

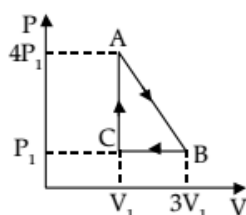
Q. 7. The specific heat of a substance is given by $C = a + bT$, where $a = 1.12 \text{ kJ kg}^{-1}\text{K}^{-1}$ and $b = 0.016 \text{ kJ-kg K}^{-2}$. The amount of heat required to raise the temperature of 1.2 kg of the material from 280 K to 312 K is :

- (1) 205 kJ (2) 215 kJ
(3) 225 kJ (4) 235 kJ

Q. 8. In a cubical box of volume V , there are N molecules of a gas moving randomly. If m is mass of each molecule and v^2 is the mean square of x component of the velocity of molecules, then the pressure of the gas is :

- (1) $P = \frac{1}{3} \frac{mNv^2}{V}$ (2) $P = \frac{mNv^2}{V}$
(3) $P = \frac{1}{3} mNv^2$ (4) $P = mNv^2$

Q. 9. An ideal gas is taken through series of changes ABCA. The amount of work involved in the cycle is :



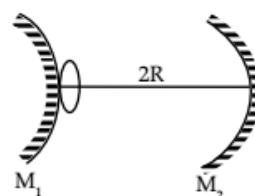
- (1) $12P_1V_1$ (2) $6P_1V_1$
(3) $3P_1V_1$ (4) P_1V_1

Q. 10. A thin square steel plate with each side equal to 10 cm is heated by a blacksmith. The rate of radiated energy by the heated plate is 1134 watts. The temperature of the hot steel plate is :

(Stefan's constant $\sigma = 5.67 \times 10^{-8} \text{ watt m}^{-2}\text{K}^{-4}$
emissivity of the plate = 1)

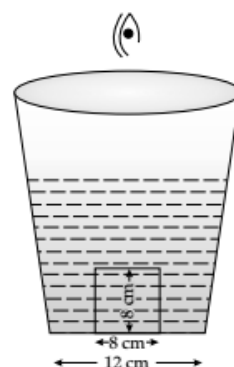
- (1) 570 K (2) 1189 K
(3) 2500 K (4) 750 K

Q. 11. Two spherical mirrors, one convex and the other concave, each of same radius of curvature R are arranged coaxially at a distance of $2R$ from each other. A small circle of radius a is drawn on the convex mirror as shown in figure. What is the radii of first two images of the circle?



- (1) $\frac{a}{3}, \frac{a}{11}$ (2) $\frac{a}{6}, \frac{a}{2}$
(3) $\frac{a}{3}, \frac{a}{4}$ (4) $\frac{a}{12}, \frac{a}{4}$

Q. 12. A cylindrical vessel of diameter 12 cm contains $800\pi \text{ cm}^3$ of water. A cylindrical glass piece of diameter 8.0 cm and height 8.0 cm is placed in the vessel. If the bottom of the vessel under the glass piece is seen by the paraxial rays (see figure), locate its image from bottom. The index of refraction of glass is 1.50 and that of water is 1.33.



- (1) 2.1 cm (2) 7.1 cm
(3) 9.1 cm (4) 11.1 cm

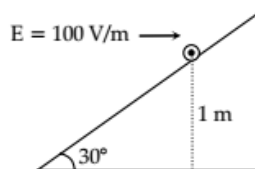
Q. 13. A prism of refractive index $\sqrt{2}$ and refracting angle A produces minimum deviation δ_m of a ray on one face at an angle of incidence 45° . The values of A and δ_m are, respectively,

- (1) $45^\circ, 45^\circ$ (2) $45^\circ, 60^\circ$
(3) $60^\circ, 30^\circ$ (4) $60^\circ, 45^\circ$

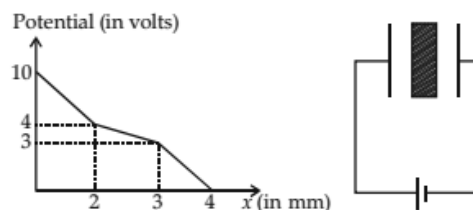
Q. 14. A converging lens of focal length f is placed at a distance 0.3 m from an object to produce an image on a screen 0.9 m from the lens. With the object and the screen in the same positions, an image of the object could also be produced on the screen by placing a converging lens of focal length

