

## JEE FORMULA NOTES

### **DEPTH Notes with Revision**

# PHYSICS

#### **KINEMATICS**

 $|Distance| \geq |Displacement|$ 

Displacement (+ve), (-ve), 0

Distance 0, +ve

 $e \approx 2.7183$ 

1. Average speed and average velocity :

Average speed (v<sub>av</sub>) =  $\frac{\text{Total distance travelled}}{\text{Time inerval}} = \frac{\Delta s}{\Delta t}$ Average velocity ( $\vec{v}_{av}$ ) =  $\frac{\text{Displacement}}{\text{Time interval}} = \frac{\Delta \vec{r}}{\Delta t} = \frac{\vec{r_2} - \vec{r_1}}{t_2 - t_1}$ 

2. Instantaneous speed and instantaneous velocity

$$v = \lim_{\Delta s \to 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt}$$
  $v = \lim_{\Delta s \to 0} \frac{\Delta r}{\Delta t} = \frac{dr}{dt}$ 

#### 3. Average and instantaneous acceleration.

Average acceleration,

 $(\vec{a}_{av}) = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1} = \frac{\Delta \vec{v}}{\Delta t} \frac{\text{Change in velocity}}{\text{Time interval}}$ 

$$(\vec{a})_{inst} = \lim_{\Delta t \to 0} \vec{a}_{av} = \frac{d\vec{v}}{dt}$$
 = Rate of change of velocity.

When direction of acceleration and velocity are opposite to each other, then acceleration is termed as retardation.

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{r}}{dt^2} = \vec{v}\frac{d\vec{v}}{d\vec{r}}$$

#### 4. CONSTANT ACCELERATION FORMAT

(i) v = u + at(ii)  $s = ut + \frac{1}{2} at^2$ (iii)  $s = s_0 + ut + \frac{1}{2} at^2$ (iv)  $v^2 = u^2 + 2as$ (v)  $s_m$  = displacement (not distance) in n<sup>th</sup> second =  $u + \frac{a}{2}(2n - 1)$ 

#### 5. ONE DIMENSIONAL MOTION WITH NON-UNIFORM ACCELERATION

(i)  $s - t \rightarrow v - t \rightarrow a - t \rightarrow Differentiation$ 

(ii)  $a - t \rightarrow v - t \rightarrow s - t \rightarrow$  Integration

- (iii) Equations of differentiation
- (iv) Equation of integration

$$V = \frac{ds}{dt} \text{ and } a = \frac{dv}{dt} = v \cdot \frac{dv}{ds}$$
$$\int ds = \int v \, dt, \int dv = \int a \, dt, \int v \, dv = \int a \, ds$$

#### 6. REACTION TIME

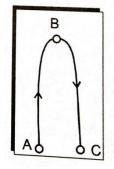
When a particular situation demands our immediate action, it takes some time before we really respond. Reaction time is the time a person takes to observe, think and act. For example, if a person is driving and suddenly a boy appears on the road, then the time elapse before e applies the breaks of the car is the reaction time. Reaction time depends on complexity of the situation and on an individual.

7. I FORMAT : (When a body is thrown vertically upward)

It includes two types of motion

(i) Deaccelerated motion from A to B because the direction of velocity and acceleration is opposite. So speed decreases

(ii) Accelerated motion from B to C because the direction of velocity an acceleration is same (downward). So speed Increases



(a) Time of flight :

$$\mathsf{T} = \frac{2u}{g}$$

#### (b) Maximum Height :

at maximum height v = 0, s =  $H_{max} = \frac{u^2}{2g}$ 

#### (c) Final velocity

 $V_f = -u$ 

i.e. the body reaches the ground with the same speed with which it was thrown vertically upwards as it thrown vertically upward.

(d) Time to reach any general height h

So, 
$$t_1 = \frac{u - \sqrt{u^2 - 2gh}}{g}$$
,  $t_2 = \frac{u - \sqrt{u^2 - 2gh}}{g} \Rightarrow t_1 + t_2 = T$  (Time of light)

II Format (Free fall) :

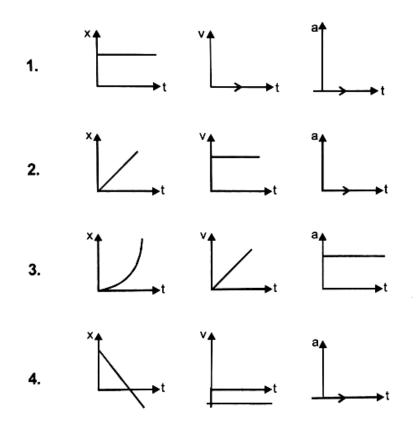
A body released near the surface of the earth is accelerated downward under the influence of force of gravity.

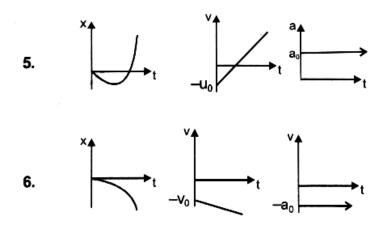
(a) Time of Flight : 
$$T = \sqrt{\frac{2H}{g}}$$

(b) Final Velocity when body reaches the ground :

$$V_{\rm f} = \sqrt{2gH}$$

8. Conversion of Graphs from x-to v-t and v-t to a-t



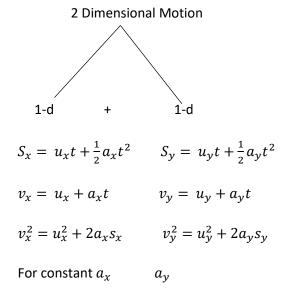


(iii) Slope of s-t graph = velocity, Slope of v-t graph = acceleration Area under v-t graph = displacement and , Area under a-t Graph – change in velocity

#### 9. RELATIVE MOTION IN 1 - D

(i)  $\vec{v}_{AB}$  = velocity of A with respect to B =  $\vec{v}_A - \vec{v}_B$ (ii)  $\vec{a}_{AB}$  = acceleration of A with respect to B =  $\vec{a}_A - \vec{a}_B$  In one dimensional motion Take a sign convention (iii)  $v_{AB} = v_A - v_B$ (iv)  $a_{AB} = a_A - a_B$ 

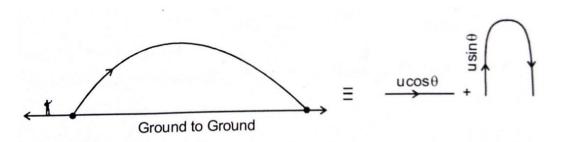
#### **10. MOTION IN TWO DIMENSION**

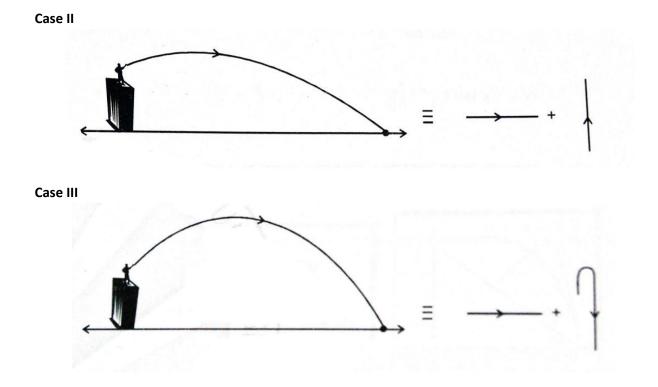


#### **11. PROJECTIL MOTION**

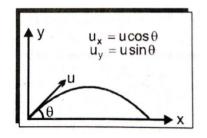
There are following cases which shows the projection of balls form three different situation

Case I





There are following parameters related to projectile motion:

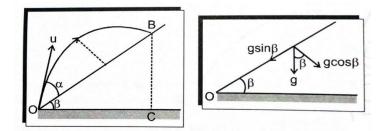


(i) 
$$T = \frac{2usin\theta}{g} = \frac{2u_y}{g}$$
  
(ii)  $H = \frac{u^2sin^2\theta}{2g} = \frac{u_y^2}{2g}$   
(iii)  $R = \frac{u^2sin\theta}{g} = u_x T = \frac{2U_X u_y}{g}$   
(iv)  $R_{max} = \frac{u^2}{g}$  at  $\theta = 45^\circ$ 

(v)  $R_{\theta} = R_{90^{\circ}-\theta}$  for same value of u. (vi) Equation of trajectory

$$Y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$
  
or y = x \tan \theta \left[ 1 - \frac{x}{R} \right]

#### **12. PROJECTILE MOTION IN INCLINED PLANE**



(i) Up the Plane:

Time of flight T =  $\frac{2usin\alpha}{gcos\beta}$ 

**Range** R = u cos 
$$\alpha$$
 T -  $\frac{1}{2}$  g sin  $\beta$ .  $T^2$ 

(ii) Down the inclined plane:

$$T = \frac{2u_y}{a_y} = \frac{2usin\alpha}{gcos\beta}$$

Range = u cos  $\alpha$  T +  $\frac{1}{2}$  gsin $\beta$ . $T^2$ 

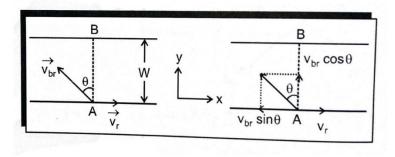
#### **13. PROBLEM RELEATED TO 2-D RELATIVE MOTION**

#### (a) Minimum distance between two bodies in motion

When two bodies are in motion, the questions like, the minimum distance between them or the time when on body overtakes the other can be solved easily by the principle of relative motion. In these type of problems one body is assumed to be at rest and the relative motion of the other body is considered

#### (b) River – Boat Problems

In river-boat problems we come across the following three terms:



 $ec{v}_r$  = absolute velocity of river

 $\vec{v}_{br}$  = velocity of boatman with respect to river or velocity of boatman in still water and  $\vec{v}_b$  = absolute velocity of boatman.

$$t = \frac{W}{V_{br} cos\theta} \qquad \dots \dots (1)$$

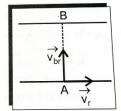
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$$x = (v_r - v_{br} \sin\theta) \frac{W}{v_{br} \cos\theta} \qquad \dots \dots (2)$$

#### (i) Condition when the boatman crosses the river in shortest interval of time

From equation (1) we can see that time (t) will be minimum when  $\theta = 0^{\circ}$ , i.e., the boatman should steer his boat perpendicular to the river current.

Also, 
$$t_{min} = \frac{W}{V_{br}}$$
 as  $\cos \theta = 1$ 



#### (ii) Condition when the boatman want to reach point B, i.e., at a point just opposite from where he started

Hence, to reach point B the boatman should row at an angle  $\theta = sin^{-1} \left(\frac{v_r}{v_{br}}\right)$ Upstream from AB.

#### (iii) Shortest path

When  $v_r > v_{br}$ : In this case x = 0,

When 
$$\theta = sin^{-1} \left( \frac{v_r}{v_{br}} \right)$$
  
Or  $s_{min} = w$  at  $\theta = sin^{-1} \left( \frac{v_r}{v_{br}} \right)$ 

When  $v_r > v_{br}$  :

$$s_{min} = w\left(\frac{v_r}{v_{br}}\right)$$
 at  $\theta = sin^{-1}\left(\frac{v_{br}}{v_r}\right)$ 

#### (c) Flag Problems:

If flag will flutter in direction of  $v_{wc}$ 

Then  $v_{wc} = v_{wc} - v_c$ 

#### (d) Aircraft Wind Problem

 $\vec{v}_a = \vec{v}_{aw} + \vec{v}_w$  $\vec{v}_{aw} =$  velocity of aircraft with respect to wind or velocity of aircraft in still air  $\vec{v}_w =$  velocity of wind  $\vec{v}_a =$  absolute velocity of aircraft

#### (e) Rain Problems

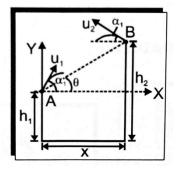
In these type of problems we again come across three terms  $\vec{v}_r$  ,  $\vec{v}_m$  ,  $\vec{v}_{rm}$  , Here ,

 $\vec{v}_r =$  velocity of rain

 $ec{v}_m =$  velocity of man (it may be velocity of cyclist or velocity of motorist also)

and  $\vec{v}_m$  = velocity of rain with respect to man.

#### 14. CONDITION FOR COLLISION OF TWO PROJECTILES:



For collision to take place, in following figure

$$an lpha = tan heta = rac{h_2 - h_1}{x}$$

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# PHYSICS

#### NLM

#### 1. FORCE

A pull or push which change or tends to change the state of rest or of uniform motion or direction of motion of any object is called force.

Force is the interaction between the object and the source (providing the pull or push). It is a vector quantity.

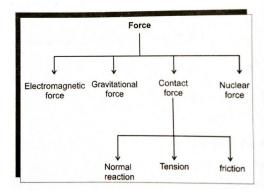
#### Effect of resultant force:

- may change only speed
- may change only direction of motion.
- may change both the speed and direction of motion.
- may change size and shape of a body

unit of force: newton and  $\frac{kg.m}{s^2}$  (MKS System)

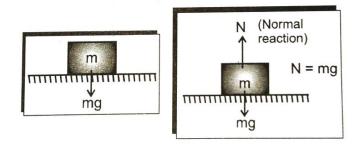
dyne and  $\frac{g.cm}{s^2}$  (CGS System)

1 newton = 10<sup>5</sup> dyne



#### **2. NORMAL REACTION**

Normal reaction always act perpendicular to contact surface in such a direction that it always tires to compress the body.



