}a)^{2}} = \frac{kQ^{2}}{a^{2}}$$

$$F_{O} = \frac{kQ^{2}}{(\sqrt{2}a)^{2}}$$

$$F_{O} = \frac{kQq}{(\sqrt{2}a)^{2}} = \frac{kQq}{a^{2}}$$

$$F_{O} = \frac{kQq}{(\sqrt{2}a)^{2}}$$

For equilibrium of charge Q at corner A, the net force on this charge along AC must be zero.

$$F_{O} = F_{C} + F_{B} \cos 45^{\circ} + F_{D} \cos 45^{\circ}$$

$$= F_{C} + 2F_{B} \cos 45^{\circ} \qquad [\because F_{B} = F_{D}]$$

$$= F_{C} + 2F_{B} \times \frac{1}{\sqrt{2}} \qquad [\because \cos 45^{\circ} = \frac{1}{\sqrt{2}}]$$

$$\Rightarrow \frac{k}{a^{2}} \frac{2Qq}{2a^{2}} = \frac{kQ^{2}}{2a^{2}} + \frac{2 \times kQ^{2}}{a^{2}} \times \frac{1}{\sqrt{2}}$$

$$\Rightarrow 2Qq = \frac{Q^{2}}{2} + \frac{Q^{2}}{\sqrt{2}} \times 2$$

$$\Rightarrow 2q = \frac{Q}{2} + Q\sqrt{2}$$

$$\Rightarrow q = \frac{Q}{4}(1 + 2\sqrt{2})$$

15. *(a)* Work done by the particle in *x*-direction is given by

$$dW = F \, dx = (a + bx) \, dx$$

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Total work done in displacement from
$$x = 0$$
 to $x = d$ will be

$$W = \int dW = \int_{0}^{d} (a + bx) \, dx = \left[ax + \frac{bx^2}{2}\right]_{0}^{d}$$
$$\Rightarrow W = \left(a + \frac{bd}{2}\right)d$$

1 .

16. (d) Kinetic energy of a proton is given by

=

⇒

$$E = \frac{1}{2} m_p v_p^2$$

$$\Rightarrow \qquad E = \frac{p^2}{2m_p} \qquad [\because p = mv]$$

$$\Rightarrow \qquad p = \sqrt{2m_p E}$$

d

....(i)

: Wavelength of proton is, $\lambda_1 = h/p$

$$\Rightarrow \qquad \lambda_1 = \frac{h}{\sqrt{2m_pE}}$$

Now, energy of photon is given by L.

$$E = hv_2 \implies E = \frac{hc}{\lambda_2}$$
$$\lambda_2 = \frac{hc}{E} \qquad \dots (ii)$$

where, λ_2 is wavelength of photon.

On dividing Eq. (ii) by Eq. (i), we get

$$\frac{\lambda_2}{\lambda_1} = \frac{hc}{E} \times \frac{\sqrt{2m_pE}}{h}$$

$$\Rightarrow \qquad \frac{\lambda_2}{\lambda_1} = \frac{c}{\sqrt{E}} \sqrt{2m_p} \Rightarrow \quad \frac{\lambda_2}{\lambda_1} \propto E^{-1/2}$$

17. (c) The FBD of block of mass 10 kg is

$$mg \sin 30^\circ$$
 $mg \cos 30^\circ$

For the equilibrium of block, the frictional force must balanced the sine component of mg.

$$= 10 \times 9.8 \times \frac{1}{2} = 49 \text{ N}$$

18. (b) Conductivity (σ) of a metallic conductor is given by

 $f = mg \sin 30^{\circ}$

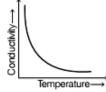
$$\sigma = \frac{1}{\rho} = \frac{ne^2\tau}{m}$$

where, ρ = resistivity of conductor, τ = relaxation time,

n = number of free electronsm = mass.

and

For metals, as the temperature increases, the relaxation time τ decreases because collisions become more frequent. Hence, the conductivity of a metallic conductor decreases with the increases of temperature.



19. (a) Given, radius of hydrogen atom,
$$r = 25 \times 10^{-13}$$
 m
Volume of one atom, $V = \frac{4}{3}\pi r^3$
Number of atoms in 1 mole = 6.023×10^{23}
Volume of 1 mole of H-atoms = $N \times \frac{4}{3}\pi r^3$
= $6.023 \times 10^{23} \times \frac{4}{3} \times 3.14 \times (25 \times 10^{-13})^3$
= 3.94×10^{-14} m³
20. (c) Given, $m = 1$ kg, $\mathbf{r} = 3t$ $\hat{\mathbf{i}} + 4\hat{\mathbf{j}}$
Velocity of body, $\mathbf{v} = \frac{d\mathbf{r}}{dt} = \frac{d}{dt}(3t\hat{\mathbf{i}} + 4\hat{\mathbf{j}})$
 $\Rightarrow \mathbf{v} = 3\hat{\mathbf{i}}$
Angular momentum, $\mathbf{L} = m(\mathbf{r} \times \mathbf{v})$
= $1 \times [(3t\hat{\mathbf{i}} + 4\hat{\mathbf{j}}) \times 3\hat{\mathbf{i}}]$
 $= \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 3t & 4 & 0 \\ 3 & 0 & 0 \end{vmatrix}$
= $[3t \times 0 - 4 \times 3]\hat{\mathbf{k}}$
 $\Rightarrow \mathbf{L} = -12\hat{\mathbf{k}}$ J-s

of g at equator is expl $g_e = g - R\omega^2 \cos \phi = g - R\omega^2$ $[:: \cos \phi = 1]$ Change in value of g is $g - g_e$

$$= R\omega^{2} = R \left(\frac{2\pi}{T}\right)^{2}$$
$$= 6.4 \times 10^{6} \times \left[\frac{2\pi}{24 \times 60 \times 60}\right]^{2}$$
$$= 3.37 \times 10^{-2} \text{ m/s}^{2} \approx 3.4 \text{ cm/s}^{2}$$

22. (a) Apparent frequency of car A = Apparent frequency of car B

$$\Rightarrow \frac{v}{v - v_s} \times v = \frac{v}{v - v_{s'}} \times v'$$
$$\Rightarrow \frac{v}{v - 15} = \frac{504}{v - 30}$$

$$\Rightarrow \qquad \qquad \nu = \frac{340 - 15}{340 - 30} \times 504 \begin{bmatrix} \because \text{ velocity of sound} \\ \text{in air is } 340 \text{ m/s.} \end{bmatrix}$$

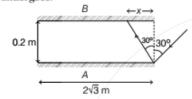
$$\Rightarrow$$
 v = 529.2 Hz

23. (b) Using KCL, I_{DC} = 3 - 1 = ZA

Using Kirchhoff's loop law, in loop BDCR1 B, we get $2 \times 2 + 3R_1 = 4$ or $R_1 = 0$

 $V_B = V_C = 2 + V_A$ ⇒ $[\because V_A = 0]$ = 2 + 0 $V_B = 2V$ ⇒

24. (d) Let N be the maximum number of reflection that ray undergoes.