- (1) f at a distance 0.1 m from the screen
(2) f at a distance 0.3 m from the screen
(3) $3f$ at a distance 0.3 m from the screen
(4) $3f$ at a distance 0.1 m from the screen

- Q. 15. Monochromatic green light of wavelength 5×10^{-7} m illuminates a pair of slits 1 mm apart. The separation of bright lines in the interference pattern formed on a screen 2 m away is :
- (1) 0.25 mm (2) 0.1 mm
(3) 1.0 mm (4) 0.01 mm
- Q. 16. What is the electric potential needed to excite He^+ to its first excited state?
- (1) 40.8 V (2) 20.4 V
(3) 10.2 V (4) 81.6 V
- Q. 17. The activity of a certain radionuclide decreases to 15 percent of its original value in 10 days. What is its half life?
- [$\ln(0.15) = -1.9$].
- (1) 3.00 days (2) 3.50 days
(3) 3.65 days (4) 3.8 days
- Q. 18. When ultraviolet light of wavelength 100 nm is incident upon a sample of silver metal, a potential difference of 7.7 volt is required to stop the photoelectrons from reaching the collector plate. The potential required to stop photo electrons when light of wavelength 200 nm is incident upon silver is :
- (1) 1.5 V (2) 1.85 V
(3) 1.95 V (4) 2.37 V
- Q. 19. A vernier calliper has 20 divisions on the vernier scale, which coincide with 19 on the main scale. The least count of the instrument is 0.1 mm. The main scale divisions are of :
- (1) 0.5 mm (2) 1 mm
(3) 2 mm (4) 1/4 mm
- Q. 20. A racing car moving towards a cliff sounds its horn. The sound reflected from the cliff has a pitch one octave higher than the actual sound of the horn. If V is the velocity of sound, the velocity of the car is :
- (1) $\frac{V}{\sqrt{2}}$ (2) $\frac{V}{2}$
(3) $\frac{V}{3}$ (4) $\frac{V}{4}$
- Q. 22. The greatest speed of transverse waves through a steel wire of radius 1 mm is $\times 10^2$ m. The breaking stress of steel is $6.0 \times 10^8 \text{ Nm}^{-2}$. Density of steel = 7800 kg m^{-3} .
- Q. 23. Length of steel rod so that it is 5 cm longer than the copper rod at all temperatures should be cm.
- (α for copper = $1.7 \times 10^{-5}/^\circ\text{C}$ and α for steel = $1.1 \times 10^{-5}/^\circ\text{C}$)
- Q. 24. An inclined plane makes an angle of 30° with the horizontal electric field E of 100 V/m. A particle of mass 1 kg and charge 0.01 C slides down from a height of 1 m. If the coefficient of friction is 0.2, the time taken for the particle to reach the bottom is sec.



- Q. 25. A capacitor filled partially with dielectric material of dielectric constant 'k'. Its electric potential versus position graph is as shown. Distance between the two plates is 4 mm. The dielectric constant of medium is



- Q. 26. One solenoid is centered inside another. The outer one has a length of 50.0 cm and contains 6750 coils, while the coaxial inner solenoid is 3.0 cm long and $\pi \text{ cm}^2$ in area and contains 150 coils. The current in the outer solenoid is changing at 3000 A/s. The emf induced in the inner solenoid is V. (Round off to two decimal places.)

Section B

- Q. 21. An engine is approaching a cliff at a constant speed. When it is at a distance of 0.9 km from cliff it sounds a whistle. The echo of the sound is heard by the driver after 5 seconds. Velocity of sound in air is equal to 330 ms^{-1} . The speed of the engine is km/h