#### **3. TENSILE FORCE**

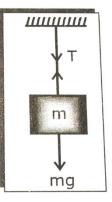
In following figure T = mg

(i) Tension always acts along the string and in such

a direction that it tries to reduce the length of string

(ii) If the sting is massless then the tension will be same along the string but if the

String have some mass then the tension will continuously change along the string.



#### 4. NEWTON'S FIRT LAW OF MOTION :

According to this law "A system will remain in its state of ret or of uniform motion unless a net external force act on it.

1<sup>st</sup> law can also be stated as " If the net external force acting on a body is zero, only then the body remains at rest.

#### 5. NEWTON'S SECOND LAW OF MOTION :

Newton's second law states, "The rate of change of momentum of a body is directly proportional to the applied force an takes place in the direction in which the force acts"

i.e., 
$$\vec{F} \propto \frac{d\vec{p}}{dt}$$
 or  $\vec{F} = k \frac{d\vec{p}}{dt}$ 

where k is a constant of proportionality.

 $\vec{p}=m\vec{v}$ , So  $\vec{F}$ = k $rac{(dm\vec{v})}{dt}$ 

For a body having constant mass,  $\Rightarrow \vec{F} = \text{km} \frac{d\vec{v}}{dt} = km\vec{a}$ 

From experiments, the value of k is found to be 1.

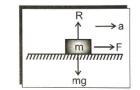
So,  $\vec{F}_{net} = m\vec{a}$ 

#### 6. APPLICATIONS OF NEWTON'S LAW:

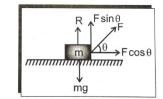
6.1 Motion of a Block on a Horizontal Smooth Surface.

Case (i) : When subjected to a horizontal pull:

F = ma or a = F/m



Case (i) : When subjected to a pull acting at an angle  $(\theta)$  to the horizontal:



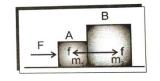
6.2 Motion of bodies in contact.

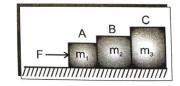
Case (i) : Two body system:

 $\Rightarrow$  a =  $\frac{F}{m_1 + m_2}$  and f =  $\frac{m_2 F}{m_1 + m_2}$ 



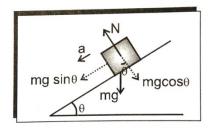
 $\Rightarrow$  a =  $\frac{F}{m_1 + m_2 + m_3}$ 



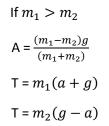


#### 6.3 Motion of a body on a smooth inclined plane:

a = g sin  $\theta$ , N = mg con $\theta$ 



#### 6.4 Pulley Block System



## 

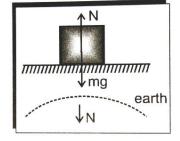
#### 7. NEWTONS' 3<sup>RD</sup> LAW OF MOTION:

Statement : "To every action there is equal and opposite reaction".

According to Newton third law two forces equal in

magnitude and opposite in direction

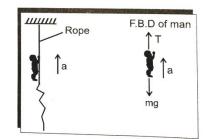
$$\vec{F}_{AB} = \overrightarrow{-F}_{BA}$$



#### 7.1 Climbing in the Rope:

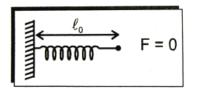
T > mg man accelerates in upward direction,

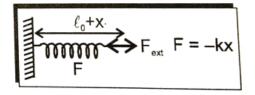
T < mg man accelerates in downward direction

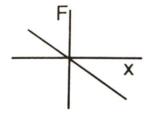


#### 7.2 Spring Force:

**1.** When spring is in its natural length, spring force is zero.



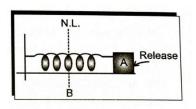


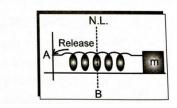


Graph between spring force v/s x

#### 2. Cutting of the spring

- (i) when the block A is released then it take some finite time to reach
  - at B. i.e., spring force doesn't change instantaneously.
- (ii) When point A of the spring is released in the above situation then the spring forces.
  - Changes instantaneously become zero because one end of the spring is free.

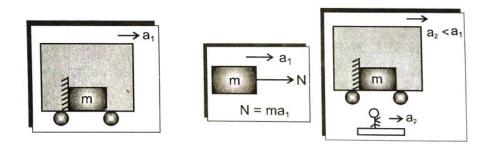


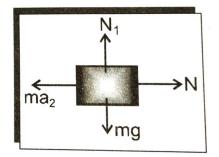


(iii) In string tension may change instantaneously.

#### 8. PSEUDO FORCE:

To apply newton's first law and second law in non inertial frame we introduce a new type of force that is pseudo force.





Pseudo force =  $ma_2$ 

$$N - ma_2 = m(a_1 - a_2)$$

 $N = ma_1$ 



## JEE FORMULA NOTES

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# PHYSICS

#### WORK POWER ENERGY

#### 1. Work Done By a constant force

$$\begin{split} \mathbf{W} &= \vec{F} \cdot \vec{s} = \vec{F} \cdot \left( \vec{r}_f - \vec{r}_i \right) = Fscos\theta \\ &= \text{Force} \times \text{displacement in the direction of force.} \\ &\text{In cgs system, the unit of work is erg.} \\ &\text{In mks system, the unit of work is Joule.} \end{split}$$

1 erg = 10<sup>-7</sup> joule

2. Work Done By a Variable Force:

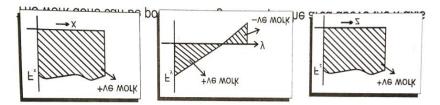
$$\vec{F} = F_x \hat{\iota} + F_y \hat{\jmath} + F_z \hat{k}$$

$$\mathrm{d}\vec{s} = dx\hat{\imath} + dy\hat{\jmath} + dz\hat{k}$$

$$W = \int_{X_A}^{X_B} F_X dx + \int_{Y_A}^{Y_B} F_Y dy + \int_{z_A}^{z_B} F_z dz$$

#### 3. Area Under Force Displacement Curve:

Graphically area under the force – displacement is the work done



below the x – axis respectively.

#### 4. Difference Between Conservative and Non Conservative Forces

S. No.	Conservative forces	Non-Conservative forces	
1	Work done does not depend upon path	Work done depends on path.	
2	Work done in a round trip is zero.	Work done in a round trip is not zero.	
3	Central in nature.	Forces are velocity-dependent and retarding in nature.	
	When only a conservative force acts within a system, the kinetic energy and potential energy can change. However their sum, the mechanical energy of the system, does not change.	Work done against a non- conservative force may be disipiated as heat energy.	
5	Work done is completely recoverable.	Work done in not completely recoverable.	

#### 5. Work Done By Conservative Forces

#### I<sup>st</sup> format: (When constant force is given)

 $dw = \vec{F} \cdot d\vec{r} (d\vec{r} = dx\hat{\imath} + dy\hat{\jmath} + dz\hat{k})$ 

**II format:** (When F is given as a function of x, y, z)

$$dw = (F_x \hat{\imath} + F_y \hat{\jmath} + F_z \hat{k}) \cdot (dx \hat{\imath} + dy \hat{\jmath} + dz \hat{k})$$

$$\Rightarrow \quad dw = F_x dx + F_y dy + F_z dz$$

#### III rd format (perfect differential format)

 $dw = (y\hat{\imath} + x\hat{\jmath}).(dx\hat{\imath} + dy\hat{\jmath}) \Rightarrow dw = ydx + xdy$ 

#### 6. ENERGY

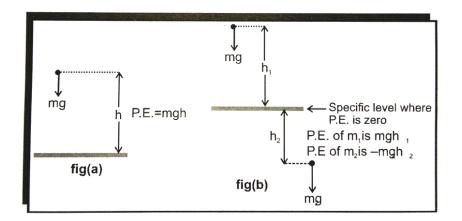
A body is said to possess energy if it has the capacity to do work. When a body possessing energy does some work, part of its energy is used up. Conversely if some work is done upon an object, will be given some energy. Energy and work are mutually convertible.

#### 6.1 Kinetic Energy

 $\mathsf{K}.\mathsf{E} = \frac{1}{2}mv^2$ 

#### 6.2 Potential Energy

 $W.D = -\Delta U$ Where  $\Delta U$  is change in potential energy



#### 6.2.1 Gravitational Potential Energy:

It is possessed by virtue of height. GPE =  $\pm$  mgh

**6.2.2** Elastic Potential Energy: It is a property of stretched or compressed springs. Elastic Potential Energy =  $\frac{1}{2}kx^2$ 

#### 7. Relation Between Potential Energy (U) and Conservation Force (F)

- If U is a function of only one variable, then  $F = -\frac{dU}{dr} = -$  slope of U-r graph If U is a function of three coordinate variables x, y and z, then (i)
- (ii)

$$F = -\left[\frac{\partial U}{\partial x}\hat{i} + \frac{\partial U}{\partial y}\hat{j} + \frac{\partial U}{\partial z}\hat{k}\right]$$

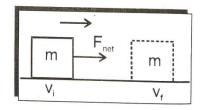
#### 8. EQUILIBRIUM

Physical situation	Stable equilibrium	Unstable equilibrium	Neutral equilibrium
Net force	Zero	Zero	Zero
Potential energy	Minimun	Maximum	Constant
When displaced mean (equilibrium) position.	A restoring nature of force will act on the body, which brings the body back towards mean position.	A force will act which moves the body away from mean position.	Force is again zero
In U-r graph	At point B	At point A	At point C
In F-r graph	At point A	At point B	At point C

#### 9. WORK ENERGY THEOREM:

 $W_{net} = \Delta K$ 

Work done by net force  $F_{net}$  in displacing a particle equals to the change in kinetic energy of the particle i.e.  $(W.D)_c (W.D)_{N.C} + (W.D)_{ext.} + (W.D)_{pseudo} = \Delta K$ Where  $(W.D)_c$  = work done by conservative force



#### **10.** Power of a Force

#### (i) Average power

$$: P_{av} = \frac{Total \ work \ done}{Total \ time \ taken} = \frac{W_{Total}}{t}$$

(ii) Instantaneous power

$$P_{ins.} = rate \ of \ doing \ work \ done = \frac{dW}{dt} = \vec{F} \cdot \vec{v} = Fv cos\theta$$

#### **11. Vertical Circular Motion**

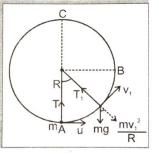
A bob of mass m is suspended from a light string of length R as shown. If velocity at bottommost point of bob is u, then depending on the value of u following three cases are possible

(i) If 
$$u \ge \sqrt{5gR}$$
, bob will complete the circle.

(ii) If 
$$\sqrt{2gR} < u < \sqrt{5gR}$$
, string will slack between

(iii If 
$$u \leq \sqrt{2gR}$$
 , bob will oscillate between CAB. In

this case V = 0 but T 
$$\neq$$
 0.



• If  $u = \sqrt{5gR}$ , bob will just complete the circle, In this case, velocity at topmost point is  $v = \sqrt{gR}$ , Tension in this critical case is zero at topmost point and 6 mg at bottommost point.

(iv) Condition for the body to reach B:

- If  $u \leq \sqrt{2gR}$  then the body will oscillate about A.
- (v) At height h from bottom velocity of bob will be,

$$v = \sqrt{u^2 - 2gH}$$

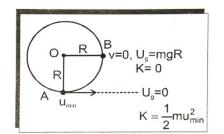
(vi)  $\sqrt{2gR} < u < \sqrt{5gR}$  then  $\cos \phi = \frac{u^2 - 2gR}{3gR}v$ 

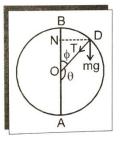
It is the angle from the vertical at which tension in the string vanishes to zero.

And after that its motion is projectile.

(vii) When 
$$u \ge \sqrt{5gR}$$
 Tension at A :  $T_A = 6mg$ 

**Tension at B:**  $T_B = 3mg$ 







## JEE FORMULA NOTES

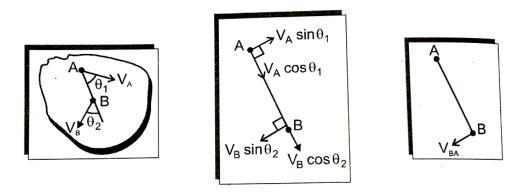
### **DEPTH Notes with Revision**

# PHYSICS

#### ROTATION

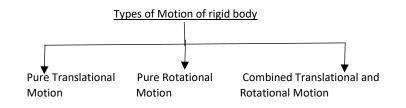
#### 1. RIGID BODY:

Rigid body is defined as a system of particles in which distance between each pair of particles remains constant (with respect to time) that means the shape and size do not change, during the motion. Eg. Fan, Pen, Table, stone and so on.



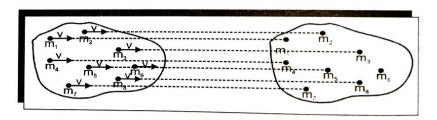
If the above body is rigid  $V_A cos \theta_1 = V_B cos \theta_2$ 

#### 2. TYPES OF MOTION OF RIGID BODY



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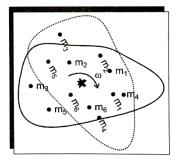
#### **2.1** Pure Translational Motion:



$$\vec{F}_{ext} = m_1 \vec{a}_1 + m_2 \vec{a}_2 + m_3 \vec{a}_3 + \dots$$

$$\vec{F}_{ext} = M\vec{a}$$

 $\vec{P} = m_1 \vec{a}_1 + m_2 \vec{a}_2 + m_3 \vec{a}_3 + \dots$ 2.2 Pure Rotational Motion:



Total Kinetic Energy  $= \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 + \dots = \frac{1}{2}I\omega^2$ Where I = Moment of Inertia =  $m_1r_1^2 + m_2r_2^2 + \dots$  $\omega$  = angular speed of body.