Suppose it covers x distance in one reflection, then

$$Nx = 2\sqrt{3}$$

$$\Rightarrow \qquad N = \frac{2\sqrt{3}}{x} = \frac{2\sqrt{3}}{0.2 \tan 30^{\circ}} \quad [\because x = 0.2 \tan 30^{\circ}]$$

$$N = \frac{6}{0.2} = 30$$

Number of reflections ray undergoes before it emerges excluding the first one are N - 1

$$= 30 - 1 = 29$$

25. (b) According to equation of motion, in vector from, $\mathbf{v} = \mathbf{u} - gt \hat{\mathbf{j}}$

$$\Rightarrow \qquad \mathbf{v} = \hat{\mathbf{i}} + \hat{\mathbf{j}} - 10t \hat{\mathbf{j}}$$

Integrating w.r.t. *t* both sides, we get

ing w.r.t. t both sides, we get $\mathbf{r} = \int \mathbf{v} \, dt = \int (\hat{\mathbf{i}} + \hat{\mathbf{j}} - 10t \, \hat{\mathbf{j}}) \, dt$

⇒

.: On comparing, we get

and
$$x = t$$

 $y = t - 5t^2$

and

$$\Rightarrow \qquad y = x - 5x^2$$

This is the required equation of trajectory of particle. 26. (a) Volume of bigger drop = Volume of two smaller

 $\hat{x}\hat{i} + y\hat{j} = t\hat{i} + t\hat{j} - 5t^2\hat{j} = t\hat{i} + (t - 5t^2)\hat{j}$

$$\Rightarrow \frac{4}{3}\pi R^{\prime 3} = 2 \times \frac{4}{3}\pi R^{3}$$

where, R' is the radius of bigger drop.

$$\Rightarrow \qquad R^{\prime 3} = 2R^{3}$$
$$\Rightarrow \qquad R^{\prime} = 2^{1/3} R$$

Initial surface energy of two small drops,

$$U_1 = 8\pi R^2 \sigma$$
 ...(i)

Final surface energy of big drop, $U_2 = 4\pi R'^2 \sigma$

$$= 4\pi \times 2^{2/3} R^2 \sigma$$

$$\frac{U_2}{U_1} = \frac{4\pi \times 2^{2/3} R^2 \sigma}{8\pi R^2 \sigma} = \frac{2^{2/3}}{2} = \frac{2^{-1/3}}{1}$$

Ratio of surface energy of bigger drop to smaller one is 2^{-1/3} : 1.

27. (b) Force on charge particle in magnetic field is balanced by centripetal force, so $\frac{mv^2}{r} = qvB\sin 90^\circ$

 $[\theta = 90^\circ$, therefore magnetic field is perpendicular]

$$= qvB$$
 [sin 90° = 1]
 mv

[given]

 mv^2

Therefore,
$$r \propto mv$$

or $\frac{r_A}{r_B} = \frac{m_A v_A}{m_B v_B}$
As, $r_A > r_B$
 $\Rightarrow m_A v_A > m_B v_B$

28. (c) Minimum wavelength for X- ray is given by

$$\lambda_{\min} = \frac{12375}{V} \text{\AA}$$

As the accelerating voltage V is decreased, λ_{min} increases.

The intensity of emitted radiation is determined by the number of electrons bombarding the target.

. Accelerating voltage does not change the intensity of X-rays emitted.

29. (b) As we know,
$$C_V = \frac{n}{2}R$$
 ...(i)

$$C_p = \left(\frac{n}{2} + 1\right)R \qquad \dots (ii)$$

On dividing Eq. (ii) by Eq. (i), we get

$$\frac{C_p}{C_V} = \gamma = \frac{\left(\frac{n}{2}+1\right)}{\frac{n}{2}} = 1 + \frac{2}{n}$$
$$\frac{C_p}{C_V} = \gamma = 1 + \frac{2}{n}$$

30. (b) Given, v = 6 m/s, r = 18 m, $g = 9.8 \text{ m/s}^2$

Now, the velocity of cyclist is given by

$$v^2 = rg \tan \theta$$
 or $\tan \theta = \frac{v^2}{rg} = \frac{6 \times 6}{18 \times 9.8}$

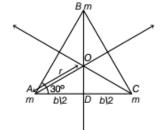
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 \Rightarrow

 $[:: \cos \omega t = 1]$

 $\mu = tan \theta$ $\mu = 0.2041$

31. (b) Let us consider an equilateral
$$\triangle ABC$$
 of side b



From figure,

-

2

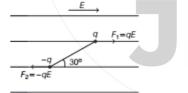
In
$$\triangle AOD$$
, $\cos 30^\circ = \frac{AD}{AO}$
 $\Rightarrow \qquad \frac{\sqrt{3}}{2} = \frac{b}{\frac{2}{r}}$ $\left[\because \cos 30^\circ = \frac{\sqrt{3}}{2}\right]$
 $\Rightarrow \qquad r = \frac{b}{2} \times \frac{2}{\sqrt{3}} = \frac{b}{\sqrt{3}}$

Moment of inertia about line passing through centroid,

 $I = 3 \times mr^2$ [due to 3 masses present in system]

$$\Rightarrow = 3 \times m \times \left(\frac{b}{\sqrt{3}}\right)^2$$
$$\Rightarrow I = mb^2$$

32. (d) When a dipole is placed in a non-uniform electric field, opposite charges of the dipole experiences a force due to E. It is as shown in the figure below



These forces will act in opposite direction. Now, since the electric field is not uniform, so the force experienced by the charges will be unequal.

Hence, their will be a net force acting on the dipole, as they do not cancel each other.

Also, forces on the charges are not linear as shown above. So, they will experience a not non-zero torque. Hence, the dipole will experience both translational force and torque in a non-uniform electric field.

33. (c) Induced emf,
$$\varepsilon = -M \frac{di}{dt}$$

where, *i* is given as, $i = i_0 \sin \omega t$

⇒

⇒ ⇒

 \Rightarrow

$= M i_0 \omega \cos \omega t$

 $\varepsilon = -M \frac{d}{dt} [i_0 \sin \omega t]$

For maximum value of emf in second coil, cos wt is maximum, i.e. 1.

$$E_{max} = M i_0 \omega$$

= 0.001 × 10 × 10 π

 $E_{\text{max}} = 0.1 \ \pi \text{V}$

Hence, maximum emf value induced in second coil is 0.1 πV.

34. (b) Diode D1 does not conduct because it is connected in reversed biased position.

Hence, only D2 conducts as it is forward biased.

∴ Current in circuit is given by

$$i = \frac{V}{R} = \frac{5}{30 + 20} = \frac{5}{50} A$$

$$\Rightarrow$$
 $i = 0.1 \text{ A}$
35. (a) Kinetic energy at $Q = 90\%$ of potential energy at P

$$\Rightarrow \frac{1}{2}mv^2 = \frac{90}{100} \times mgh$$
$$\Rightarrow v = \sqrt{1.8gh} \Rightarrow v = \sqrt{1.8 \times 10 \times 2}$$

v = 6 m/s**36.** (c) Let displacement, $x = A \sin \omega t$

Velocity, $v = \frac{dx}{dt} = A\omega \cos \omega t$

Kinetic energy of particle in SHM,

$$K = \frac{1}{2}mv^2 \implies K = \frac{1}{2}m\omega^2 A^2 \cos^2 \omega t$$
$$= \frac{1}{2}m\omega^2 A^2 \left(\frac{1+\cos 2\omega t}{2}\right) \qquad \begin{bmatrix} \because \cos^2 \theta \\ = \frac{1+\cos 2\theta}{2} \end{bmatrix}$$
$$= \frac{1}{4}m \,\omega^2 A^2 (1+\cos 2\omega t)$$

 \therefore New angular frequency, $\omega_K = 2\omega$

. Frequency of oscillation of kinetic energy = 2

$$f \qquad \left[\because f = \frac{\omega}{2\pi} \right]$$

37. (a) According to law of radioactivity, the rate of disintegration is given as

$$R = \lambda N = \lambda N_0 e^{-\lambda t}$$

Given,
$$R = 5000$$

 $\Rightarrow 5000 = \lambda N_{-} e^{-\lambda t}$

$$\Rightarrow 5000 = \lambda N_0 e^{-\lambda t} \qquad ...(i)$$
After 5 min, $R = 1250$

$$\therefore \quad 1250 = \lambda N_0 e^{-\lambda(t+5)} \qquad \dots (ii)$$

 $\left[\because m = \frac{M}{l} \right]$

On dividing Eq. (i) by Eq. (ii), we get

$$\frac{5000}{1250} = \frac{e^{-\lambda t}}{e^{-\lambda(t+5)}} \implies 4 = e^{5\lambda}$$
Taking log both sides, we get
$$\log_e 4 = \log_e(e^{5\lambda})$$

$$\Rightarrow \qquad \log_e 4 = 5\lambda$$

$$\Rightarrow \qquad \lambda = \frac{1}{5}\log_e 2^2$$

$$\Rightarrow \qquad \lambda = 0.4\log_e 2$$

38. (a) In a uniform electric field, potential difference across two parallel plates of capacitor, V = Ed

where, E is electric field and d is separation between plates.

$$V = 2000 \times (1 \times 10^{-3}) = 2V$$

39. (b) When light travel in meta-material, physical characteristics remain unchanged.