- Q. 40. What would be the product when neopentyl chloride reacts with sodium ethoxide :
- (1) 2-Methyl-butan-2-ol
 - (2) Neo pentyl alcohol
 - (3) Both A and B
 - (4) 2-Methyl-but-2-ene
- Q. 41. The missing structures A and B in the reaction sequence:
- $$\text{R-CH}_2\text{-CH}_2\text{OH} \xrightarrow[350^\circ\text{C}]{\text{Al}_2\text{O}_3} \text{R-CH=CH}_2$$
- $$\xrightarrow[\text{(ii) ZnH}_2\text{O}^{\oplus}]{\text{(i) O}_3} \text{RCHO} + \text{A}; \text{RCHO} \xrightarrow{\text{Reduce}} \text{B};$$
- are :
- (1) CH₃OH, RCOOH
 - (2) Methanal, RCH₂OH
 - (3) Ethanal, RCOOH
 - (4) Methanal, RCHOHR
- Q. 42. CH₃-CH₂-CHO $\xrightarrow[\text{alkali}]{\text{Dil}}$ Product. The product in the above reaction is :
- (1) CH₃-CH₂COOH
 - (2) CH₃-CH₂-CH₂OH
 - (3) CH₃-CH₂-CH(OH)-CH₂-CHO
 - (4) CH₃-CH₂-CH(OH)-CH(CH₃)-CHO
- Q. 43. Identify the product A in the following reaction
- $$\text{CH}_2 \begin{cases} \text{COOH} \\ \text{COOH} \end{cases} \xrightarrow{\text{A}} \text{CH}_3\text{COOH} + \text{A}$$
- (1) CO₂
 - (2) CH₃CHO
 - (3) CH₃OH
 - (4) None of these
- Q. 44. When propionamide reacts with Br₂ in the presence of alkali the product is :
- (1) CH₃CH₂CH₂NH₂
 - (2) CH₃CH₂NH₂
 - (3) C₃H₇CN
 - (4) C₂H₅CN
- Q. 45. A pyranose ring consists of a skeleton of :
- (A) 5 carbon atoms and one oxygen atom
 - (2) 6 carbon atoms
 - (3) 6 carbon atoms and one oxygen atom
 - (4) 4 carbon atoms and one oxygen atom
- Q. 46. A mixture of benzene and chloroform is separated by :
- (1) Sublimation
 - (2) Separating funnel
 - (3) Crystallization
 - (4) Distillation
- Q. 47. Which of the following is a double salt :
- (1) Carnallite
 - (2) Mohr's salt
 - (3) Alum
 - (4) All are correct
- Q. 48. Heating of MgCl₂ 6H₂O in absence of HCl gives :
- (1) MgCl₂
 - (2) MgO
 - (3) Mg₃N₂
 - (4) Mg(OH)₂
- Q. 49. A reddish-pink substance on heating gives off a vapour which condenses on the sides of the test tube and the substance turns blue. If on cooling water is added to the residue it turns to original colour. The substance is :
- (1) Iodine crystals
 - (2) Copper sulphate crystals
 - (3) Cobalt chloride crystals
 - (4) ZnO
- Q. 50. Ozone on reacting with KI in neutral medium produces :
- (1) KIO₃
 - (2) KOH
 - (3) KCl
 - (4) KO₂

Section B

- Q. 51. The decomposition of N₂O into N₂ and O₂ in presence of gaseous argon follows second order kinetics, with
- $$k = (5.0 \times 10^{11} \text{ L mol}^{-1} \text{ s}^{-1}) e^{-\frac{29000 \text{ K}}{T}}$$
- Arrhenius parameters are kJ mol⁻¹.
- Q. 52. The total number of α and β particles emitted in the nuclear reaction ${}_{92}^{238}\text{U} \rightarrow {}_{82}^{214}\text{Pb}$ is.....
- Q. 53. The solubility of Co₂[Fe(CN)₆] in water at 25°C from the following data : Conductivity of saturated solution of Co₂[Fe(CN)₆] = 2.06 × 10⁻⁶ ohm⁻¹ cm⁻¹ and that of water = 4.1 × 10⁻⁷ ohm⁻¹ cm⁻¹. The ionic molar conductivities of Co²⁺ and [Fe(CN)₆]⁴⁻ are 86 and 444 ohm⁻¹ cm² mol⁻¹ respectively, is × 10⁻⁶ mol/L.
- Q. 54. In an ionic solid r₍₊₎ = 1.6 Å and r₍₋₎ = 1.864 Å. Use the radius ratio rule to the edge length of the cubic unit cell is Å.
- Q. 55. A storage battery contains a solution of H₂SO₄ 38% by weight. At this concentration, vant Hoff factor is 2.50. At the battery content freeze temperature will be K. K_f = 1.86 K Kg mol⁻¹.
- Q. 56. The density of gold is 19 g/cm³. If 1.9 × 10⁻⁴ g of gold is dispersed in one litre of water to

give a sol having spherical gold particles of radius 10 nm, the number of gold particles per mm^3 of the sol will be $\times 10^6$.