#### 2.3 Combined translational and rotational Motion

A body is said to be in translational and rotational motion if all the particles rotates about an axis of rotation and the axis of rotation moves with respect to the ground.

#### 3. MOMENT OF INERTIA

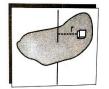
#### Moment of inertia depends on:

(i) Density of the material of body(iii) Axis of rotation

(ii) shape & size of body

#### 4. Moment of Inertia of Rigid Bodies

 $I = \int r^2 dm$ Where the integral is taken over the system.



#### 5. Two Theorems

(i) Theorem of parallel axes  $I = I_{CM} + mr^2$ or  $I_2 = I_1 + mr^2$ 



#### (ii) Theorem of parallel axes

 $I_Z = I_X + I_Y$ 



#### 6. Moment of Inertia of different body:

(i) Thin rod

$$I_1 = 0, \quad I_2 = \frac{ml^2}{12}, I_3 = \frac{ml^2}{3}$$
$$I_4 = \frac{ml^2}{12} \sin^2\theta, \ I_5 = \frac{ml^2}{3} \sin^2\theta$$

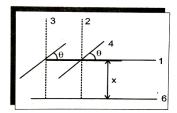


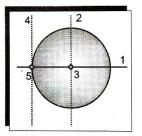
(iii)

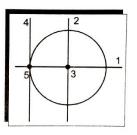
$$I_1 = I_2 = \frac{mR^2}{4}, I_3 = I_1 + I_2 = \frac{mR^2}{2}$$
$$I_4 = I_2 + mR^2 = \frac{5}{4}mR^2, I_5 = I_3 + mR^2 = \frac{3}{2}mR^2$$

 $I_4 = I_2 + mR^2 = \frac{3}{2}mR^2$ ,  $I_5 = I_3 + mR^2 = 2mR^2$ 

 $I_1 = I_2 = \frac{mR^2}{2}, I_3 = I_1 + I_2 = mR^2$ 



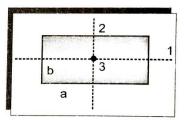




(iv) Rectangular slab

**Circular ring** 

$$I_1 = \frac{mb^2}{12}, I_2 = \frac{ma^2}{12}$$
$$I_3 = I_1 + I_2 = \frac{m}{12}(a^2 + b^2)$$

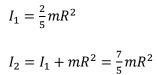


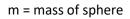
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#### (v) Square slab

$$I_1 = I_2 = I_3 = \frac{ma^2}{12}$$
$$I_4 = I_1 = I_3 = \frac{ma^2}{6}$$

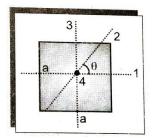


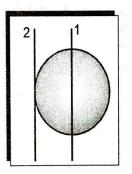


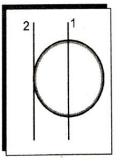


(vii) Hollow sphere









#### 7. Torque about point:

Torque of force  $\vec{F}$  about a point  $\vec{\tau} = \vec{r} \times \vec{F}$ 

#### 8. Torque about axis:

 $\vec{\tau} = \vec{r} \times \vec{F}$ 

Where  $\vec{\tau} =$  torque acting on the body about the axis of rotation

 $\vec{r}$  = position vector of the point of application of force about the axis of rotation.

 $\vec{F}$  = force applied on the body.

$$\vec{\tau}_{net} = \vec{\tau}_1 + \vec{\tau}_2 + \vec{\tau}_3 + \dots$$

#### 9. Body is in Equilibrium:-

We can say rigid body is in equilibrium when it is in

(a) Translational equilibrium

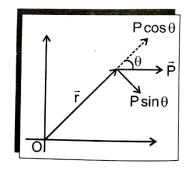
i.e. 
$$\vec{F}_{net} = 0 \Rightarrow F_{net x} = 0$$
 and  $F_{net y} = 0$  and

(b) Rotational equilibrium  $\vec{F}_{net} = 0$ , i.e., torque about any point is zero

#### **10. ANGULAR MOMENTUM**

#### 10.1 Angular momentum of a particle about a point.

$$\begin{split} \vec{L} &= \vec{r} \times \vec{P} \implies L = rp \sin \theta \\ |\vec{L}| &= r_{\perp} \times P, \\ |\vec{L}| &= P_{\perp} \times r \end{split}$$



#### 10.2 Angular Momentum of a rigid body rotating about a fixed axis

 $L = I\omega$ 

Here , I is the moment of inertia of the rigid body about axis.

**Note:** Angular momentum about axis is the component of  $I\vec{\omega}$  along the axis.

In the most of the cases angular momentum about axis is I

#### **10.3** Conservation of Angular Momentum:

Or 
$$\vec{\tau}_{net} = \frac{\vec{dL}}{dt}$$
 Now, suppose that  $\vec{\tau}_{net} = 0$ 

then  $\frac{\vec{dL}}{dt} = 0$  , so that  $\vec{L} = \text{constant}$ .

#### 10.4 ANGULAR IMPULSE

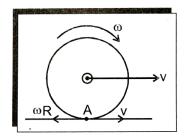
The angular impulse of a torque in a given time interval is defined as  $\int_{t_1}^{t_2} \vec{\tau} \, dt$ 

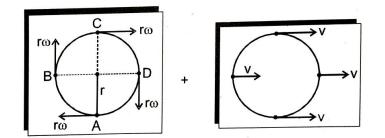
$$ec{ au}=rac{ec{\mathrm{d} ec{L}}}{\mathrm{d} t}$$
 ,  $ec{ au}\,dt=dec{L}$  or  $\int_{t_1}^{t_2}ec{ au}\,dt$ 

= angular impulse =  $\vec{L}_2 - \vec{L}_1$ 

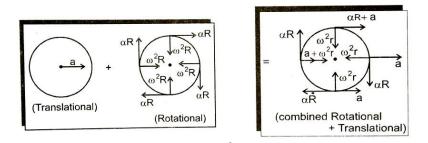
#### 11. Combined Translational and Rotational Motion of a Rigid Body:

- To understand the concept of combined translational and rotational motion we consider a uniform disc rolling on a or horizontal surface. Velocity of its center of mass is  $V_{COM}$  and its angular speed is  $\omega$  as shown in figure. We divide our problem in two parts
- (1) Pure Rotational + (2) Pure Translational about center of mass.





Acceleration of a point on the circumference of the body in R + T motion: The net acceleration of different points on the rigid body.

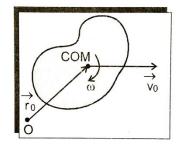


## 11.1 Angular momentum of a rigid body in combined rotation and translation

Let O be a fixed point in an inertial frame of reference.

Angular momentum of the body about O is.

$$\vec{L} = \vec{L}_{cm} + M(\vec{r}_0 \times \vec{v}_0)$$



## **12. UNIFORM PURE ROLLING**

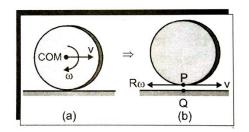
Pure rolling means no relative motion (or no slipping at point of contact between two bodies.)

$$v_p = v_Q$$

or 
$$v-R\omega = 0$$

or 
$$v = R\omega$$

If 
$$v_p > v_Q$$
 or  $v > Rac$ 



the motion is said to be forward slipping and if  $v_p < v_Q < R\omega$  ,the motion is said to be backward slipping.

Now, suppose an external force is applied to the rigid body, the motion will no longer remain uniform. The condition of pure rolling on a stationary ground is,

a = R $\alpha$ 

Thus,  $v = R\omega$ ,  $a = R\alpha$  is the condition of pure rolling on a stationary ground. Sometime it is simply said rolling.

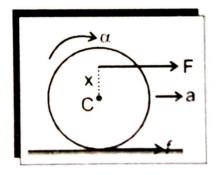
## **12.1** Pure rolling when force F act on a body:

a = linear acceleration,  $\alpha$  = angular acceleration

from linear motion: F + f = Ma

from rotational motion:  $Fx - Fr = I\alpha$ 

$$a = \frac{F(R+x)}{MR(C+1)}, f = \frac{F(x-RC)}{R(C+1)}$$



## **12.2** Pure Rolling on an Inclined Plane:

$$a = \frac{gsin\theta}{1+c}$$

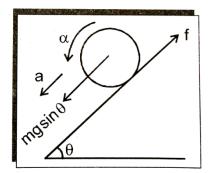
So body which have low value of C have greater acceleration.

Note: We can represent the moment of inertia of a different rigid body in a following way.

$$I = CMR^2$$

Value of C = 1 for circular ring (R),

C = 
$$\frac{1}{2}$$
 for circular disc (D) and solid cylinder (S.C)  
C =  $\frac{2}{3}$  for Hollow sphere (H.S), C =  $\frac{2}{5}$  for solid sphere (S.S)



## **13. TOPPLING**

Torque about E

Fb = (mg)a

Or 
$$a = \frac{Fb}{mg}$$

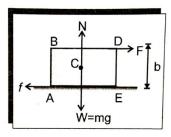
F increases

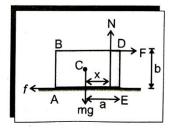
Fb + N (a – x) = mg a

If x = a

 $F_{max}b = mga$ 

$$F_{max} = \frac{mga}{b}$$







## JEE FORMULA NOTES

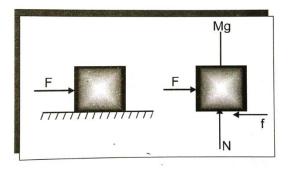
## **DEPTH Notes with Revision**

# PHYSICS

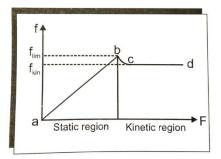
## FRICTION

## **1. FRICTION**

Friction is a contact force that opposes the relative motion or tendency of relative motion of two bodies.



## 1.1 Static frictional force



When there is no relative motion between the contact surfaces, frictional force is called static frictional force. It is a self- adjusting force The direction of static friction on a body is such that the total force acting force acting on It keeps it at rest with respect to the body in contact.

## **1.2 Limiting Frictional force**

This frictional force act when body is about to move. This is the maximum frictional force that can exist at thee contact surface.

(i) The magnitude of limiting fictional force is proportional to the normal force at the contact surface.  $F_{lim} \propto N \Rightarrow f_{lim} = \mu_s N$ 

Here  $\mu_s$  is a constant the value of which depends on nature of surfaces in contact and is called as 'coefficient of static friction'.

## **1.3 Kinetic Frictional Force**

Once relative motion starts between the surface in contact, the frictional force is called as kinetic frictional force is called as kinetic frictional force. The magnitude of kinetic frictional force is also proportional to normal force.

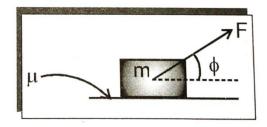
 $f_k = \mu_k N$ 

From the previous observation we can say that  $\mu_k < \mu_s$ 

Although the coefficient of kinetic frictional varies with speed, we shall neglect any variation

i.e., when relative motion starts a constant frictional force starts opposing its motion.

## 2. MINIMUM FORCE REQUIRED TO MOVE THE PARTICLE:

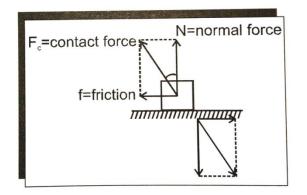


 $F = \mu mg / (cos\phi + \mu sin\phi)$ 

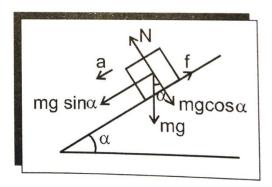
## **3. FRICITON AS THE COMPONENT OF CONTACT FORCE:**

The perpendicular component is called the normal contact force or normal force and parallel component is called friction.

$$F_{c max} = \sqrt{\mu^2 N^2 + N^2} \qquad \{when f_{max} = \mu N\}$$



## 4. MOTION ON A ROUGH INCLINED PLANE



## ANGLE OF REPOSE:

When, mg sin  $a_c = mg \cos a_c$   $\Rightarrow \tan a_c = \mu$ where  $a_c$  is called angle of repose



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

## **CENTRE OF MASS**

## 1. Centre of Mass of a System of 'N' Discrete Particles:

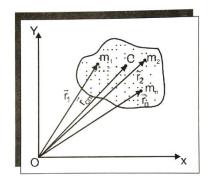
$$\vec{r}_{cm} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots + m_n \vec{r}_n}{m_1 + m_2 + \dots + m_n}$$

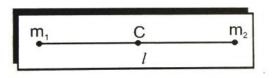
where,  $m_i \vec{r_i}$  is called the **moment of mass** of particle with respect to origin.

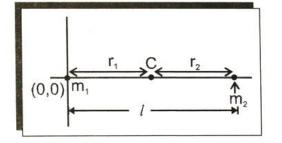
$$X_{COM} = \frac{\sum_{i=1}^{n} m_i x_i}{M}$$

Similarly,  $y_{COM} = \frac{\sum_{i=1}^{n} m_i y_i}{M}$  and  $z_{COM} = \frac{\sum_{i=1}^{n} m_i z_i}{M}$ 

2. Positon of COM of two particles:-







$$r_{1} = \frac{0 + m_{2}l}{m_{1} + m_{2}} = \frac{m_{2}l}{m_{1} + m_{2}} \qquad \dots (1)$$

$$r_{2} = l - \frac{m_{2}l}{m_{1} + m_{2}} = \frac{m_{1}l}{m_{1} + m_{2}} \qquad \dots (2)$$

$$m_{1}r_{1} = m_{2}r_{2} \qquad \dots (3)$$

Centre of mass of two particles system lie on the joining the Centre of mass of two particle system.