 $v = \frac{c}{|n|}$

where, |n| is the relative refractive index of meta-material.

 $|n| = \frac{c}{c}$

As,

⇒ =

⇒

⇒

....

Chemistry

- 41. (a) o-nitrophenol forms intramolecular H-bonding whereas molecules of p-nitrophenol get associated through intermolecular H-bond. ... o-nitrophenol is the most volatile compound.
- 42. (a) The magnetic moment is given by
 - $\mu = \sqrt{n(n+2)}$ BM.

(where, n = number of unpaired electron). Electronic configuration of

$$Ti^{2+}(22): 1s^2 2s^2 2p^6 3s^2 3p^6 3d^2$$

: Number of unpaired electrons = 2

:.
$$\mu = \sqrt{2(2+2)} = \sqrt{8}$$

r =

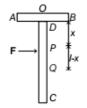
- 43. (a) Only Xe can form compounds with fluorine among noble gases because, Xe is large in size and have high atomic mass. Due to having larger atomic radius the force of attraction between the outer electrons and protons in the nucleous is weaker. Hence, they are easily available to form compound.
- 44. (a) Helium is used as a cryogenic agent due to its very low boiling point.

45. (c,d) The rate of reaction for the given reaction is

$$= -\frac{1}{2}\frac{d[A]}{dt} = -\frac{1}{3}\frac{d[B]}{dt} = \frac{1}{3}\frac{d[C]}{dt} = \frac{1}{4}\frac{d[D]}{dt}$$

$$\Rightarrow \quad |n| = \frac{\lambda_{air}}{\lambda_{med}} \quad \Rightarrow \quad \lambda_{med} = \frac{\lambda_{air}}{|n|}$$

40. (d) Let O be the centre of mass of part AB and Q that of CD. Let M be the mass per unit length of the parts AB and CD.



As, no rotation is set up about point P, so moment of part AB about P = moment of part CD about P

or
$$(ml) x = (2 ml) (l-x)$$

or $x = 2l - 2x$
or $x = \frac{2l}{3}$

Distance of P from the end

$$C = 2l - x = 2l - 2l/3 = 4l/3$$

46. (a) Cyclohexanol on reaction with H₂SO₄ and heating gives cyclohexene as follows

47. (a) Addition of HCl to 3-methylbutene gives 2-chloro-2-methylbutane as major product. The mechanism reaction is as follows

$$\begin{array}{c} CH_3 & CH_3 \\ | \\ CH_3 - CH - CH = CH_2 + H^+ \longrightarrow CH_3 - CH - CH - CH_3 \\ \\ Rearrangement \end{array}$$

$$CH_3$$
 CH_3
 H_3 CH_3 CH_3
 CH_3 CH_2 CH_3 CH_3 CH_2 CH_3
 CH_3 CH_3 CH_2 CH_3 CH_2 CH_3
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48. (a) Energy for atom, $E \propto \frac{Z^2}{z^2}$ For hydrogen, Z = 1, n = 1

For lithium Z = 3, n = ?

.:. For same energy,

$$E_{\rm H} = E_{\rm Li} \implies \frac{Z_{\rm H}^2}{n_{\rm H}^2} = \frac{Z_{\rm Li}^2}{n_{\rm Li}^2}$$

$$\therefore \quad n_{\rm Li}^2 = \frac{Z_{\rm Li}^2 \times n_{\rm H}^2}{Z_{\rm H}^2} \implies n_{\rm Li}^2 = \frac{3^2 \times 1}{1}$$
$$n_{\rm Li} = 3$$

While angular momentum $(nh/2\pi)$ is independent of atomic number.

∴ For 3*s*-orbital of lithium atom, energy and angular momentum is equal to that of 1*s* orbital of hydrogen atom.

49. (a) Sodium iodide reacts with ammonia to produce tetraamminesodium iodide. The reaction is conducted in liquid ammonia. The reaction is as follows

$$NaI + 4NH_3 \longrightarrow [Na(NH_3)_4] I$$

Sodium Ammonia
iodide Tetraammine-
sodium iodide

- **50.** *(d)* Sodium or ammonium thiosulphate is used as a fixing agent in photography. They converts the silver halide into soluble, complex silver salts that dissolve in the fixer. During this process the film loses its original silver halide milkiness overlaying the image and becomes clear.
- 51. (d) Epoxy ethane reacts with ammonia forming a mixture of mono, di, tri-ethanol amines, in presence of small amount of water as follows.

$$\begin{array}{c} O\\ nH_2C & \hline CH_2 + NH_3 & \rightarrow H_2N - CH_2 - CH_2 - OH\\ Mono ethanol amine \\ + HO - CH_2 - CH_2 - N - CH_2 - CH_2 - OH\\ Diethanol amine \\ + \\ HO - CH_2 - CH_2 - N - CH_2 - CH_2 - OH\\ CH_2 \\ \downarrow \\ CH_2 \\ \downarrow \\ OH\\ Tri-ethanol amine \end{array}$$

- **52.** *(b)* Dialysis is a process of removing excess electrolyte from colloidal solution by means of diffusion through a suitable membrane.
- (a) Maltase converts maltose into glucose by hydrolysis as follows

- 54. (a) Starch is a polymer of glucose in which glucopyranose units are bonded by α -linkage. It is made up mixture of amylose and amylopectin.
- 55. (c) Methyl alcohol can be distinguished from ethyl alcohol by iodoform test as follows by using sodium hydroxide and iodine.

$$C_2H_5OH \xrightarrow{\text{NaOH/1}_2} CHI_3 \text{ (yellow ppt.)}$$

 $CH_3OH \xrightarrow{\text{NaOH/1}_2} \text{No ppt.}$

- 56. (a) Sodium stearate (C₁₇H₃₅COO⁻Na⁺) is an anionic soap. Anionic part of sodium stearate is involved in cleansing action.
- 57. (b) BaF₂ is not an anti-fluorite structure. It is of AB₂ type i.e. fluorite (CaF₂) structure. While Rb₂S, K₂O and Li₂O are anti-fluorite structures.
- 58. (a) The shape of ClF₃ is as follows



1-shape structure

It has two lone pairs at equatorial position.

- **59.** (b) Molecular electronic configuration for given species are
 - (a) $O_2 = \sigma \, 1 \, s^2 \, \sigma^* 1 \, s^2 \, \sigma 2 s^2 \, \sigma^* 2 s^2 \, \sigma \, 2 p_x^2 \, \pi \, 2 p_y^2 \, \pi 2 p_z^2$ $\pi^* 2 p_y^1 \, \pi^* 2 p_z^1$
 - It has two unpaired electrons.
 - (b) O₂²⁻ : It has no unpaired electron.
 - (c) N₂²⁺ : It has one unpaired electron.
 - (d) B₂: It has two unpaired electrons.
 ∴ O₂^{2−} is diamagnetic in nature.
- **60.** (c) Bond order for the various compounds are as follows

For SO2,

Number of bonds = 4
Number of (SO) groups = 2
$$\cdot$$
 Bond order = $\frac{4}{2}$ = 2

For SO₃,

Number of bonds = 6 Number of (SO) groups = 3

:. Bond order =
$$\frac{6}{3} = 2$$

For SO₄²⁻,

Number of bonds = 6 Number of (SO) groups = 4 19

$$\therefore \text{ Bond order} = \frac{6}{4} = 1.5$$

For SO₃²⁻,

Ó

Number of bonds = 4 Number of (SO) groups = 3

$$\therefore$$
 Bond order = $\frac{4}{3}$ = 1.33

Hence, correct order is $SO_2 = SO_3 > SO_4^{2-} > SO_3^{2-}$.

61. (b) The energy required for ionisation H-atom is given by, $E = \frac{-kZe^2}{2}$

where, Z = atomic number e = charge on proton/electronr = radius of that electron

$$\therefore \qquad E \propto \frac{1}{r} \text{ or } E \propto r^{-1}$$

$$\therefore \qquad n = -1$$

- **62.** (*a*) BHA is antioxidant (i.e. prevent oxidation). It help in food preservation by retarding the action of oxygen on food. As it is more reactive towards oxygen than the food material.
- 63. (c) In MnO₄,

$$x + (-2)4 = -1 \implies x = +7$$

25 Mn⁺⁷ = [Ar], no unpaired electrons.

Thus, it will not show *d-d* transition. It is dark purple coloured due to charge transfer from ligand to metal.