- Q. 57. A given mixture consists only of pure substance X and pure substance Y. The total weight of the mixture is 3.72 gm. The total number of moles is 0.06. If the weight of one mole Y is 48 g and if there is 0.02 mole X in the mixture, the weight of one mole of X is g.
- Q. 58. The number of times larger the spacing between the energy levels with $n = 3$ and $n = 8$ spacing between the energy level with

$n = 8$ and $n = 9$ for the hydrogen atom is

- Q. 59. Dipole moment of HX is 2.59×10^{-30} coulomb-metre. Bond length of HX is 1.39 Å. The ionic character of molecule is %.
- Q. 60. For the gaseous reaction,
 $\text{K}_{(g)} + \text{F}_{(g)} \rightarrow \text{K}^+_{(g)} + \text{F}^-_{(g)}$, ΔH was calculated to be 19 kcal/mol under conditions where the cations and anions were prevented by electrostatic separation from combining with each other. The ionisation energy of K is 4.3 eV. The electron affinity of F is (in eV)

Mathematics

Section A

Q. 61. $\int \frac{3x+1}{2x^2-2x+3} dx$ equals :

- (1) $\frac{1}{4} \log(2x^2 - 2x + 3) - \frac{\sqrt{5}}{2} \tan^{-1} \left(\frac{2x-1}{\sqrt{5}} \right) + C$
 (2) $\frac{3}{4} \log(2x^2 - 2x + 3) + \frac{\sqrt{5}}{2} \tan^{-1} \left(\frac{2x-1}{\sqrt{5}} \right) + C$
 (3) $\frac{3}{4} \log(2x^2 - 2x + 3) + \frac{\sqrt{5}}{2} \tan^{-1} \left(\frac{4x-2}{\sqrt{5}} \right) + C$
 (4) $\frac{1}{4} \log(2x^2 - 2x + 3) - \frac{\sqrt{5}}{2} \tan^{-1} \left(\frac{4x-2}{\sqrt{5}} \right) + C$

Q. 62. $\int_0^{\frac{\pi}{2}} \frac{x \sin x}{1 + \cos^2 x} dx$ equals :

- (1) 0
 (2) $\frac{\pi}{4}$
 (3) $\frac{\pi^2}{4}$
 (4) $\frac{\pi^2}{2}$

Q. 63. Area in first quadrant bounded by $y = 4x^2$, $x = 0$, $y = 1$ and $y = 4$ is :

- (1) $\frac{3}{7}$
 (2) $\frac{5}{7}$
 (3) $\frac{7}{3}$
 (4) $\frac{7}{5}$

Q. 64. If the curves $y^2 = 6x$, $9x^2 + by^2 = 16$, cut each other at right angles then the value of b is :

- (1) 2
 (2) 4
 (3) $\frac{9}{2}$
 (4) 3

Q. 65. Let $f(x) = \tan^{-1} \phi(x)$, where $\phi(x)$ is monotonically increasing for $0 < x < \frac{\pi}{2}$. Then $f(x)$ is :

- (1) increasing in $\left(0, \frac{\pi}{2}\right)$
 (2) decreasing in $\left(0, \frac{\pi}{2}\right)$
 (3) increasing in $\left(0, \frac{\pi}{4}\right)$ and decreasing in $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$
 (4) decreasing in $\left(0, \frac{\pi}{4}\right)$ and increasing in $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$

Q. 66. The function $g(x) = \frac{f(x)}{x}$, $x \neq 0$ has an extreme value when :

- (1) $g'(x) = f(x)$
 (2) $f(x) = 0$
 (3) $x g'(x) = f(x)$
 (4) $g(x) = f'(x)$

Q. 67. The ratio $\frac{2^{\log_2 a^a} - 3^{\log_2 (a^2+1)^2} - 2a}{7^{4 \log_{49} a} - a - 1}$ simplifies to

- (1) $a^2 - a - 1$
 (2) $a^2 + a - 1$
 (3) $a^2 - a + 1$
 (4) $a^2 + a + 1$

Q. 68. The number of real solutions of

$$x - \frac{1}{x^2 - 4} = 2 - \frac{1}{x^2 - 4} \text{ is :}$$

- (1) 0
 (2) 1
 (3) 2
 (4) infinite

Q. 69. A GP consists of an even number of terms. If the sum of all the terms is 5 times the

sum of the terms occupying odd places, the common ratio will be equal to :