## 3. Centre of Mass of a Continuous Mass Distribution

For continuous mass distribution the Centre of mass can be located by replacing summation sign with an integral sign. Proper limits for the integral are chosen according to the situation

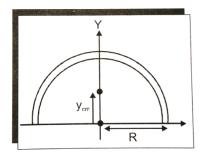
$$x_{cm} = \frac{\int x dm}{\int dm}$$
,  $y_{cm} = \frac{\int y dm}{\int dm}$ ,  $z_{cm} = \frac{\int z dm}{\int dm}$ 

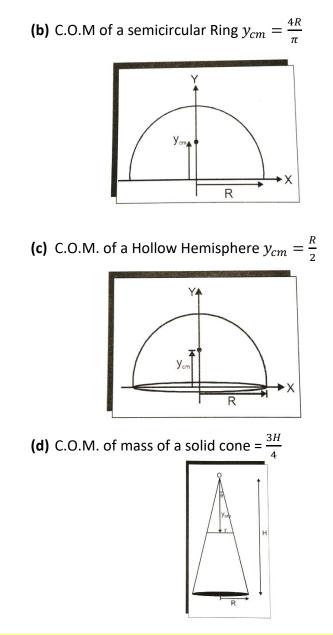
 $\int dm = M \ (mass \ of \ the \ body)$ 

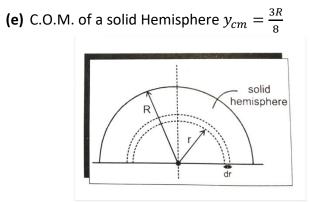
here x,y,z in the numerator is the coordinate of the center of mass of the dm mass.

$$\vec{r}_{cm} = \frac{1}{M} \int \vec{r} dm$$

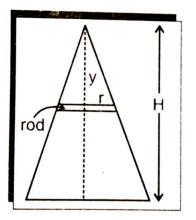
(a) C.O.M of a semicircular Ring  $y_{cm} = \frac{2R}{\pi}$ 







(f) C.O.M. of mass of triangular plate  $y_{cm} = \frac{2H}{3}$ 



## 4. CAVITY PROBLEMS:

If some mass or area is removed from a rigid body then the position of Centre of mass of the remaining portion is obtained by assuming that in a remaining part +m & - m mass is there.

## 5. Velocity of C.O.M of system:

To find the velocity of Centre of mass we differentiate equation (1) with respect to time

$$\frac{d\vec{r}_{com}}{dt} = \frac{m_1 \frac{d\vec{r}_1}{dt} + m_2 \frac{d\vec{r}_2}{dt} + m_3 \frac{d\vec{r}_3}{dt} + \cdots}{m_1 + m_2 + m_3 + \cdots}$$

$$\Rightarrow \vec{v}_{com} = \frac{m_1 \frac{d\vec{r}_1}{dt} + m_2 \frac{d\vec{r}_2}{dt} + m_3 \frac{d\vec{r}_3}{dt} + \cdots}{m_1 + m_2 + m_3 + \cdots}$$

$$\vec{v}_{com} = \frac{m_1 v_1 + m_2 v_2 + m_3 v_3 \dots}{m_1 + m_2 + m_3 \dots} \qquad \dots (2)$$

## 6. Acceleration of Centre of mass of the system:-

To find the acceleration of C.O.M we differentiate equation (2)

$$\Rightarrow \frac{d\vec{v}_{com}}{dt} = \frac{m_1 \frac{d\vec{v}_1}{dt} + m_2 \frac{d\vec{v}_2}{dt} + m_3 \frac{d\vec{v}_3}{dt} + \cdots}{m_1 + m_2 + m_3 + \cdots}$$

$$\vec{a}_{com} = \frac{m_1 \vec{a}_1 + m_2 \vec{a}_2 + m_3 \vec{a}_3 \dots}{m_1 + m_2 + m_3 \dots} \qquad \dots (3)$$

Now  $(m_1 + m_2 + m_3)$ 

$$\vec{a}_{com} = m_1 \vec{a}_1 + m_2 \vec{a}_2 + m_3 \vec{a}_3 + \dots$$

$$\vec{F}_{net(system)} = \vec{F}_{1net} + \vec{F}_{2net} + \vec{F}_{3net} + \dots$$

The internal forces which the particles exert on one another play absolutely no role in the motion of the Centre of mass.

## Case I : If $F_{net} = 0$ then we conclude:

- (a) The acceleration of Centre of mass is zero ( $\vec{a}_{com} = 0$ ) If  $a_1, a_2, a_3$  .... is acceleration of  $m_1, m_2, m_3$  mass in the system then  $a_1, a_2, a_3$  may or may not be zero.
- (b) K.E. of the system is not constant it may change due to internal force.
- (c) Velocity of Centre of mass is constant ( $\vec{a}_{com} = constant$ ) but v<sub>1</sub>, v<sub>2</sub>, v<sub>3</sub> may or may not constant. It may be change due to internal force.

From eq (2)  $m_1 \vec{v}_1 + m_2 \vec{v}_2 + m_3 \vec{v}_3$ + ...... = constant This is called momentum conservation.

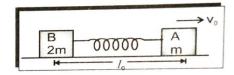
## "If resultant external force is zero on the system, then the net momentum of the system must remain constant".

## Case II: When Centre of mass is at rest.

$$\vec{v}_{com} = 0$$
 then  
 $\frac{d\vec{r}_{com}}{dt} = 0 \implies \vec{r}_{com} = constant.$ 

i.e.  $\vec{r}_1, \vec{r}_2, \vec{r}_3$  ..... may or may not change

## 7. SPRING BLOCK SYSTEM:



Maximum extension 
$$x_0 = v_0 \sqrt{\frac{2}{3k}}m$$

$$x_{max} = x_1 + x_2 = \frac{2mF}{k(m+F)}$$

## 8. IMPULSE:

Impulse of a force  $\vec{F}$  acting on a body for the time interval t =t<sub>1</sub> to t = t<sub>2</sub> is defined as

$$\vec{I} = \int_{t_1}^{t_2} \vec{F} dt$$

$$\vec{I} = \int_{t_1}^{t_2} \vec{F} dt = \int m \frac{d\vec{v}}{dt} dt = \int m d\vec{v}$$

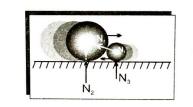
$$\vec{I}=m(\vec{v}_2-\vec{v}_1)=\Delta \vec{P}=$$
 change in momentum due to force  $\vec{F}$ 

Also 
$$\vec{I}_{Re} = \int_{t_1}^{t_2} \overrightarrow{F_{Res}} dt = \Delta \vec{P}$$
 (impulse – momentum theorem)

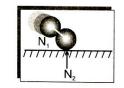
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## 9. Impulsive force:

A force, of relatively higher magnitude and acting for relatively shorter time, is called impulsive force. An impulsive force can change the momentum of a body in a finite magnitude in a very short time interval. Impulsive force is a relative term. There is no clear boundary between an impulsive and Non-Impulsive force.



 $N_1$ ,  $N_3$  = Impulsive;  $N_2$  = non-impulsive



## Both normal are Impulsive 10. COEFFICIENT OF RESTITUTION (e)

The coefficient of restitution is defined as the ratio of the impulses of reformation and deformation of either body.

 $e = \frac{Impulse \ of \ reformation}{Impulse \ of \ deformation} = \frac{\int F_r dt}{F_d dt}$ 

 $e = \frac{Velocity of separation of point of contact}{Velocity of approach of point of contact}$ 

## 11. Line of Motion

The line passing through the center of the body along the direction of resultant velocity.

## 12. Line of Impact

The line passing through the common normal to the surfaces in contact during impact is called line of impact. The force during collision acts along this line on both the bodies.

Direction of Line of impact can be determined by:

- (a) Geometry of colliding objects like spheres, discs, wedge etc.
- (b) Direction of change of momentum.

If one particle is stationary before the collision then the line of impact will be along its motion after collision.

 $e = \frac{velocity \ of \ seperation \ along \ line \ of \ impact}{velocity \ of \ approach \ along \ line \ of \ impact}$ 

## 13. Conservation of Linear Momentum

(i) For a single mass or single body If net force acting on the body is zero. Then,  $\vec{p} = constant$  or  $\vec{v} = constant$ (if mass = constant)

### (ii) For a system of particles or system of rigid bodies

If net external force acting on a system of particles or system of rigid bodies is zero, then,

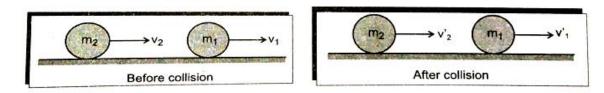
 $\vec{P}_{CM} = constant$  or  $\vec{V}_{CM} = constant$ 

## **14. COLLISION**

### In every type of collision only linear momentum remains constant

## (i) Head on elastic collision

In this case linear momentum and kinetic energy both are conserved. After solving two conservation equations. We get

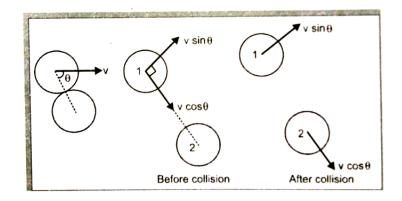


$$v_1 = \left(\frac{m_1 - m_2}{m_1 + m_2}\right) v_1 + \left(\frac{2m_2}{m_1 + m_2}\right) v_2$$

and 
$$v_1 = \left(\frac{m_2 - m_1}{m_1 + m_2}\right) v_2 + \left(\frac{2m_1}{m_1 + m_2}\right) v_1$$

## (ii) Head on inelastic collision

- (a) In an inelastic collision, the colliding particles do not regain their shape and size completely after collision.
- (b) Some fraction of mechanical energy is retained by the colliding particles in the form of deformation potential energy. Thus, the kinetic energy of the particles no longer remains conserved.
- (c) However, in the absence of external forces, law of conservation of linear momentum still holds good.
- (d) (Energy loss)<sub>Perfectly Inelastic</sub> > (Energy loss)<sub>Partial Inelastic</sub>
- (e) 0 < e < 1



(iii) Oblique collision (both elastic and inelastic)

Ball	Component along common tangent direction		Component along common normal direction	
	Before	After	Before	After
	collision	collision	collision	collision
1	$v \sin_{\theta}$	$v sin_{\theta}$	$v \cos \theta$	0
2	· 0	0	0	νcosθ

## 15. Variable Mass

(i) We now consider those mass is variable, i.e. those in which mass enters or leaves the system. A typical case is that of the rocket from which hot gases keep on escaping thereby continuously decreasing its mass.

(ii) Magnitude of thrust force is given by, 
$$\vec{F}_r = \left| \vec{v}_r \left( \pm \frac{dm}{dt} \right) \right|$$

**Note:** Direction of  $\vec{F}_t$  is parallel to  $\vec{v}_r$  if mass of system is increasing or  $\frac{dm}{dt}$  is positive. Direction of  $\vec{F}_t$  is antiparallel to  $\vec{v}_r$  if mass of system is decreasing or  $\frac{dm}{dt}$  is negative.

(iii) Based on this fact velocity of rocket at time t is given by

$$v = u - gt + v_r \ln\left(\frac{m_0}{m}\right)$$

Value of g has been assumed constant in above equation.

(iv) If mass is just dropped from a moving body then the mass which is dropped acquires the same velocity as that of the moving body.

Hence,  $\vec{v}_r = 0$  or no thrust force will act in this case.



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

## **CIRCULAR MOTION**

## 1. Angular Velocity $\omega$

## (i) Average Angular Velocity

$$\omega_{av} = \frac{\textit{Total Angle of Rotation}}{\textit{Total time taken}};$$

$$\omega_{av} = \frac{\theta_2 - \theta_1}{t_2 - t_1} = \frac{\Delta \theta}{\Delta t}$$

where  $\theta_1$  and  $\theta_2$  are angular position of the particle at time  $t_1$  and  $t_2$  respectively.

## (ii) Instantaneous Angular Velocity

The rate at which the position vector of a particle with respect to the center rotates, is called as instantaneous angular velocity with respect to the center.

$$\omega = \lim_{\Delta t \to 0} \frac{\Delta \theta}{\Delta \theta} = \frac{d\theta}{dt}$$

Relation between speed and angular velocity:

V = r $\omega$  is a scaler quantity  $\left(\vec{\omega} \neq \frac{\vec{v}}{r}\right)$ 

## 2. Relative Angular Velocity

$$\begin{split} \omega_{AB} &= \frac{(v_{AB})\perp}{r_{AB}} \\ \text{Here } v_{AB\perp} &= Relavitve \ velocity \ \perp \ to \ position \ vector \ AB \end{split}$$

## **3.** Angular Acceleration $\alpha$ :

## (i) Average Angular Acceleration:

Let  $\omega_1$  and  $\omega_2$  be the instantaneous angular speeds at times  $t_1$  and  $t_2$  respectively, then the average angular acceleration  $\alpha_{av}$  is defined as

$$\alpha_{av} = \frac{\omega_2 - \omega_1}{t_2 - t_1} = \frac{\Delta \omega}{\Delta \omega}$$

## (ii) Instantaneous Angular Acceleration:

It is t limit of average angular acceleration as  $\Delta t$  approaches zero, i.e.,

$$\alpha = \lim_{\Delta t \to 0} \frac{\Delta \omega}{\Delta t} = \frac{d\omega}{dt} = \omega \frac{d\omega}{d\theta}$$

### Important points:

- It is also axial vector with dimension  $[T^{-2}]$  and unit rad/s<sup>2</sup>
- If  $\alpha$  = 0, circular motion is said to be uniform.