- 64. (c) Rutherford model could not explain, the
 - (a) electronic structure of an atom.
 - (b) stability of an atom.
- 65. (a) The oxidation state of Ni in [Ni(CO)₄] is 0. The electronic configuration of Ni is 3d⁸ 4s².

Ni (ground state) = 1 1 1 1 1

As CO is a strong ligand, pairing of electrons occur.

$$Ni(CO)_4 = \boxed{1 \ 1 \ 1 \ 1 \ 1 \ 1} \qquad \underbrace{4s}_{sp^3}$$

As, it has *sp*³ hybridisation, so the geometry is tetrahedral. Since, it has no unpaired electrons. So, the complex is diamagnetic.

- 66. (a) The SI unit of Boltzmann's constant is JK⁻¹.
- (a) Acetone does not undergo substitution reaction because it does not contain suitable leaving group.

58. (a) Oxidation number of Co in
$$[\operatorname{CoF}_6]^{2^-}$$

 $x + (-1 \times 6) = -2$
 \therefore $x = 4$
 \therefore Electronic configuration of Co^{4+} ,
 $\operatorname{Co}^{4+} = [\operatorname{Ar}] 3d^5$
 $\operatorname{Co}^{4+} = \boxed{11111111}$

- ∴ Number of unpaired electrons = 5 ∴ Magnetic moment = $\sqrt{n(n+2)} = \sqrt{5 \times 7} = \sqrt{35}$ BM
- **69.** (a) Heavy water is used as a moderator in nuclear reactors. It has higher boiling point compare to ordinary water, thus it is more associated as compared to ordinary water. Dielectric constant of $H_2O > D_2O$. Therefore H_2O is more effective solvent.
- 70. (c) According to sequence rule, the priority order is Cl>C₂H₅ > CH₃ > H, so in R configuration.

(1) Cl

(1)

71.

$$C_2H_5\downarrow$$

 $| (3)$
 $-C-CH_3$ *R*-configuration
 $H^{(4)}$

(c) Molecular mass
=
$$\frac{\text{Weight of organic substance taken}}{\text{Air displaced at STP}} \times 22400$$

 $=\frac{0.2}{56} \times 22400 = 80$

72. (a)
$$C_2H_5OH(l) + 3O_2(g) \longrightarrow 2CO_2(g) + 3H_2O(l)$$

$$\Delta U = -1364.47 \text{ kJ/mol},$$

$$\Delta n_g = -1, T = 25^{\circ}\text{C} = 298 \text{ K}$$

$$\Delta H = \Delta U + \Delta n_g RT$$

$$\Delta H = 1004.47 \text{ /} -1 \times 8.314 \text{ x}$$

298

5. (c) (a)
$$\Delta G = \Delta H - I \Delta S$$

For a system, total entropy change is ΔS_{total}

$$\Delta H_{\text{total}} = 0$$

 $\Delta G_{\text{system}} = -T\Delta S_{\text{tot}}$
 $\Delta G_{\text{system}} = -T$

$$\Delta S_{total}$$

Thus, (a) is true,

...

(b) For isothermal reversible process, $\Delta E = 0$. By first law of thermodynamics,

$$\Delta E = q \times W$$

$$\therefore \qquad W_{\text{reversible}} = -q = -\int_{V_t}^{V_f} p \ dV$$

$$W_{\text{reversible}} = -nRT \ln \frac{V_f}{V_t}$$

Thus, (b) is also true. (c) $\Delta G^{\circ} = \Delta H^{\circ} - T\Delta S^{\circ}$ $\Delta G^{\circ} = -nRT \text{ In } K = -RT \text{ In } K \text{ (for } n = 1)$ $\therefore \qquad -RT \text{ In } K = \Delta H^{\circ} - T\Delta S^{\circ}$ $\therefore \qquad \text{ In } K = -\left(\frac{\Delta H^{\circ} - T\Delta S^{\circ}}{RT}\right)$

Thus, (c) is false. (d) $\Delta G^{\circ} = -RT \ln K$ $\therefore \ln K = -\frac{\Delta G^{\circ}}{RT}$ $\therefore K = e^{-\Delta G^{\circ}/RT}$

Thus, (d) is also true.
74. (d)
$$Pb(OH)_2 \longrightarrow Pb^{2+} + 2OH^-$$

 $K_{sp} = [Pb^{2+}] [OH^-]^2 = S \times (2S)^2$

$$K_{en} = 4S^3$$

$$= 4 \times (6.7 \times 10^{-6})^3 = 1.20 \times 10^{-15}$$

In a solution with pH = 8

$$[H^+] = 10^{-8} \text{ and } [OH^-] = 10^{-6}$$

1.20×10⁻¹⁵ = $[Pb^{2+}] [10^{-6}]^2$

$$[Pb^{2+}] = \frac{1.2 \times 10^{-15}}{[10^{-6}]^2} = 1.2 \times 10^{-3} M$$

75. (c) Molarity

 $=\frac{10 \times \text{density} \times \text{percentage weight of solute}}{\text{molecular weight of the solute}}$

$$\Rightarrow$$
 Density = $\frac{3.60 \times 98}{10 \times 29}$ = 1.216 = 1.22 g mol⁻

$$\therefore \qquad \frac{p - p_s}{p} = \frac{n}{n + N} = \frac{w/m}{\frac{w}{m} + \frac{W}{M}} \Rightarrow \frac{w}{m} < < < \frac{W}{M}$$
$$\therefore \qquad \frac{p^\circ - p_s}{p^\circ} = \frac{w/m}{\frac{W}{M}} = \frac{w}{m} \times \frac{M}{W}$$
$$0.0125 = \frac{w \times 18}{m \times W} \Rightarrow \frac{w}{mW} = \frac{0.0125}{18}$$

a. English Proficiency

- 81. (c) 'Immutable' means 'unchangeable'.
- 82. (a) 'Ignominious' means 'shameful'.
- 83. (a) 'Conjecture' means 'making a guess'.
- 84. (d) Institutional is the correct word to fill the blank. Institutional is the word which means relating to principles esp of law, so legally also every human has rights of freedom and equality.

 $m = \frac{\text{Weight of solute } (w) \times 1000}{\text{Molar mass of solute } (m) \times \text{Weight of } H_2O(W)}$

Now, molality,
$$m = \frac{0.0125}{18} \times 1000$$

= 0.69 = 0.7

Mole fraction of oxygen = $\frac{\frac{w}{32}}{\frac{w}{32} + \frac{w}{16}} = \frac{\frac{1}{32}}{\frac{3}{32}} = \frac{1}{3}$

Let the total pressure = p Pressure exerted by oxygen (partial pressure)

$$= \chi_{O_2} \times p_{\text{total}} = p \times \frac{1}{3}$$

:. The fraction of total pressure exerted by oxygen is $\frac{1}{3}$.

78. (b) NaCl + KNO₃ → NaNO₃ + KCl Sum of molar conductivity of reactant = Sum of molar conductivity of products

$$\Lambda^{\circ}(\text{NaNO}_{3}) = \Lambda^{\circ}_{\text{m}}(\text{NaCl}) + \Lambda^{\circ}_{\text{m}}(\text{KNO}_{3}) - \Lambda^{\circ}_{\text{m}}(\text{KCl})$$

$$= 128 + 111 - 152$$

= 87 S cm² mol⁻¹

9. (d)
$$Ca^{2+} + 2e^- \longrightarrow Ca$$
 (at cathode)

$$1 \text{ mole CaCl}_2 = 2F$$

7

From $Q = it \Rightarrow n \cdot 2F = it$

$$\Rightarrow t = \frac{n \cdot 2F}{i} = \frac{30}{40} \times \frac{2 \times 96500}{5} \quad \left(\because n = \frac{w}{m} = \frac{30}{40} \right)$$
$$= 28950 \text{ s} = \frac{28950}{60 \times 60}$$

= 8.04 = 8 h

80. (*a*) As the value of reduction potential of metal ion increases, the tendency of metal oxide to get reduce into metal increases.