- (1) 2 (2) 3
(3) 4 (4) 5

Q. 70. If sum of the coefficient of second and fourth terms in the expansion of $\left(2x - \frac{1}{3x^2}\right)^5$, in descending powers of x , is S , Then The value $\left|\frac{81}{40}S\right|$ of is :

- (1) 27 (2) 57
(3) 72 (4) 75

Q. 71. If the vertices of a triangle be $(0, 0)$, $(6, 0)$ and $(6, 8)$, then its incentre will be :

- (1) $(2, 1)$ (2) $(1, 2)$
(3) $(4, 2)$ (4) $(2, 4)$

Q. 72. If the line $3x + 4y = m$ touches the circle $x^2 + y^2 = 10x$, then m is equal to :

- (1) $-40, 10$ (2) $40, -10$
(3) $40, 10$ (4) $-40, -10$

Q. 73. Which of the following are not parametric coordinates of any point on the parabola $y^2 = 4ax$:

- (1) $(at^2, 2at)$ (2) $\left(am^2, \frac{2a}{m}\right)$
(3) $(a/m^2, 2a/m)$ (4) $(am^2, -2am)$

Q. 74. Tangents are drawn from a point on the circle $x^2 + y^2 = 25$ to the ellipse $9x^2 + 16y^2 - 144 = 0$ then find the angle between the tangents.

- (1) $\frac{\pi}{4}$ (2) $\frac{3\pi}{4}$
(3) $\frac{\pi}{2}$ (4) $\frac{2\pi}{3}$

Q. 75. Parametric form of the hyperbola $\frac{x^2}{4} - \frac{y^2}{9} = -1$ is :

- (1) $(2 \tan \theta, 3 \sec \theta)$ (2) $(3 \sec \theta, 2 \tan \theta)$
(3) $(9 \sec \theta, 4 \tan \theta)$ (4) $(3 \tan \theta, 2 \sec \theta)$

Q. 76. Consider

Statement 1 : $(p \wedge \sim q) \wedge (\sim p \wedge q)$ is a fallacy.

Statement 2 : $(p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$ is a tautology.

- (1) Statement- 1 is true; Statement- 2 is true; Statement- 2 is a correct explanation for Statement- 1
(2) Statement- 1 is true; Statement- 2 is true; Statement- 2 is not a correct explanation for Statement- 1
(3) Statement- 1 is true; Statement- 2 is false.
(4) Statement- 1 is false; Statement- 2 is true

Q. 77. If $1, \alpha_1, \alpha_2, \dots, \alpha_{n-1}$ are the roots of unity, then $(1 + \alpha_1)(1 + \alpha_2) \dots (1 + \alpha_{n-1})$ is equal to (when n is even) :

- (1) $n - 1$ (2) n
(3) 0 (4) 2

Q. 78. The d.c's of a line whose direction ratios are $2, 3, -6$, are :

- (1) $\frac{2}{7}, \frac{3}{7}, \frac{-6}{7}$ (2) $\frac{-2}{7}, \frac{3}{7}, \frac{-6}{7}$
(3) $\frac{2}{7}, \frac{-3}{7}, \frac{-6}{7}$ (4) $\frac{-2}{7}, \frac{-3}{7}, \frac{-6}{7}$

Q. 79. Unit vector perpendicular to the plane of the triangle ABC with position vectors $\vec{a}, \vec{b}, \vec{c}$ of the vertices A, B, C is :

- (1) $\frac{(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{\Delta}$
(2) $\frac{(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{2\Delta}$
(3) $\frac{(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{4\Delta}$
(4) $\frac{2(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{\Delta}$

Q. 80. The minimum number of zeros in an upper triangular matrix will be :

- (1) $\frac{n(n-1)}{2}$ (2) $\frac{n(n+1)}{2}$
(3) $\frac{2n(n-1)}{2}$ (4) None of these

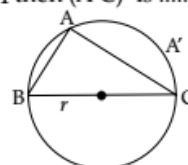
Section B

Q. 81. The Probability that A speaks truth is $\frac{3}{4}$ and that of B is $\frac{4}{5}$. The probability that

they contradict each other in stating the same fact is p , then the value of $40p$ is :