• As 
$$\omega = \frac{d\theta}{dt}$$
,  $\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$ ,

i.e., second derivative of angular displacement w.r.t. time gives angular acceleration.

*α* is a axial vector and direction of *α* is along *ω* If *ω* increases and opposite to *ω* if *ω* decreases

## 4. Radial and tangential acceleration

$$a_t = \frac{dv}{dt}$$
 rate of change of speed  
and  $a_r = \omega^2 r = r \left(\frac{v}{r}\right)^2 = \frac{v^2}{r}$ 

## Following three points are important regarding the above discussion:

- (i) In uniform circular motion, speed (v) of the particle is constant, i.e.,  $\frac{dv}{dt} = 0$ . Thus,  $a_1 = 0$  and a =  $a_r = r\omega^2$
- (ii) In accelerated circular motion,  $\frac{dv}{dt}$  = positive, i.e.,  $a_t$  is along  $\hat{e}_t$ or tangential acceleration of particles is parallel to velocity  $\vec{v}$  because  $\vec{v} = r\omega\hat{e}_t$  and  $\vec{a}_t = \frac{dv}{dt}\hat{e}_t$
- (iii) In decelerated circular motion,  $\frac{dv}{dt}$  = negative and hence, tangential Acceleration is anti-parallel to velocity  $\vec{v}$ .

## Relation between angular acceleration and tangential acceleration

$$a_{\mathrm{t}} = rac{dv}{dt} = r rac{d\omega}{dt}$$
 or  $a_t = r lpha$ 

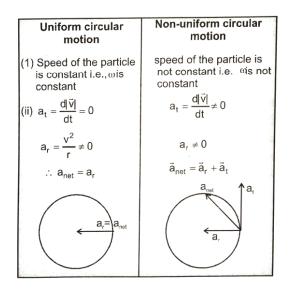
## 5. Relations among Angular Variables

These relations are also referred as equations of rotational motion and are-

$$\omega = \omega_0 + \alpha t \qquad \dots (1)$$
  

$$\omega = \omega_0 t + \frac{1}{2} \alpha t^2 \qquad \dots (2)$$
  

$$\omega^2 = \omega_0^2 + 2\alpha \theta \qquad \dots (3)$$



## 6. Centripetal Force:

**Concepts:** This is necessary resultant force towards the center called the centripetal force.

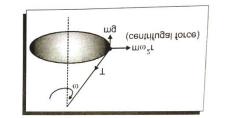
$$F = \frac{mv^2}{r} = m\omega^2 r$$

(i) A body moving with constant speed in a circle is not in equilibrium.

- (ii) It should be remembered that in the absence of the centripetal force thee body will move in a straight line with constant speed.
- (iii) It is not a new kind of force which acts on bodies. In fact, any force which is directed towards the center may provide the necessary centripetal force.

## 7. Centrifugal Force:

Centrifugal force is a fictitious force which has to be Applied as a concept only in a rotating frame of reference to apply Newton's law of motion (in that frame) FBD of ball w.r.t. non inertial frame rotating with the ball.

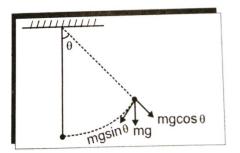


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## 8. SIMPLE PENDULUM:

 $T - \operatorname{mgcos}\theta = mv^2/L$ Or, T = M(gcos  $\theta$  +  $v^2/L$ )

$$\begin{aligned} \left|\vec{F}_{net}\right| &= \sqrt{(mgsin\theta)^2 + \left(\frac{mv^2}{L}\right)^2} \\ &= m\sqrt{g^2sin^2\theta + \frac{v^4}{L^2}} \end{aligned}$$



## 9. CONICAL PENDULUM:

Speed v =  $\frac{r\sqrt{g}}{(L^2 - r^2)^{1/4}}$  and

Tension T =  $\frac{mgL}{(L^2 - r^2)^{1/2}}$ 

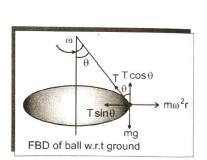
## **10. CIRCULAR TURNING ON ROADS:**

Centripetal force are provided by following ways.

## **10.1 By Friction Only**

For a safe turn without sliding safe speed

$$v \le \sqrt{\mu r g}$$
  
10.2 By Banking of Roads Only  $v = \sqrt{rgtan\theta}$ 



## **10.3** By Friction and Banking of Road Both

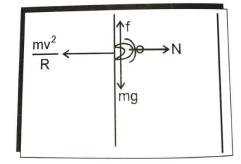
Maximum safe speed 
$$v_{max} = \sqrt{\frac{rg(\mu + tan\theta)}{(1 + \mu tan)}}$$

## 11. DEATH WELL:

N = 
$$\frac{mv^2}{R}$$
 ,  $f = mg$  ,  $f_{max} = \frac{\mu mv^2}{R}$ 

Cyclist does not drop down when

$$f_{max} \ge mg \Rightarrow \frac{\mu m v^2}{R} \ge mg, v \ge \sqrt{\frac{gR}{\mu}}$$





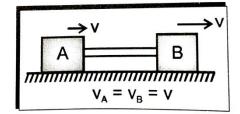
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# PHYSICS

## **CONSTRAINED MOTION**

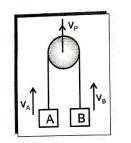
1. STRING CONSTRANT: Ist format: - (when string is fixed)



## II<sup>nd</sup> format(when pulley is also moving)

 $v_{AP} = -v_{AB}$ (-ve sign indicate the direction of each block is opposite with respect to Pulley)

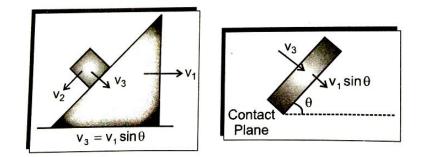
$$v_A - V_P = -v_B + v_P \qquad \Longrightarrow \qquad v_P = \frac{v_A - v_B}{2}$$



## **III format:**

- 1. First choose the longest string in the given problem which contains the point of which velocity/acceleration to be find out.
- 2. Now mark a point on the string wherever if comes in contact or leaves the contact of real bodies.
- **3.** If due to motion of a point , length of the part of a string with point is related, increases then its speed will be taken +ve otherwise –ve.

## 2. WEDGEE CONSTRAINED:



Components of velocity and acceleration perpendicular to the contact surface of the two objects is always equal if there is no deformation and they remain in contact.



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

## SIMPLE HARMONIC MOTION

## 1. Different Equations In SHM

(i) 
$$F = -kx$$

(ii) 
$$a = \frac{F}{m} = -\left(\frac{k}{m}\right)x = -\omega^2 x$$

(iii) 
$$\omega = \sqrt{\frac{k}{m}} =$$
 angular frequency of SHM

(iv) 
$$\frac{d^2x}{dt^2} = -\omega^2 x$$

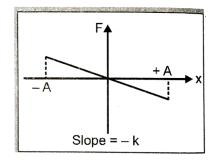
(v) 
$$F \propto -x$$
 or  $a \propto -x$ 

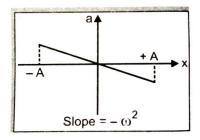
Is the sufficient and necessary condition for a periodic

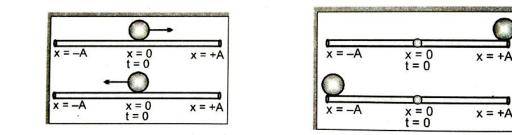
motion to be simple harmonic.

(vi) If x = A sin 
$$\omega t$$
 then  $v = \frac{dx}{dt} = \omega A \cos \omega t$  and  $a = \frac{dv}{dt} = -\omega^2 A \sin \omega t$ 

From these three equations we can see that x-t, v-t and a-t all three functions oscillate simple harmonically with same angular frequency  $\omega$ , Here x oscillates between +A and –A, v between + $\omega$ A and –  $\omega$ A and a between + $\omega^2 A$  and –  $\omega^2 A$ .

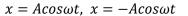




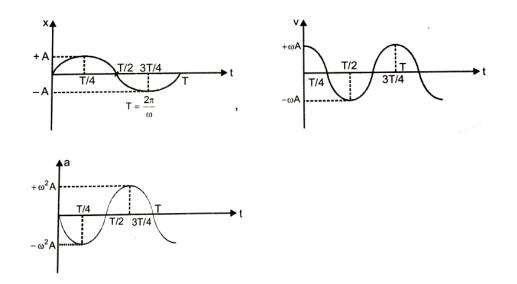


 $x = Asin\omega t, x = -Asin\omega t$ 

2.



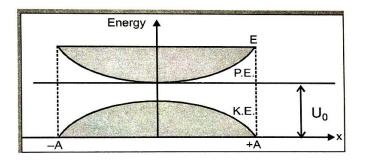
**3.** If  $x = Asin\omega t$ . Then,  $v = \omega Aco\omega t$  and  $a = -\omega^2$ . Corresponding x - t, v - t and a - t graphs are shown.



4.	Physical Quantity	At mean position	At extreme position	At general point
	Speed	ωΑ	zero	$\omega\sqrt{A^2-x^2}$
	Acceleration	zero	$\pm \omega^2 A$	$-\omega^2 x$
	Force	zero	$\pm kA$	-kx
	Kinetic energy	$\frac{1}{2}kA^2$	zero	$\frac{1}{2}k(A^2-x^2)$
		$\frac{1}{2}m\omega^2 A^2$		
	Potential energy	U <sub>0</sub>	$U_0 + \frac{1}{2}kA^2$	$U_0 + \frac{1}{2}kx^2$
	Total mechanical	$U_0 + \frac{1}{2}kA^2$	$U_0 + \frac{1}{2}kA^2$	$U_0 + \frac{1}{2}kA^2$

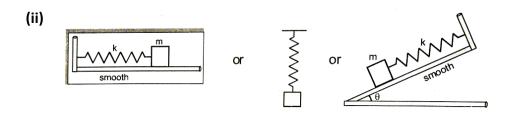
Energy  $U_0$  or potential energy at mean position can be zero.

5. Potential energy versus x or kinetic energy versus x graph is parabola. While total energy versus x graph is a straight line as it remains constant.



6. Spring Block System

(i) 
$$\omega = \sqrt{\frac{k}{m}}, T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{k}}, f = \frac{1}{T} = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

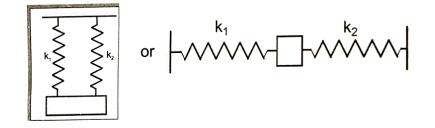


 $T = 2\pi \sqrt{\frac{m}{k}}$ 

In all three cases,

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#### (iii) Parallel combination



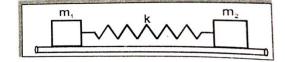
In both cases  $k_e = k_1 + k_2$ 

(iv) Series combination

$$k_e = \frac{k_1 k_2}{k_1 + k_2} \text{ or } \frac{1}{k_e} = \frac{1}{k_1} + \frac{1}{k_2}$$

(v) In case of two body oscillation,  

$$T = 2\pi \sqrt{\frac{\mu}{k}}$$
 where,  
 $\mu = \text{Reduced mass of two blocks} = \frac{m_1 m_2}{m_1 + m_2}$ 

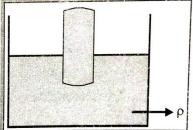


(vi) A blank of mass m and area of cross section A is floating in a liquid of density  $\rho$ . When depressed, it starts oscillating like a spring – block system.

Effective value of k in this case is

 $k=\rho Ag$ 

$$\therefore \quad T = 2\pi \sqrt{\frac{m}{\rho Ag}}$$



- (vii) If mass of spring m<sub>s</sub> is also given, then T =  $2\pi \sqrt{\frac{m + \frac{m_s}{3}}{k}}$
- (viii) Every wire is also like a spring of force constant given by  $k = \frac{YA}{1}$ .

From here itself we conclude that force constant of a spring is inversely proportional to its length. If length of spring is halved its force constant will become two times.

#### 7. Pendulum

(i) Only small oscillations of a pendulum are simple harmonic in nature:

$$T = 2\pi \sqrt{\frac{l}{g}} \,.$$

(ii) Second's pendulum is one whose time period is 2 s and length is 1 m.  $X = A \sin \omega t, x = -A \sin \omega t$   $X = A \cos \omega t, x = -A \cos \omega t$  (iii) Time period of a pendulum of length of the order of radius of earth is

$$T = 2\pi \sqrt{\frac{1}{g\left(\frac{1}{l} + \frac{1}{R}\right)}}$$

From here we can see that

$$T = 2\pi \sqrt{\frac{R}{g}}$$
 or 84.6 min if  $\rightarrow \infty$ .