Since, reduction potential of only Ag is positive among the given, thus Ag₂O readily gets reduced to Ag metal. In other words, it can be said that Ag₂O is the least stable oxide among the given.

- **85.** *(c)* Volumes is the most appropriate option here. Other options do not match here.
- 86. (c) In the context of the sentence, the option 'skirted' is a appropriate word which means to avoid or evade.
- 87. (b) Immortal means living forever; never dying or decaying. So, among the given options, 'perishable' would be its correct opposite meaning word. Perishable means likely to decay easily.

- (c) 'Opposed' is the correct option. Opposite meaning word to the given italicised word is 'patronised'.
 Patronised means provide favour or support.
 Opposed means disagreeing with someone/something.
- 89. (c) Barbarous' means extremely brutal, uncivilised. So, 'civilised' would be its correct opposite meaning word.

b. Logical Reasoning

- **96.** (c) Figure shown in option (c) will make a complete square on joining with the problem figure.
- 97. (c) From figures (A), (C) and (E),



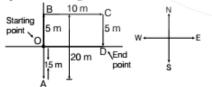
- **98.** (b) The contents of the third figure in each row (and column) are determined by the contents of the first two figures. Lines are carried forward from the first two figures to the third one, except where two lines appear in the same position, in which they are cancelled out.
- 99. (d) From the given four positions of a single block.
 Faces adjacent to face having red colour
 = blue, pink, yellow, green
 Clearly, black is opposite to red.
- 100. (c) In figure (A), the dot is placed in the region which is common to the circle and triangle. Now, we have to search similar common region in the four options. Only in figure (c), we find such a region which is common to the circle and triangle.
- 101. (b) The pattern is as following

$$G \xrightarrow{+3} J \xrightarrow{+3} M \xrightarrow{+3} P \xrightarrow{+3} S \xrightarrow{+3} V$$

$$4 \xrightarrow{\times 2+1} 9 \xrightarrow{\times 2+2} 20 \xrightarrow{\times 2+3} 43 \xrightarrow{\times 2+4} 90 \xrightarrow{\times 2+5} 185$$

 $T \xrightarrow{-2} R \xrightarrow{-2} P \xrightarrow{-2} N \xrightarrow{-2} L \xrightarrow{-2}$ So, V185J will replace the question mark.

102. (a) According to the given information, the direction of Neeraj is as following



- 90. (c) 'Atheist' is the best alternative.
- 91. (c) 'Epicure' is the best alternative.
- **92.** (b) 'Philanthropist' is the correct answer, other alternatives are not relevant.
- 93. (c) CBEDA 94. (d) CDEAB 95. (a) DEBAC

So, it is clearly shown that, Neeraj is 10 m for in East direction from his starting position.

103.*(b)* Let the average age of 8 men = *x* yr

Total age of 8 man = Average × Total man

= 8x yrNow, new average age = x + 2 yrTotal age = 8(x + 2) yr

Difference of ages = 8(x+2) - 8x

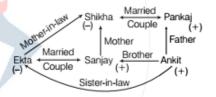
= 8x + 16 - 8x

$$= 16 \text{ vr}$$

Age of new man
$$= 20 + 16 = 36$$
 vr

So, the new man is 36 yr older to the man by whom the new man is replaced.

104.(d) The relation is as following



It is clearly shown that, Shikha is the mother of Ankit.

105. (c) According to the question

From left end, position of *R* = Total children

Position from right end +1

= 40 - 13 + 1 = 28 th

Hence, number of children between P and R = (28 - 13) - 1 = 14

Mathematics

106. (a) Let z = x + iyRe(z + 2) = |z - 2|Re $(x + iy + 2) = |x + iy - 2| \Rightarrow x + 2 = \sqrt{(x - 2)^2 + y^2}$ Squaring on both sides, $(x + 2)^2 = (x - 2)^2 + y^2$

$$(x + 2) = (x - 2) + y$$

 $x^{2} + 4 + 4x = x^{2} + 4 - 4x + y^{2} \Rightarrow y^{2} = 8x$

The locus of z is a parabola.

107. (a) Let α , β be the roots of $x^2 - abx - a^2 = 0$ where, $\alpha + \beta = ab$ and $\alpha\beta = -a^2$, which shows product of roots < 0, i.e. one root must be negative and the other must be positive. Hence, equation has one positive root and one negative root.

108. (c) Given,
$$a + 2b + 3c = 12 \forall a, b, c \in R$$

As, AM \ge GM $\frac{a+b+b+c+c+c}{6} \ge \sqrt[6]{ab^2c^3}$ $\Rightarrow \quad \frac{12}{6} \ge \sqrt[6]{ab^2c^3} \Rightarrow \quad ab^2c^3 \le 2^6$

Hence, the maximum value of ab^2c^3 is 2^6 .

109. (a) a_n of the series $= n(2n+1)^2 \forall n \in N$

$$a_{n} = n[4n^{2} + 4n + 1] \implies a_{n} = 4n^{3} + 4n^{2} + n$$

$$S_{n} = \Sigma a_{n} = 4\Sigma n^{3} + 4\Sigma n^{2} + \Sigma n$$

$$= 4\left(\frac{n(n+1)}{2}\right)^{2} + \frac{4n(n+1)(2n+1)}{6} + \frac{n(n+1)}{2}$$

$$= \frac{n(n+1)}{2}\left[2n^{2} + 2n + \frac{4(2n+1)}{3} + 1\right]$$

$$= \frac{n(n+1)}{2}\left[\frac{6n^{2} + 6n + (8n+4) + 3}{3}\right]$$

$$= \frac{n(n+1)}{2}\left[\frac{6n^{2} + 14n + 7}{3}\right]$$

$$= \frac{n}{6}(n+1)(6n^{2} + 14n + 7)$$
110. (d) $\log_{225} 70 = \frac{\log_{e} 70}{\log_{e} 225} = \frac{\log_{e} 7 + \log_{e} 5 + \log_{e} 2}{\log_{e} 25 + \log_{e} 9}$

$$= \frac{1 + \frac{\log_{e} 5}{\log_{e} 7} + \frac{\log_{e} 2}{\log_{e} 7}}{\log_{e} 7}$$

$$= \frac{1}{2\frac{\log_e 5}{\log_e 7} + 2\frac{\log_e 3}{\log_e 7}}$$
$$= \frac{1 + \log_7 5 + \log_3 2 \times \log_5 3 \times \log_7 5}{2[\log_7 5 + \log_5 3 \times \log_7 5]}$$
$$= \frac{1 + a + abc}{2[a + ab]} = \frac{1 + a + abc}{2a(1 + b)}$$

 (b) Two circles intersect maximum at two distinct points.

Now, two circles can be selected in $^{10}C_{\rm 2}$ ways.

The total number of points of intersection are $^{10}C_2\times 2$

$$= \frac{10 \times 9}{1 \times 2} \times 2 = 90$$
112. (c) $\frac{C_1}{C_0} = n, \frac{C_2}{C_1} = \frac{(n-1)}{2}, \frac{C_3}{C_2} = \frac{n-2}{3}$ and so on.
 $\frac{C_1}{C_0} + 2\frac{C_2}{C_1} + 3\frac{C_3}{C_2} + ..., n\frac{C_n}{C_{n-1}} = \Sigma n = \frac{n(n+1)}{2}$
On putting $n = 20$,
 $\frac{C_1}{C_0} + 2\frac{C_2}{C_1} + 3\frac{C_3}{C_2} + ..., + 20\frac{C_{20}}{C_{19}} = \frac{20 \times 21}{2} = 210$
113. (c) Given, $\begin{vmatrix} 0 & x-p & x-q \\ x+p & 0 & x-r \\ x+q & x-r & 0 \end{vmatrix} = 0$
 $= (x-p)(x+q)(x-r) + (x-q)\begin{vmatrix} x+p & 0 \\ x+q & x-r\end{vmatrix} = 0$
 $\Rightarrow (x-r)[(x-p)(x+q) + (x-q)(x+p)(x-r) = 0$
 $\Rightarrow (x-r)[x^2 - px + qx - pq + x^2 - qx + px - pq] = 0$
 $\Rightarrow (x-r)[2x^2 - 2pq] = 0 \Rightarrow x-r = 0 \text{ or } x^2 - pq = 0$
either $x = r$ or pq
114. (c) $A \cdot adj A = |A|I$
 $|A| = xyz - (8x + 3z + 4y) + 28$
 $\Rightarrow 60 - 20 + 28 = 68$
 $\Rightarrow (adj A)^{-1}$ always exists whenever $(A)^{-1}$ exists.
 $\therefore A \cdot adj A = |A|I$
 $= 68 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 68 & 0 & 0 \\ 0 & 68 & 0 \\ 0 & 0 & 68 \end{bmatrix}$
115. (b) Given, $f(x) = 4x - x^2$
 $f(a+1) - f(a-1)$
 $= [4(a+1) - (a+1)^2] - [4(a-1) - (a-1)^2]$
 $= [4a + 4 - a^2 - 1 - 2a] - [4a - 4 - a^2 - 1 + 2a]$
 $\Rightarrow 8 - 4a = 0$