Q. 82. Let right angled isosceles triangle ABC be inscribed in a circle according to adjacent diagram vertex A is moved along the circle

to reach at A' such that $\widehat{AA'} = \frac{\pi r}{3}$, if $r = \sqrt{3} + 1$ then $(A'C)^2$ is



Q. 83. Let $\lambda_1, \lambda_2 \in [0, \pi]$ are the solutions of the equation $\operatorname{cosec}\left(\frac{\pi}{4} + x\right) + \operatorname{cosec}\left(\frac{\pi}{4} - x\right) = 2\sqrt{2}$, then $8(\sin^2 \lambda_1 + \sin^2 \lambda_2)$ is equal to

- Q. 84 Let $x = \sin^{-1}(\sin 8) + \cos^{-1}(\cos 11) + \tan^{-1}(\tan 7)$, and $x = k(\pi - 2.4)$ for an integer k , then the value of k is.....
- Q. 85. If in a frequency distribution, the mean and median are 21 and 22 respectively, then its mode is approximately
- Q. 86. Number of selections of at least one letter from the letters of MATHEMATICS, is
- Q. 87. Let (p_1, q_1, r_1) & (p_2, q_2, r_2) are satisfying
- $$\begin{vmatrix} 1 & p & p^2 \\ 1 & q & q^2 \\ 1 & r & r^2 \end{vmatrix} = 6 \text{ (where } p_i, q_i, r_i \in \mathbb{N} \text{ and } p_i < q_i < r_i \text{ and } i = 1, 2) \text{ and point } (p_1, q_1, r_1) \text{ lies on the plane } 2x + 3y + 6z = k_1 \text{ and point } (p_2, q_2, r_2) \text{ lies on the plane } 2x + 3y + 6z = k_2 \text{ (where } p_1 = p_2 = 1) \text{ If distance between these planes is 'd', then value of } (210d) \text{ is}$$
- Q. 88. Let $f: R - \left\{\frac{1}{2}\right\} \rightarrow R - \left\{\frac{1}{2}\right\}$, $f(x) = \frac{x-2}{2x-1}$ be a function such that $x = m$ is the solution of $f(x) + 2f^{-1}(x) + 2 = f(f(x))$, then m is equal to
- Q. 89. The value of $\lim_{x \rightarrow 0} \frac{(\sin(\ell n e^x))^2}{(e^{\tan^2 x} - 1)}$ is
- Q. 90. If functions g & h are defined as
- $$g(x) = \begin{cases} x^2 + 1 & x \in Q \\ px^2 & x \notin Q \end{cases}$$
- and $h(x) = \begin{cases} px & x \in Q \\ 2x + q & x \notin Q \end{cases}$
- If $(g + h)(x)$ is continuous at $x = 1$ and $x = 3$, then $3p + q$ is

ANSWER-KEY

Physics

Q. No.	Answer	Q. No.	Answer
1	(4)	16	(1)
2	(1)	17	(3)
3	(1)	18	(1)
4	(4)	19	(3)
5	(2)	20	(2)
6	(4)	21	108
7	(3)	22	[2.77 or 2.78 or 2.76]
8	(2)	23	14.17
9	(3)	24	2.00
10	(2)	25	3.00
11	(1)	26	2.43
12	(2)	27	4.00
13	(3)	28	20.00
14	(2)	29	3.00
15	(3)	30	0.05

Chemistry

Q. No.	Answer	Q. No.	Answer
31	(2)	46	(4)
32	(4)	47	(4)
33	(3)	48	(2)
34	(1)	49	(3)
35	(2)	50	(2)
36	(2)	51	241.10
37	(3)	52	8.00
38	(1)	53	2.67
39	(3)	54	4.00
40	(4)	55	243.92
41	(2)	56	2.40
42	(4)	57	90.00
43	(1)	58	3.23
44	(2)	59	11.65
45	(1)	60	3.48

Mathematics

Q. No.	Answer	Q. No.	Answer
61	(2)	76	(2)
62	(3)	77	(3)
63	(3)	78	(1)
64	(3)	79	(2)
65	(1)	80	(1)
66	(4)	81	14.00
67	(4)	82	2.00
68	(1)	83	6.00
69	(3)	84	5.00
70	(2)	85	24
71	(3)	86	863.00
72	(2)	87	90.00
73	(2)	88	2.00
74	(3)	89	1.00
75	(1)	90	2.00