Hence time period of a pendulum of infinite length is  $2\pi \sqrt{\frac{R}{g}}$ Or 84.6 min, Further,

$$T = 2\pi \sqrt{\frac{\iota}{g}} \text{ if } \ll R \text{ or } \frac{1}{\iota} \gg \frac{1}{R}.$$

(iv) If point of suspension has an acceleration  $\vec{a}$ , then T =  $2\pi \sqrt{\frac{l}{|g_e|}}$ Here  $\vec{g}_e = \vec{g} - \vec{a} = \vec{g} + (-\vec{a})$ 

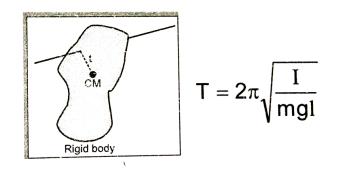
> **For example** if point of suspension has an upward acceleration  $\vec{a}$ , then  $(-\vec{a})$  is downwards or parallel to  $\vec{g}$ . Hence,  $|\vec{g}_e| = g + a$

or T = 
$$2\pi \sqrt{\frac{1}{g+a}}$$

(v) If a constant force  $\vec{F}$  (in addition to weight and tension ) acts on the bob then,

$$T = 2\pi \sqrt{\frac{1}{|g_e|}}$$
 Here,  $\vec{g}_e = \vec{g} + \frac{\vec{F}}{m}$ 

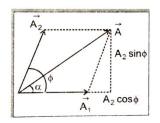
8. Physical Pendulum



#### 9. Combination of two S.H.M

Suppose the two individual motions are represented by,

 $\begin{array}{ll} x_1 = A_1 \sin \omega t \\ \text{And} & x_1 = A_1 \sin \omega t \\ \text{Both the simple harmonic motions have same} \\ \text{Angular frequency} \ . \end{array}$ 



Then the resultant motion is given by

$$x = x_1 + x_2 = A_1 \sin \omega t + A_2 \sin(\omega t + \emptyset) = A \sin(\omega t + \alpha)$$

Here, 
$$\sqrt{A_1^2 + A_2^2 + 2A_1A_2\cos\phi}$$
 and  $\tan \alpha = \frac{A_2\sin\phi}{A_1 + A_2\cos\phi}$ 

#### Important point to remember before solving the questions.

- **1.** Convert all the trigonometric ratios into sine form and ensure that  $\omega t$  terms is with +ve sign.
- 2. Make the sign between two term +ve.
- **3.** A<sub>1</sub> is the amplitude of that S.H.M whose phase is small.
- 4. Then resultant  $x = A_{net}$  is the vector sum of  $A_1 \& A_2$  with angle between them is the phase difference between two S.H.M



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

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### WAVES

1. In any type of wave, oscillations of a physical quantity y are produced at one place and these oscillations (along with energy and momentum) are transferred to other places also.

#### 2. Classification of Waves

A wave may be classified in following three ways.

**First** a transverse wave is one in which oscillations of y are perpendicular to wave velocity. Electromagnetic waves are transverse in nature. Sound wave are longitudinal in nature.

**Second** Mechanical waves require medium for their propagation. Sound wave are mechanical in nature. Non mechanical waves do not require medium for their propagation.

**Third** Transverse string wave is one dimensional. Transverse waves on the surface of water are two dimensional. Sound wave due to a point source is three dimensional.

#### 3. Wave Equation

In any wave equation y = f(x,t)

Only those functions of x and t represent a wave equation which satisfy

$$\frac{\partial^2 y}{\partial x^2} = (constant) \ \frac{\partial^2 y}{\partial t^2}$$

Here constant =  $\frac{1}{v^2}$  where v is the wave speed.

All functions of x and t of type,  $y = f(ax \pm bt)$  then

(i) Wave travels along positive x- direction. If ax and bt have opposite signs and it travels along negative x-direction if they have same signs.

#### 4. Plane Progressive Harmonic Wave

General equation of this wave is,  $y = A \sin(\omega t \pm kx \pm \phi)$ Or  $y = A \cos(\omega t \pm kx \pm \phi)$ In these equations,  $T = \frac{2\pi}{\omega}, \omega = 2\pi f = \frac{1}{2} = \frac{\omega}{2\pi}$ (i) k is wave number,  $k \frac{2\pi}{\lambda}$ (ii) Wave speed  $v = \frac{\omega}{k} = f\lambda$ 

#### 5. Particle Speed $(v_p)$ And Wave Speed (v) In case of Harmonic Wave

(i) y = f(x,t) where x and t are two variables. So,  $v_p = v \frac{\partial y}{\partial x}$ (ii) In Harmonic wave, particles in SHM. (iii) **Relation between**  $v_p$  and v;  $v_p = -v \frac{\partial y}{\partial x}$ 

#### 6. Phase Difference ( $\Delta \phi$ )

Case I

 $\Delta \phi = \omega(t_1 - t_2) \text{ or } \Delta \phi = \frac{2\pi}{T}, \Delta t = \text{phase difference of one particle at a time interval of } \Delta t$ . **Case II**  $\Delta \phi = K(x_1 \sim x_2) = \frac{2\pi}{\lambda}. \Delta x = \text{ phase difference at onetime between two particles at a path difference of } \Delta x.$ 

#### 7. Energy Density (u), Power [P] And Intensity (I) In Harmonic Wave

(i) Energy density  $u = \frac{1}{2}\rho\omega^2 A^2$  = energy of oscillation per unit volume. (ii) Power  $P = \frac{1}{2}\rho\omega^2 A^2 Sv$  = energy transferred per unit time (S = Area) (iii) Intensity  $I = \frac{1}{2}\rho\omega^2 A^2 v$  = energy transferred per unit time per unit area.

#### 8. Longitudinal Wave

(i) There are three equations associated with any longitudinal wav y(x, t),  $\Delta P(x, t)$  and  $\Delta \rho(x, t)$ (ii) y represents displacement of medium particles from their mean position parallel to direction of wave velocity. (iii) From y(x,t) equation, we can make  $\Delta P(x, t)$  equation by using the fundamental relation between them,  $\Delta P = -B \cdot \frac{\partial Y}{\partial x}$  and  $\Delta \rho = -\rho \cdot \frac{\partial y}{\partial x}$ B = Bulk Modulus. (iv)  $\Delta P_0 = BAk$  and  $\Delta \rho_0 = \rho Ak$ (v)  $\Delta P(x, t)$  and  $\Delta \rho(x, t)$  are in same phase. But y(x,t) equation has a phase difference of  $\frac{\pi}{2}$  with rest two equations.

 $v = \sqrt{\frac{T}{\mu} = \frac{T}{\rho S}}$ 

 $v = \sqrt{\frac{E}{\rho}}$ 

 $\therefore v = \sqrt{\frac{P}{\rho}}$ 

#### 9. Wave Speed

(i) Speed of transverse wave on a stretched wire:

(ii) Speed of longitudinal wav:

(a) In solids, E = Y = Young's modulus of elasticity: 
$$v = \sqrt{\frac{Y}{\rho}}$$

(b) In gases, According to Newton.

 $E = B_r$  = Isothermal bulk modulus of elasticity = P

But result did not match with this formula. Laplace made correction in it. According to him,

$$\gamma = \frac{c_p}{c_v} = 1 + \frac{2}{f} \text{ (f = degree of freedom)}$$
  
= Adiabatic bulk modulus of elasticity =  $\gamma p$ 

$$\therefore \qquad v = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\gamma RT}{M}} = \sqrt{\frac{\gamma kT}{M}}$$

#### 10. Effect of Temperature, Pressure And Relative Humidity in Speed of Sound In Air (On In A Gas)

(i) With temperature v  $\propto \sqrt{T}$ 

- (ii) With pressure Pressure has no effect on speed of sound as long as temperature remains constant.
- (iii) With relative humidity: With increase in relative humidity in air, density decreases, Hence, speed of sound increase.

#### 11. Sound Level (L)

L =  $10 log_{10} \frac{I}{I_0}$  (in dB)

Here  $I_0$  = intensity of minimum audible sound

$$= 10^{-12} watt/m^2$$

While comparing loudness of two sounds we may write,

$$L_2 - L_1 = 10 \log_{10} \frac{l_2}{l_1}$$

In case of point source,  $I \propto \frac{1}{r^2}$  or  $\frac{l_2}{l_1} = \left(\frac{r_1}{r_2}\right)^2$ ,

In case of line source,  $I \propto \frac{1}{r}$  or,  $\frac{I_2}{I_1} = \left(\frac{r_1}{r_2}\right)$ ,

**12. Doppler Effect In sound:**  $\left(\frac{v \pm v_m \pm v_0}{v \pm v_m \pm v_s}\right)$ 

**13.** Beats:  $f_b = f_1 - f_2$   $(f_1 > f_2)$ 

#### 14. Stationary Waves

- (i) Stationary waves are formed by the superposition of two identical waves travelling in opposite directions.
- (ii) Formation of stationary waves is really the interference of two waves in which coherent (same frequency) source are required.
- (iii) By the work 'identical waves' we mean that they must have same value of v,  $\omega$ , and k. Amplitude may be different, but same amplitudes are preferred.
- (iv) In stationary wave all particle oscillate with same value of  $\omega$  but amplitudes varying from A<sub>1</sub>+A<sub>2</sub> to A<sub>1</sub>-A<sub>2</sub>. Points were amplitude is maximum (or A<sub>1</sub> + A<sub>2</sub>) are called antinodes (or points of constructive interference and points where amplitude is minimum (or A<sub>1</sub> A<sub>2</sub>) are called nodes (or points of destructive interference).
- (v) If  $A_1 = A_2 = A$ , them amplitude at antinode is 2A and at node is zero. In This case point at node do not oscillate.
- (vi) Points at antinodes have maximum energy of oscillation and points at nodes have minimum energy of oscillation and points at nodes have minimum energy of oscillation (zero when  $A_1 A_2$ ).
- (vii) Points lying between two successive nodes are in same phase. They are out of phase with the points lying between two neighboring successive nodes.
- (viii) Equation of stationary wave is of type,

 $Y = 2A \sin kx \cos \omega t \qquad \qquad y = A \cos kx \sin \omega t \quad \text{etc}$ 

This equation can also be written as,

 $y = A_X \sin \omega t$   $y = A_X \cos \omega t$ 

If x = 0 is a node then,  $A_x = A_0 \sin kx$ ,

If x = 0 is an antinode then,  $A_x = A_0 \cos kx$ 

Here  $A_0$  is maximum amplitude at antinode.

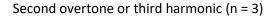
(ix) Energy of oscillation in a given volume can be obtained either by adding energies due to two individual waves travelling in opposite directions or by integration. Because in standing wave amplitude and therefore energy of oscillation varies point to point.

#### 15. Oscillation of Stretched Wire or Organ Pipes

(i) Stretched wire

Fundamental tone or first harmonic (n = 1)

First overtone or second harmonic (n = 2)



$$f = n\left(\frac{v}{2l}\right)$$
. Here, n = 1, 2, 3, .....

Even and odd both harmonics are obtained.

Here, 
$$v = \sqrt{\frac{T}{\mu}}$$
 or  $\sqrt{\frac{T}{\rho s}}$ 

(ii) **Open organ pipe** 

Fundamental tone or first harmonic (n = 1)









First overtone or second harmonic (n = 2)

Second overtone or third harmonic (n = 3)

$$f = n\left(\frac{v}{2l}\right)$$
, n = 1, 2, 3, .....

Even and odd both harmonics are obtained. Here, v = speed of sound in air.

v will be either given in the question, otherwise calculate from v =  $\sqrt{\frac{\gamma RT}{M}}$ .

#### (iii) Closed organ pipe

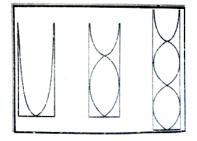
Fundamental tone or first harmonic (n = 1)

First overtone or third harmonic (n = 3)

Second overtone or fifth harmonic (n = 5)

$$f = n\left(\frac{v}{4l}\right) n = 1, 3, 5, \dots$$





#### Note:

(i) Stationary transverse wave are formed in stretched wire and longitudinal stationary waves are formed in organ pipes.

(ii) Open end of pipe is displacement antinode, but pressure and density nodes.

Closed end of pipe is displacement node, but pressure and density antinodes.

(iii) Laplace correction e = 0.6r (in closed pipe and 2e = 1.2r (in open pipe)

Hence, f =  $n\left[\frac{v}{2(l+1.2r)}\right]$  (in open pipe) and f =  $n\left[\frac{v}{4(l+0.6r)}\right]$  (in closed pipe)

(iv) If an open pipe and a closed pipe are of same lengths then fundamental frequency of open pipe is two times the fundamental frequency of closed pipe.



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

### ELASTICITY

**1.** Stress 
$$=\frac{F}{A}$$
 = restoring force per unit area.

**2.** Strain 
$$\frac{\Delta X}{X}$$
 = change per unit original.

- **3.** Modulus of Elasticity  $E = \frac{Stress}{Strain}$
- 4. Materials which offer more resistance to external deforming forces have higher value of modulus of elasticity.

#### 5. Young's Modulus of Elasticity

$$Y = \frac{F/A}{\Delta 1/1} = \frac{F_1}{A\Delta 1}$$
 F = Mg and A =  $\pi r^2$ 

6. Bulk Modulus of Elasticity

$$\mathsf{B} = \frac{F/A}{\Delta V/V} = -\frac{\Delta p}{\frac{\Delta V}{V}} \quad or \quad -\frac{dp}{dV/V}$$

7. Shear Modulus of Elasticity or Modulus of Rigidity

- 8. Solids have all three moduli of elasticities, Young's modulus, bulk modulus and shear modulus. Whereas liquids and gases have only bulk modulus.
- **9.** Every wire is like a spring whose force constant is equal to.

$$\mathsf{k} = \frac{YA}{l} \quad or \quad k \propto \frac{1}{l}$$

**10.** Potential energy stored in a stretched wire

$$\mathsf{U} = \frac{1}{2}k(\Delta l)^2 = \frac{1}{2} \left(\frac{YA}{l}\right) (\Delta l)^2$$

**11.** Potential energy stored per unit volume (also called energy density) in a stretched wire,

$$U = \frac{1}{2} \times Stress \times Strain$$

**12.** Change in Length of a Wire  $\Delta l = \frac{Fl}{AY}$ 

Here F is tension in the wire. If wire is having negligible mass, tension is uniform throughout the wire and change in length is obtained directly. Otherwise by integration.