$$\Rightarrow 3-4a=0$$

 $\therefore a=2$

116. (c) Let $R = \{(a, b) : a + b \text{ is an even integer } a, b \in Z\}$ For $a \in Z$, a + a = 2a is an even integer. $\therefore (a, a) \in R \forall a \in Z$

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.:. R is reflexive. Let $(a, b) \in R \Rightarrow a + b$ is an even integer. \Rightarrow (b + a) is an even integer \Rightarrow (b, a) $\in \mathbb{R}$ $\Rightarrow R$ is symmetric. $Let(a, b), (b, c) \in R$ \Rightarrow (a + b) and (b + c) are even integers. \Rightarrow (a + b) + (b + c) = (a + c + 2b) is an even integer. \Rightarrow (a + c + 2b) - 2b = (a + c) is an even integer. \Rightarrow (a, c) $\in R \Rightarrow R$ is transitive. . R is an equivalence relation. Let $R = \{(a, b) : (a - b) \text{ is an even integer, } a, b \in Z\}.$ For $a \in \mathbb{Z}$, a - a = 0 is an even integer. $(a, a) \in R \forall a \in Z$ ∴ R is reflexive. Let $(a, b) \in R \implies (a - b)$ is an even integer. $\Rightarrow -(a - b)$ is an even integer. \Rightarrow (b - a) is an even integer \Rightarrow $(b, a) \in R$ $\Rightarrow R$ is symmetric. Let $(a, b), (b, c) \in R$ $\Rightarrow (a - b), (b - c)$ are even integers. $\Rightarrow (a - b) + (b - c)$ is an even integer. $\Rightarrow (a - c)$ is an even integer. $\Rightarrow (a, c) \in R$ $\Rightarrow R$ is transitive. . R is an equivalence relation. Let $R = \{(a, b) : a < b, a, b \in Z\}$ Let $a \in \mathbb{Z}$. a < a is false. ∴ R is not reflexive. ∴ R is not an equivalence relation. Let $R = \{(a, b) : a = b, a, b \in Z\}.$ It is quite easy to check that R is an equivalence relation. **117.** (b) Since, $\sim (p \lor q) \equiv (\sim p \land \sim q)$ and $\sim (p \land q) \equiv (\sim p \lor \sim q)$ So, options (a) and (d) are not true. $\sim (p \rightarrow q) \equiv p \land \sim q$, so option (c) is not true. Now, $p \rightarrow q \sim p \lor q$ $\sim q \rightarrow \sim p \equiv [\sim (\sim q) \lor \sim p]$ $\equiv q \lor \sim p \equiv \sim p \lor q \implies p \to q \equiv (\sim q \to \sim p)$ **118.** (a) $4^{-x+0.5} - 7.2^{-x} < 4$ Let $2^{-x} = t$ The equation becomes $2t^2 - 7t - 4 < 0 \implies (t - 4)(2t + 1) < 0$ $\Rightarrow 2(t-4)\left\{t-\left(-\frac{1}{2}\right)\right\} < 0 \Rightarrow -\frac{1}{2} < t < 4$

Here,
$$n = 5$$
, $a_1 = \frac{1}{4}$, $a_2 = 0$, $a_3 = \frac{3}{8}$,
 $a_4 = 0$, $a_5 = 1/8$
120. (b) $|\cot x| = \cot x + \frac{1}{\sin x}|$
Let $\cot x > 0 \Rightarrow \cot x = \cot x + \frac{1}{\sin x} = 0$
 $\Rightarrow \frac{1}{\sin x} = 0$ which is not possible.
Let $\cot x \le 0 \Rightarrow -\cot x = \cot x + \frac{1}{\sin x}$
 $\Rightarrow -2\cot x = \frac{1}{\sin x}$
 $\Rightarrow -2\cot x = \frac{1}{2} \Rightarrow x = \frac{2\pi}{3}, \frac{8\pi}{3}$
 \therefore The number of solutions is 2.
121. (a) Let $I = (\sin^{-1}x)^3 + (\cos^{-1}x)^3$
 $= (\sin^{-1}x + \cos^{-1}x)[(\sin^{-1}x)^2 + (\cos^{-1}x)^2 - ((\sin^{-1}x)(\cos^{-1}x))]$
 $= \frac{\pi}{2} \Big[(\sin^{-1}x + \cos^{-1}x)^2 - 3\sin^{-1}x \Big(\frac{\pi}{2} - \sin^{-1}x \Big) \Big]$
 $= \frac{\pi}{2} \Big[3 \Big[(\sin^{-1}x)^2 - \frac{\pi}{2} (\sin^{1}x) + \frac{\pi^2}{16} - \frac{\pi^2}{16} \Big] + \frac{\pi^2}{4} \Big]$
 $= \frac{\pi}{2} \Big[\frac{\pi^2}{16} + 3 \Big(\sin^{-1}x - \frac{\pi}{4} \Big)^2 \Big]$
(sin $^{-1}x - \frac{\pi}{4} \Big)^2 \ge 0$
For minimum value put $\Big(\sin^{-1}x - \frac{\pi}{4} \Big)^2 = 0$

Minimum values = $\frac{\pi}{2}\left[\frac{\pi^2}{16} + 0\right] = \frac{\pi^3}{32}$

Since, $t = 2^{-x} > 0 \forall x \in R$

Solution is $(-2, \infty)$.

As, 2x is an increasing function,

119. (a) $\cos^3 x \cdot \sin 2x = \frac{\cos 3x + 3\cos x}{4} \times \sin 2x$

 $=\frac{1}{8}(\sin 5x - \sin x) + \frac{3}{8}(\sin 3x + \sin x)$

 $=\frac{1}{4}\sin x + \frac{3}{8}\sin 3x + \frac{1}{8}\sin 5x$

⇒

 $0 < t < 4 \implies 0 < 2^{-x} < 2^2$

-x < 2 or x > -2

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... (i)

122.(b) Let P(x, y) be the original position of the point w.r.t. the original axes. Let us move the origin at new position to (h, k).

Hence, the position of the same point P in the new system is

 $x' = x - h \implies y' = y - k$ Here, (h, k) = (1, 2)

x' = (x - 1), y' = (y - 2).... According to the question,

 $y^{2} - 8x - 4y + 12 = (y - 2)^{2} - 4a(x - 1)$

 $\Rightarrow y^2 - 8x - 4y + 12 = y^2 - 4y + 4 - 4ax + 4a$

On comparing respective coefficients, we get

 $4a = 8 \Rightarrow a = 2$

123. (d) Equations of the bisectors of the angles between the given straight lines are given by

$$\frac{3x+4y+7}{\sqrt{9+16}} = \pm \frac{12x+5y-8}{\sqrt{144+25}}$$

 \Rightarrow 13(3x + 4y + 7) = ± 5(12x + 5y - 8)

 $\Rightarrow 39x + 52y + 91 = \pm (60x + 25y - 40)$

Taking positive signs,

39x + 52y + 91 = 60x + 25y - 40 $\Rightarrow -21x + 27y + 131 = 0 \Rightarrow 21x - 27y - 131 = 0$ Taking negative signs,

$$(39x + 52y + 91) = -(60x + 25y - 40)$$

99x + 77y + 51 = 0⇒

124.(b) Since, the circle touches X-axis,

$$(x-h)^2 + (y-k)^2 = k^2$$

Also, it passes through the points (1, -2) and (3, -4).