- **13.** In case of solids and liquids bulk modulus is almost constant. In case of a gas, it is process dependent. In isothermal process  $B = B_T = p$ In adiabatic process  $B = B_s = \gamma p$
- 14. Compressibility = 1/B
- **15.** When pressure is applied on a substance, its volume decreases, while mass remains constant. Hence its density will increases,

$$\rho' = \frac{\rho}{1 - \Delta p/B} \text{ or } \rho' = \rho \left(1 + \frac{\Delta p}{B}\right) \text{ if } \frac{\Delta p}{B} \ll 1$$



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

### **FLUID MECHANICS**

1. The pressure P is defined at that point as the normal force per unit area, i.e.,

$$P\frac{dF_{\perp}}{dA}$$

2. Relative Density (or Specific Gravity) of any Substance  $RD = \frac{Density of that substance}{Density of that substance}$ 

$$=\frac{Density of vital substant}{Density of water}$$

Weight in air = Change in weight in water when completely immersed in it

**3.** Effect of Temperature on Density:

$$\rho' = \frac{\rho}{1 + \gamma \Delta \theta}$$

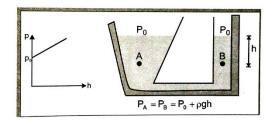
4. Effect of Pressure on Density:

$$\rho' = \frac{\rho}{1 - \frac{\Delta p}{B}}$$

**5.** 1 Pa = 1 Nm  $^{-2}$ , 1 Bar =  $10^5$  Pa,  $1 \text{ atm} = 1.013 \times 10^5 \text{ Pa}$ 

Gauge pressure = absolute pressure – atmospheric pressure

**6.** Pressure at depth h below the surface of water,  $p = p_0 + \rho g h$ 



Change in pressure per unit depth  $rac{dp}{dh}=
ho g$ 

#### 7. Barometer

$$p_1 = p_2$$
  

$$\therefore \qquad p_0 = h\rho g$$

Or 
$$h = \frac{p_0}{\rho g}$$
  
h is approximately 76cm of mercury.

#### 8. Force on Side Wall of Vessel

Net force can be evaluated by Integrating equation

$$\mathsf{F} = \int dF = \int_0^h x \rho g b dx$$

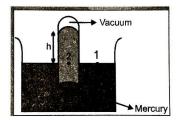
 $\mathsf{F} = \frac{\rho g b h^2}{2}$ 

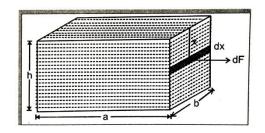
8.1 Average Pressure on Side Wall

$$\langle p \rangle_{av} = \frac{F}{bh} = \frac{1}{2} \frac{\rho g b h^2}{bh} = \frac{1}{2} \rho g h$$

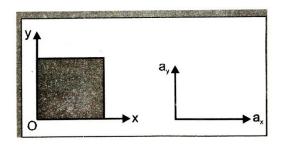
8.2 Torque on the Side Wall due to Fluid Pressure This net torque is

$$\tau = \int d\tau = \int_0^h \rho g b (hx - x^2) dx = \frac{1}{6} \rho g b h^2$$





8.3 Pressure Distribution in an Accelerated Frame



If container has an acceleration component  $a_{\boldsymbol{x}}$  in x-direction and  $a_{\boldsymbol{y}}$  in y-direction. Then,

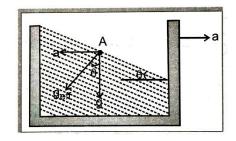
$$rac{dp}{dx} = -
ho a_x$$
 and  $rac{dp}{dy} = -
ho ig(a_y+gig)$ 

Due to acceleration of container, liquid filled in it experience a pseudo force Relative to container and due to this the free surface of liquid which normal to the gravity

$$\theta = \tan^{-1}\left(\frac{a}{g}\right)$$

Pressure at a point A in the accelerated container as shown in figure is given as

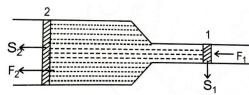
$$P_A = P_0 + h\rho \ \sqrt{a^2 + g^2}$$



#### 9. PASCAL'S PRINCIPLE

"The pressure applied at one point in an enclosed fluid is transmitted uniformly to every part of the fluid and to the walls of the container."

$$F_2 = p_2 \times S_2 \Rightarrow F_2 = \frac{F_1}{S_1} \times S_2$$



#### **10. ARCHIMEDE'S PRINCIPLE**

If a heavy object is immersed in water, it seems to weight less than when it is in air. This is because the water exerts an upward force called **buoyant force**. It is equal to the weight of the fluid displaced by the body.

A body wholly or partially submerged in a fluid is buoyed up by a force equal to the weight of the displaced fluid. This result is known as **Archimedes' principle.** 

- (i) Up thrust  $F = V_i \rho_I g_e$
- (ii) When a solid whose density is less than the density of liquid floats in it then, some fraction of solid remains immersed in the liquid. In this case,

(i) Weight = Up thrust (ii) Fraction of volume immersed  $f = \frac{\rho_s}{\rho_l}$ 

(iii) When a solid whose density is more than the density of liquid is completely immersed in it then upthrust acts on the 100% volume and apparent weight is less than its actual weight.  $W_{ann} = W - F$ 

#### **11. ASSUMPTIONS OF IDEAL FLUID**

- (1) Fluid is incompressible: density of fluid remain constant throughout the fluid.
- (2) Fluid is non-viscous: fluid friction is absent
- (3) Doesn't show rotational effect: If we release anybody in the flowing section there it will not rotate about its C.O.M.
- (4) Stream line flow: velocity of fluid at any particular point remains constant with time It may vary with position.

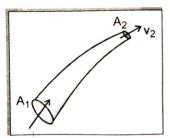
#### **12. EQUATION OF CONTINUITY**

According to the equation of continuity, if flow is steady mass of fluid entering at end A, per second = mass of fluid leaving the end  $A_2$  per second.

$$\frac{dV}{dt} = A_1 v_1$$

According to the definition of steady flow

$$A_1 v_1 \rho = A_2 v_2 \rho \quad or \quad A_1 v_1 + A_2 v_2 \quad or \quad v \propto \frac{1}{A}$$



#### **13. BERNOULLIS EQUATION**

It relates the variables describing the steady laminar of liquid. It is based on energy conservation.

#### Assumptions

The fluid is incompressible, non-viscous, non-rotational and streamline flow.

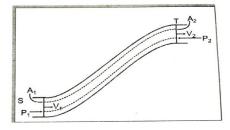
$$p + \rho gh + \frac{1}{2}\rho v^{2} = constant$$

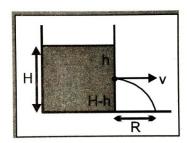
$$p_{1} + \rho gh_{1} + \frac{1}{2}\rho v_{1}^{2} = p_{2} + \rho gh_{2} + \frac{1}{2}\rho v_{2}^{2}$$
(i)  $v = \sqrt{2gh} = \sqrt{2gh_{top}}$ 
(ii)  $t = \sqrt{\frac{2(H-h)}{2}} = \sqrt{\frac{2h_{bottom}}{2}}$ 

(ii) 
$$t = \sqrt{\frac{2(H-h)}{g}} = \sqrt{\frac{2h_{bottom}}{g}}$$

(iii) R = vt = 
$$2\sqrt{h(H-h)} = 2\sqrt{h_{top} \times h_{bottom}}$$

(iv) 
$$R_{max} = H \text{ at } h = \frac{H}{2}$$





(v) Time taken to empty a tank if hole is made at bottom.

$$t = \frac{A}{a} \sqrt{\frac{2H}{g}}$$

#### 14. Pitot Tube

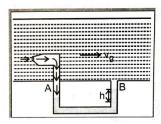
It is a device used to measure flow velocity of fluid.

It if the a liquid of density  $\rho$ , then

$$P_A = P_B = h(\rho - \rho_g)g$$

Now if we apply Bernoulli's equation at ends A and B we'll have

$$\frac{1}{2}\rho_g^2 = P_A - P_B = h\rho g$$



**Note:** *Pitot tube is also used to measure velocity of aero planes with respect to wind. It can be mounted at the top surface of the plain and hence the velocity of wind can be measured with respect to plane.* 

#### 15. (a) COHESIVE FORCE

The force of attraction between the molecules of the same substance is called cohesive force

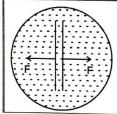
#### **15. (b) ADHESIVE FORCE**

The force at attraction between the molecules of different substances is called adhesive force.

#### **16. SURFACE TENSION**

The property of a liquid at rest due to which its free surface tries to have minimum surface area and behaves as if it were under tension somewhat like a stretched elastic membrane is called surface tension.

T = (F/L)



#### **16.1 SURFACE ENERGY**

When the surface area of a liquid is increased, the molecules from the interior rise to the surface. This requires work against force of attraction of the molecules just below the surface. This work is stored in the form of potential energy.

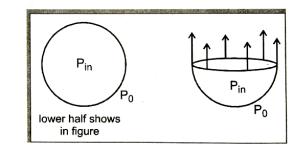
One has to apply an external force F equal and opposite to it to keep the wire in equilibrium. Thus,

F = 2TL

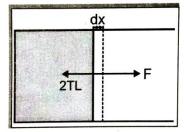
But (2l) (dx) is the total increases in area of both the surface of the film. Let is be Da. Then,

dW = Tda or 
$$T = \frac{dW}{dA}$$

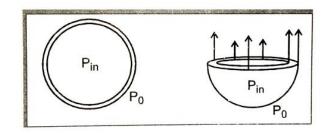
#### 16.2 Excess Pressure Insider a liquid drop:



$$P_{in} - P_0 = \frac{2T}{R} = Excess Pressure$$



#### 16.3 Excess pressure inside a bubble



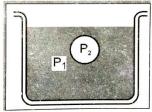
 $P_{in} - P_0 = \frac{4T}{R} = \text{Excess pressure}$ 

#### Note:

(1) If we have an air bubble inside a liquid, a single surface is formed. On the convex side.

The pressure in the concave side (that is in the liquid ) by an amount  $\frac{2T}{R}$ .

$$\therefore \qquad P_2 - P_1 = \frac{2T}{R}$$



**16.4** For any curved surface excess pressure on the concave side =  $2T\left(\frac{1}{R_1} + \frac{1}{R_2}\right)$  For spherical curved surface  $R_1, R_2$ 

16.5 Pressure inside a charged bubble:

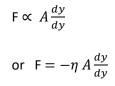
$$P_{in} = P_0 + \frac{4T}{R} - \frac{\sigma^2}{2\varepsilon_0}$$

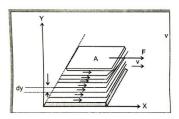
17. CAPILLARY ACTION: Capillary rise or fall.

$$h = \frac{2T}{R\rho g} = \frac{2Tcos\theta}{r\rho g}$$

$$\left(as R = \frac{r}{\cos\theta}\right)$$

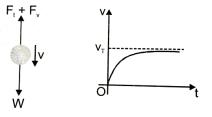
#### **18. VISCOSITY AND NEWTON'S LAW OF VISCOUS FORCE**





The negative sign shows that viscous force on a liquid layer acts in a direction opposite to the relative velocity of flow of fluid. Above Eq. is known as Newton's law of viscous force.

**19.** TERMINAL VELOCITY  $(V_T)$ 



$$v_T = \frac{2}{9} \frac{r^2(\rho - \sigma)g}{\eta}$$



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

#### GRAVITATION

#### 1. Gravitational force between two point Masses is

$$F = G \frac{m_1 m_2}{r^2}$$

#### 2. Acceleration Due to Gravity

(i) On the surface of earth  $g = \frac{GM}{R^2} = 9.81 m s^{-2}$ (ii) At height h from the surface of earth.

$$\mathbf{g} = \frac{g}{\left(1 + \frac{h}{R}\right)^2} = g\left(1 - \frac{2h}{R}\right)$$
 if h << R

(iii) At depth d from the surface of earth.

$$g = g\left(1 - \frac{d}{R}\right)$$

g' = 0 if d = R ie, at center of earth (iv) Effect of rotation of earth at latitude  $\emptyset$ ,

 $g' = g - R\omega^2 cos^2 \phi$ At equator  $\phi = 0, g' = g - R\omega^2 = minimum value.$ At poles,  $\phi = 90^\circ, g' = g = maximum value.$ At equator effect of rotation of earth is maximum and value of g is minimum. At pole effect of rotation of earth is zero and value of g is maximum.

#### 3. Field Strength

(i) Gravitation field strength at a point in gravitational field is defined as,

 $\vec{E} = \frac{\vec{F}}{m} = gravitational force per unit mass.$ 

(ii) Due to a mass point

$$E = \frac{GM}{r^2}$$
 (towards the mass) or  $E \propto \frac{1}{2}$ 

(iii) Due to solid sphere Inside points

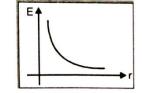
$$E_{i} = \frac{GM}{R^{3}}r$$
  
At r = 0, E = 0 i.e., Centre  
At r = R, E =  $\frac{GM}{R^{2}}$  *ie, on surface*

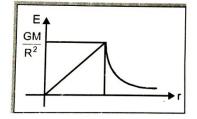
Outside points,  $E_0 = \frac{GM}{R^2}$  ie, on surface As  $r \to \infty$ ,  $E \to 0$ On the surface E-r graph is continuous.