 $(1-h)^2 + (-2-k)^2 = k^2$... (ii) ... (iii)

 $(3-h)^2 + (-4-k)^2 = k^2$ and

Subtracting Eq. (iii) from Eq. (ii), we get h = k + 5

On solving these equations, we get

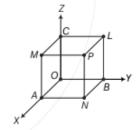
k = -10, -2 and h = -5, 3By putting the values of (h, k) = (-5, -10) or (3, -2)in Eq. (i), we get $x^{2} + y^{2} + 10x + 20y + 25 = 0$

 $x^2 + y^2 - 6x + 4y + 9 = 0$ or

125. (b) x = 9 meets the hyperbola at $(9, 6\sqrt{2})$ and $(9, -6\sqrt{2})$. Then, the equations of tangent at these points are $3x - 2\sqrt{2y} - 3 = 0$ and $3x + 2\sqrt{2y} - 3 = 0$. The combined equation of these two tangent is $9x^2 - 8y^2 - 18x + 9 = 0.$

126. (d) Let the points be A(10i + 3j), $B(12\hat{i} - 15\hat{j})$ and $C(a\hat{i} + 11\hat{j})$.

 $AB = |2\hat{i} - 18\hat{j}|$ and $AC = (a - 10)\hat{i} + 8\hat{j}$ Since, A, B and C are collinear, then $\frac{2}{a-10} = -\frac{18}{8} \Rightarrow a = \frac{82}{9}$ 127. (d) We have, |a| = 3, |b| = 4 and |c| = 5. It is given that $\mathbf{a} \perp (\mathbf{b} + \mathbf{c}), \mathbf{b} \perp (\mathbf{c} + \mathbf{a}) \text{ and } \mathbf{c} \perp (\mathbf{a} + \mathbf{b})$ \Rightarrow a · (b + c) = 0, b.(c + a) = 0 and c · (a + b) = 0 $\Rightarrow \mathbf{a} \cdot \mathbf{b} + \mathbf{a} \cdot \mathbf{c} = \mathbf{b} \cdot \mathbf{c} + \mathbf{b} \cdot \mathbf{a} = \mathbf{c} \cdot \mathbf{a} + \mathbf{c} \cdot \mathbf{b} = 0$ or $\mathbf{a} \cdot \mathbf{b} + \mathbf{b} \cdot \mathbf{c} + \mathbf{c} \cdot \mathbf{a} = 0$ (adding all the above equations) Now, $|\mathbf{a} + \mathbf{b} + \mathbf{c}|^2 = |\mathbf{a}|^2 + |\mathbf{b}|^2 + |\mathbf{c}|^2 + 2$ $(\mathbf{a} \cdot \mathbf{b} + \mathbf{b} \cdot \mathbf{c} + \mathbf{c} \cdot \mathbf{a})$ $= 3^2 + 4^2 + 5^2 = 50$ \therefore |a+b+c|= $5\sqrt{2}$ **128.** (d) We have, $|(a \times b) \cdot c| = |a| |b| |c|$ \Rightarrow ||a|| ||b|| c|sin $\theta \cos \alpha$ | = |a||b||c| $\Rightarrow |\sin \theta| |\cos \alpha| = 1 \Rightarrow \theta = \frac{\pi}{2} \text{ and } \alpha = 0$ \Rightarrow a \perp b and c \parallel $\hat{n} \Rightarrow$ a \perp b and c \perp both a and b. ⇒ a, b, c are mutually perpendicular. $\Rightarrow \mathbf{a} \cdot \mathbf{b} = \mathbf{b} \cdot \mathbf{c} = \mathbf{c} \cdot \mathbf{a} = 0$ **129.**(c) Let each edge of cube be a, then coordinates of the vertices of cube are O(0, 0, 0), A(a, 0, 0), B(0, a, 0), C(0,0, a), N(a, a, 0), P (a, a, a), L(0, a, a), M(a, 0, a)



Direction ratios of the diagonals OP, AL, BM and CN are(a, a, a), (-a, a, a), (a, -a, a) and (a, a, -a).Let θ be the acute angle between diagonals OP and AL.

$$\begin{aligned} \therefore \quad \cos\theta &= \frac{a_1 a_2 + b_1 b_2 + c_1 c_2}{\sqrt{a_1^2 + b_1^2 + c_1^2} \sqrt{a_2^2 + b_2^2 + c_2^2}} \\ &= \frac{a \times (-a) + a \times a + a \times a}{\sqrt{a^2 + a^2 + a^2} \sqrt{(-a)^2 + a^2 + a^2}} \\ &= \frac{-a^2 + a^2 + a^2}{\sqrt{3a^2} \sqrt{3a^2}} = \frac{a^2}{a\sqrt{3} \times a\sqrt{3}} \\ \Rightarrow \quad \cos\theta &= \frac{1}{3} \quad \Rightarrow \quad \theta = \cos^{-1}\left(\frac{1}{3}\right) \end{aligned}$$

130. (b) Given lines are $L_1: \frac{x+1}{3} = \frac{y+2}{1} = \frac{z+1}{2}$ and $L_2: \frac{x-2}{1} = \frac{y+2}{2} = \frac{z-3}{3}$ Now, convert into vector form $L_1:(-\hat{i}-2\hat{j}-\hat{k})+\lambda(3\hat{i}+\hat{j}+2\hat{k})$ $L_2:(2\hat{i} - 2\hat{j} + 3\hat{k}) + \mu(\hat{i} + 2\hat{j} + 3\hat{k})$ Line L_1 comparing with $\mathbf{a}_1 + \lambda \mathbf{b}_1$, and L_2 comparing with $a_2 + \mu b_2$, then we have $\mathbf{b}_1 = 3\hat{\mathbf{i}} + \hat{\mathbf{j}} + 2\hat{\mathbf{k}}$ and $\mathbf{b}_2 = \hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$ Perpendicular to both \mathbf{b}_1 and $\mathbf{b}_2 = \mathbf{b}_1 \times \mathbf{b}_2$ $=\hat{i}(3-4)-\hat{j}(9-2)+\hat{k}(6-1)=-\hat{i}-7\hat{j}+5\hat{k}$ $\therefore \text{ Required unit vector} = \frac{-\hat{i} - 7\hat{j} + 5\hat{k}}{\sqrt{(-1)^2 + (-7)^2 + (5)^2}}$ $=\frac{-\hat{1}-7\hat{j}+5\hat{k}}{\sqrt{75}}=\frac{-\hat{1}-7\hat{j}+5\hat{k}}{5\sqrt{3}}$

131. (b) The given line is $\mathbf{r} = \mathbf{a} + t\mathbf{b}$, where $\mathbf{a} = 2\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$, $\mathbf{b} = \hat{\mathbf{i}} - \hat{\mathbf{j}} + 4\hat{\mathbf{k}}$ and given plane is $\mathbf{r} \cdot \mathbf{n} = \mathbf{d}$, where $\mathbf{n} \neq \hat{\mathbf{i}} + 5\hat{\mathbf{j}} + \hat{\mathbf{k}}$, $\mathbf{d} = 5$.

Since, $b \cdot n = 1 - 5 + 4 = 0$

... Given line is parallel to given plane.

. The distance between the line and the plane is equal to length of the perpendicular from the point $\mathbf{a} = 2\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$ on the line to the given plane.

.: Required distance

$$= \frac{\left| (2\hat{i} - 2\hat{j} + 3\hat{k}) \cdot (\hat{i} + 5\hat{j} + \hat{k}) - 5 \right|}{\sqrt{1 + 25 + 1}}$$
$$= \frac{\left| 2 - 10 + 3 - 5 \right|}{\sqrt{27}} = \frac{10}{3\sqrt{3}}$$

132. (c) Let E_1 = event of getting both red cards

 E_2 = event of getting both kings

and $E_1 \cap E_2$ = event of getting 2 kings of red cards

$$\therefore P(E_1) = \frac{{}^{26}C_2}{{}^{52}C_2} = \frac{325}{1326}, P(E_2) = \frac{{}^{4}C_2}{{}^{52}C_2} = \frac{6}{1326}$$

and $P(E_1 \cap E_2) = \frac{{}^{2}C_2}{{}^{52}C_2} = \frac{1}{1326}$

∴ P(both red or both kings) = P(E₁ ∪ E₂)
= P(E₁) + P(E₂) - P(E₁ ∩ E₂)
=
$$\frac{325}{1326} + \frac{6}{1326} - \frac{1}{1326} = \frac{330}{1326} = \frac{55}{221}$$

133.(d) Since, A and B are independent events.

$$\therefore P(A / B) = P(A) = \frac{1}{2}$$

$$\Rightarrow P\left(\frac{A}{A \cup B}\right) = \frac{P[A \cap (A \cup B)]}{P(A \cup B)}$$

$$= \frac{P(A)}{P(A \cup B)} = \frac{1/2}{\frac{1}{2} + \frac{1}{5} - \frac{1}{10}} = \frac{1/2}{\frac{1}{2} + \frac{1}{5} - \frac{1}{10}} = \frac{1/2}{\frac{6}{10}} = \frac{5}{6}$$
Similarly, $P\left(\frac{A \cap B}{A' \cup B'}\right) = P\left(\frac{A \cap B}{(A \cap B)'}\right) = 0$

134. (b) Let $E_1 = \text{coin shows head}$, $E_2 = \text{coin shows tail}$, A = drawn ball is blue

$$P(E_1) = \frac{1}{2} = P(E_2)$$

 $P(A/E_1)$ = Probability of drawing a blue ball from bag I = 2/7

 $P(A/E_2)$ = Probability of drawing a blue ball from bag II = 6/8

By Baye's theorem, we have

$$P\left(\frac{E_1}{A}\right) = \frac{P(E_1) P\left(\frac{A}{E_1}\right)}{P(E_1) P\left(\frac{A}{E_1}\right) + P(E_2) P\left(\frac{A}{E_2}\right)}$$
$$= \frac{\frac{1}{2} \times \frac{2}{7}}{\frac{1}{2} \times \frac{2}{7} + \frac{1}{2} \times \frac{6}{8}} = \frac{\frac{2}{7}}{\frac{2}{7} + \frac{6}{8}} = \frac{2}{7} \times \frac{56}{58} = \frac{8}{29}$$

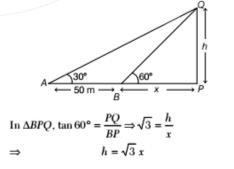
135. (c) Given, E(X) = 3 and $E(X^2) = 11$ Variable of $X = E(X^2) - [E(X)]^2 = 11 - 3^2 = 11 - 9 = 2$

136. (d) Given, $x_1 + x_2 + x_3 + ... + x_{10} = 12$ and $x_1^2 + x_2^2 + \dots + x_{10}^2 = 18$

$$\sigma^{2} = \frac{1}{n} \sum x^{2} - \left(\frac{1}{n} \sum x\right)^{2}$$
$$= \frac{1}{10} \times 18 - \left(\frac{1}{10} \times 12\right)^{2} = \frac{9}{5} - \frac{36}{25} = \frac{9}{25}$$

:. Standard deviation = 3/5

137. (c) Let PQ be the chimney whose height is h metres.

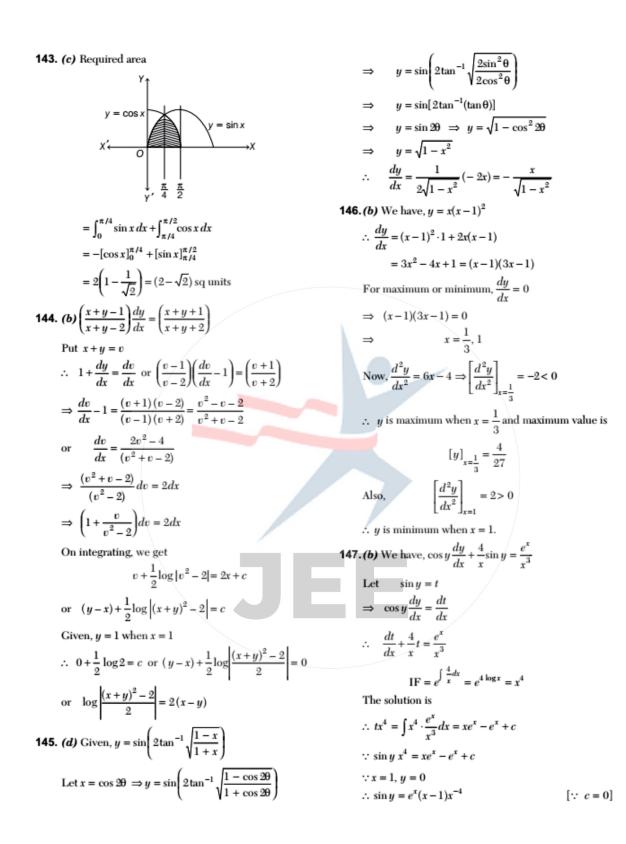


...(i)

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and in
$$\Delta APQ$$
, tan $30^{\circ} = \frac{PQ}{AP}$
 $\Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{50 + x}$
 $\Rightarrow 30^{\circ} + x = h\sqrt{3}$
 $\Rightarrow 0^{\circ} + x = h\sqrt{3}$
 $= 1 + \tan^{2} \frac{x}{2}$
 $= 1 + \tan^{2} \frac{x$



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Player A			Player B			
xi	x _i - 61	$(x_i - 61)^2$	yi	y _i – 61	$(y_i - 61)^2$	
58	- 3	9	94	33	1089	
59	- 2	4	26	- 35	1225	
60	-1	1	92	31	961	
54	- 7	49	65	4	16	
65	4	16	96	35	1225	
66	5	25	78	17	289	
52	-9	81	14	-47	2209	
75	14	196	34	-27	729	
69	8	64	98	37	1369	
52	-9	81	13	-48	2304	
$\sum x_i = 610$		$\sum (x_i - 61)^2 = 526$	$\sum_{yi} = 610$		$\sum (y_i - 61)^2 = 11416$	

For player A, Mean =
$$\frac{\sum x_i}{n} = \frac{610}{10} = 61$$

SD = $\sqrt{\frac{\sum (x_i - 61)^2}{N}}$
= $\sqrt{\frac{526}{10}} = 7.25$
For player B, Mean = $\frac{\sum y_i}{n} = \frac{610}{10} = 61$
SD = $\sqrt{\frac{\sum (y_i - 61)^2}{N}}$
= $\sqrt{\frac{11416}{10}}$
= 33.79

Since, SD for player A is 7.25 < SD for player B is 33.79.

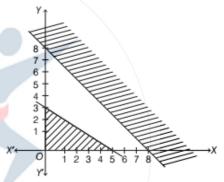
Hence, player A is more consistent player.

149. (b) Table for equation x + y = 8 is

$$\begin{array}{c|ccc} x & 0 & 8 \\ \hline y = 8 - x & 8 & 0 \\ \end{array}$$

Table for equation 3x + 5y = 15 is

x	0	5
$y = \frac{15 - 3x}{5}$	3	0



It can be concluded from the graph, that there is no point which can satisfy all the constraints simultaneously. Therefore, the problem has no feasible solution.

150. (a) Substitute 0 for y in the equation $4y^2 = 4x^2 - x^3$, $0 = x^2(4 - x) \implies x = 0, x = 4$

It means curve makes the loop symmetric about X-axis between 0 and 4.

Area =
$$2\int_0^4 y \, dx = \frac{2}{2} \int_0^4 \sqrt{4x^2 - x^3} \, dx = \int_0^4 x \sqrt{4 - x} \, dx$$

Let $4 - x = t \implies -dx = dt$

Area =
$$-\int_{4}^{6} (4-t)\sqrt{t} dt$$

= $\int_{0}^{4} (4\sqrt{t}-t\sqrt{t})dt = \left[4 \times \frac{2}{3}t^{3/2} - \frac{2}{5}t^{5/2}\right]_{0}^{4}$
= $\frac{8}{3} \times 8 - \frac{2}{5} \times 32 = \frac{64}{3} - \frac{64}{5} = 64 \times \frac{2}{15} = \frac{128}{15}$