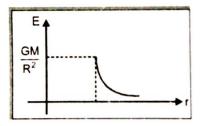
(iv) Due to a spherical shell Inside points,  $E_i = 0$ 

Outside point,  $E_0 = \frac{GM}{r^2}$ 

At the surface,  $E = \frac{GM}{R^2}$ On the surface E-r graph is discontinuous.





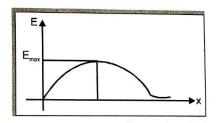


(v) On the axis of a ring

$$E_x = \frac{GMx}{(R^2 + x^2)^{3/2}}$$

At x = 0, E = 0 ie, at Centre

If x>>R, E = 
$$\frac{GM}{x^2}$$



Ie, ring behaves as a point mass As  $x \to \infty, E \to 0$ 

$$E_{max} = \frac{2GM}{3\sqrt{3R^2}}$$
 at  $x = \frac{R}{\sqrt{2}}$ 

#### 4. Gravitational Potential

(i) Gravitational potential at a point in a gravitational field is defined as the negative of work done by gravitational force in moving a unit mass from infinity to that point.

Thus,

$$V_P = \frac{W_{\infty} \to P}{m}$$

(ii) Due to a point mass

$$V = -\frac{Gm}{r}$$
$$V \to \infty \text{ as } r \to 0$$
And V  $\to 0 \text{ as } r \to \infty$ 

(iii) Due to solid sphere Inside points

$$V_i = -\frac{GM}{R^3} (1.5R^2 - 0.5r^2)$$
  
At r = R, V =  $-\frac{GM}{R}$  ie, on surface  
At r = 0, V =  $1.5\frac{GM}{R}$  ie, at centre.

V-r graph is parabolic for inside points and potential at center is 1.5 times the potential at surface.

**Outside points** 
$$V_0 = -\frac{GM}{R}$$
 ie, on surface

At 
$$r = R$$
,  $V = -\frac{GM}{R}$  ie, on surface  
As  $r \to \infty$ ,  $V \to 0$ 

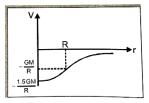
(iv) Due to a spherical shell

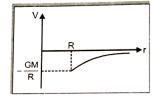
Inside points 
$$V_i = -\frac{GM}{R} = constant$$

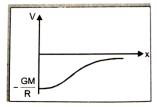
Outside points  $V_0 = -\frac{GM}{R}$ 

(v) On the axis of a ring

$$V_x = -\frac{GM}{\sqrt{R^2 + X^2}}$$
  
At x = 0, V =  $-\frac{GM}{R}$  ie, at centre,  
This is the minimum value.  
As  $x \to \infty$ ,  $V \to 0$ 







#### 5. Gravitation Potential Energy

(i) This is negative of work done by gravitational forces in making the system from infinite separation to the present position. (ii) Gravitational potential energy of two points masses, is  $U = -\frac{Gm_1m_2}{r}$ 

(iii) To find gravitational potential energy of more than two point masses we have to make pairs of masses, neither of the pair should be repeated. For example, in case of four point masses.

$$U = -G\left[\frac{m_4m_3}{r_{43}} + \frac{m_4m_2}{r_{42}} + \frac{m_4m_1}{r_{41}} + \frac{m_3m_2}{r_{32}} + \frac{m_3m_1}{r_{31}} + \frac{m_3m_1}{r_{21}}\right]$$

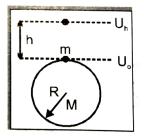
For n point masses, total number of pairs will be  $\frac{n(n-1)}{2}$ .

If a point mass m is placed on the surface of earth, The potential energy here is  $U_0 = -\frac{GMm}{R}$  and potential

Energy at height h is  $U_h = -\frac{GMm}{(R+h)}$ The difference in potential energy would be

$$\Delta U = U_h - U_0 \text{ or } \Delta U = \frac{mgh}{1 + \frac{h}{R}}$$

If h << R,  $\Delta U = mgh$ 



#### 6. Relation Between Field Strength $\vec{E}$ and potential V

(i) If V is a function of only one variable (say r) then,

$$E = -\frac{dV}{dr} = -$$
 slope of V-r graph

(ii) If V is a function of three coordinate variables x, y and z then,

$$\vec{E} = -\left[\frac{\partial V}{\partial x}\hat{i} + \frac{\partial V}{\partial y}\hat{j} + \frac{\partial V}{\partial z}\hat{k}\right]$$

#### 7. Escape Velocity

(i) From the surface of earth,

$$v_e = \sqrt{2gR} = \sqrt{\frac{2GM}{R}} \quad \left(as \ g = \frac{GM}{R^2}\right) = 11.2 km s^{-2}$$

(ii) Escape velocity does not depend upon the angle at which particle is projected from the surface.

#### 8. Motion of Satellites

(i) Orbital speed

$$v_0 = \sqrt{\frac{GM}{r}}$$

 $\mathsf{K} = \frac{GMm}{2r}$ 

(ii) Time period  $T = \frac{2\pi}{\sqrt{GM}} r^{3/2}$ 

(iv) Potential energy 
$$U = -\frac{GMm}{2r}$$

(v) Total mechanical energy 
$$E - \frac{GMm}{2r}$$

• Near the surface of earth, r = R and 
$$v_0 = \sqrt{\frac{GM}{R}} = \sqrt{gR} = 7.9 km s^{-1}$$

This is the maximum speed of earth's satellite.

Time period of such a satellite would be,

$$T = \frac{2\pi}{\sqrt{GM}} R^{3/2} = 2\pi \sqrt{\frac{R}{g}} = 84.6min$$

This is the minimum time period of any earth's satellite.

9. Kepler's laws

Keplar's three empirical laws describe the motion of planets.

First law Each planet moves in an elliptical orbit, with the sun at one focus of the ellipse.

**Second law** The radius vector, drawn from the sun to a planet, sweeps out equal areas in equal time interval ie, areal velocity is constant. This law is derived from law of conservation of angular momentum.

$$\frac{dA}{dt} = \frac{L}{2m} = constant$$

Here L is angular momentum and m is mass of planet.

**Third law**  $T^2 \propto r^3$  where r is semi-major axis of elliptical path.

Circle is a special case of an ellipse. Therefore second and third laws can also be applied for circular path. In third law, r is radius of circular path.



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

## Heat

## 1. Calorimetry

(i) Q = ms $\Delta\theta$ , when temperature changes without change in state.

(ii) Q = MI, when state changes without change in temperature.

(iii) s = specific heat of any substance = heat required to increase the temperature of unit mass by 1°C or 1K.

(iv) c = heat capacity of a body = ms = heat required to increase the temperature of whole body by 1°C or 1K.

(v) Specific heat of water is 1 calg<sup>-1</sup> °C between 14.5°C and 15.5°C.

(vi) L = latent heat = heat required to convert unit mass of that substance from one to another state.

(vii) Water equivalent of a vessel It is mass of equivalent water which takes same amount of hat as take by the vessel for same rise of temperature.

## 2. Thermal Expansion

(i)  $\Delta l = l\alpha\Delta\theta$ ,  $\Delta s = s\beta\Delta\theta$  and  $\Delta V = V\gamma\Delta\theta$ (ii)  $\beta = 2\alpha$  and  $\gamma = 3\alpha$  for isotropic medium. (iii) **Time period of pendulum**:

$$\mathsf{T} = 2\pi \sqrt{\frac{l}{g}} \quad or \qquad T \propto \sqrt{l}$$

Increasing Temperature  $\Delta \theta$  :

$$\Delta T = (T' - T) = \frac{1}{2}T\alpha\Delta\theta$$

Time lost/gained  $\Delta t = \frac{\Delta T}{T_{t}} \times t$ 

(iv) **Thermal Stress:** strain 
$$\frac{\Delta l}{l} = \alpha \Delta \theta$$

$$\therefore \qquad F = A \times \text{stress} = YA\alpha\Delta\theta$$

Rod applies this much force on wall to expand.

## 3. Effect of temperature on different physical quantities

(i) **On Density** : 
$$\rho' = \rho(1 - \gamma, \Delta\theta)$$
 if  $\gamma, \Delta\theta \ll 1$ 

(ii) In Fluid Mechanics Case 1 :  $\rho_s < \rho_l$ 

Fraction f =  $\frac{\rho_s}{\rho_l}$ 

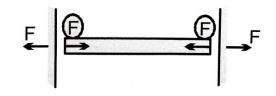
When temperature is increased,  $\rho_s$  and  $\rho_l$  both will decreases, Hence, fraction may increase, decrease or remains same. At higher temperature,  $f'\left(\frac{1+\gamma_l\Delta\theta}{1+\gamma_s\Delta\theta}\right)$ 

If  $\rho_l < \rho_s$  , f' >f or immersed fraction will increase.

Case 2:  $\rho_s < \rho_l$   $W_{app} = W - F$ 

Here  $F_S = \rho_l g$ 

With increase in temperature V<sub>s</sub> will increase and  $\rho_l$  will decrease, while g will remain unchanged. Therefore upthrust may increase, decrease or remain same.



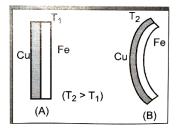
At some higher temperature.  $F' = \left(\frac{1+\gamma_S \Delta \theta}{1+\gamma_I \Delta \theta}\right)$ 

If  $\gamma_S > \gamma_l$ , upthrust will increase. Therefore apparent weight will decrease.

## (iii) Bimetallic Strip

## Note

If two strips of equal length but of different metals are placed on each other and riveted, the single strip so formed is called '**bimetallic strip'** [see given fig.].



## 4. Heat Transfer

## Heat conduction through a rod

(i) Heat flow in steady state  $Q = \frac{kA(\theta_1 - \theta_2)}{l}t$ (ii) Rate of flow of heat = heat current or  $H = \frac{dQ}{dt} = \frac{TD}{R}$ Here TD = temperature difference =  $\theta_1 - \theta_2$  and R = thermal resistance =  $\frac{l}{KA}$ 

## 5. SLABS IN PARALLEL AND SERIES

## (a) Slabs in series (in steady state):

$$R = R_1 + R_2 + R_3 + \dots$$

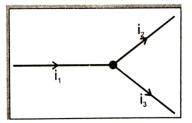
(b) Slabs in parallel:

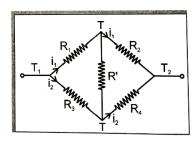
$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

## 6. Junction Law

According to the Junction law thee sum of all the heat current Directed towards a point is equal to the sum of all the heat currents Directed away from the points.

 $i_1 = i_2 + i_3$ 





## WHEAT STONE BRIDGE

 $R_1R_4 = R_2R_3$ 

## 7. Radiation

(i) Absorptive power a =  $\frac{energy \ absorbed}{energy \ incident}$   $a \le 1, a = 1 \ for \ perfectly \ black \ body$ 

(ii) Spectral absorptive power  $a_{\lambda}$  = absorptive power of wavelength  $\gamma$ .

 $a_{\lambda} \leq 1, a_{\lambda} = 1$  for perfectly black body

(*iii*) Emissive power e Energy radiated per unit area per unit time is called emissive power of a body.

(iv) **Spectral emissive power**  $e_{\lambda}$  Emissive power of wavelength  $\lambda$  is known as spectral emissive power  $\int_{0}^{\infty} e_{\lambda} d_{\lambda}$ .

(v) Kirchhoff's law If different bodies (including a perfectly block body) are kept at same temperature, than

$$e_{\lambda} \propto a_{\lambda}$$
 or  $\frac{e_{\lambda}}{a_{\lambda}} = constant$ 

or =  $(e_{\lambda})_{\text{Perfectly blackbody}}$ 

\* Good absorbers of a particular wavelength  $\lambda$  are also good emitters of same wavelength  $\lambda$ .

\* At a given temperature, ration of  $e_{\lambda}$  and  $a_{\lambda}$  for anybody is constant. This ration is equal to  $e_{\lambda}$  of perfectly black body at that temperature.

- (vi) Stefan's law Emissive power of a body is given by,  $e = e_r \sigma T^4$
- Here  $e_r$  = emissivity, emittance, relative emissivity or relative emittance.
  - $e_r \leq 1, e_r = 1$  for a perfectly black body.
- (vii) Total energy radiated by a body,  $E = e_r \sigma T^4 A t$
- (viii)  $a = e_r$  or absorptivity of a body = its emissivity.
- (ix) Cooling of a body by radiation

(a) Rate of cooling = 
$$-\frac{dT}{dt} = \frac{e_r A_\sigma}{ms} (T^4 - T_0^4)$$
 or  $-\frac{dT}{dt} \propto T^4 - T_0^4$ 

- (b) Newton's law of cooling when  $\Delta T$  is small then Rate of cooling  $\propto$  temperature difference.
- (c) If body cools by radiation according to Newton, then temperature of body decreases exponentially.
- (d) Shortcut approximation of  $e^{-at}$  then

$$\left(\frac{\theta_1 - \theta_2}{t}\right) = \alpha \left[\frac{\theta_1 - \theta_2}{t} - \theta_0\right]$$

(x) Wien's displacement law

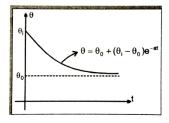
$$\lambda_m \propto \frac{1}{T}$$
 or  $\lambda_m T = constant$ 

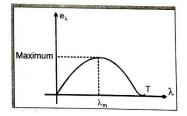
= Wien's constant 'b' =  $2.89 \times 10^{-3} m - K$ Further, area of this graph will give total emissive power which is proportional to  $T^4$ .

## 8. Kinetic theory of Gases

(i) pV = nRT =  $\frac{m}{M}$  RT (m = mass of gas in gms)

(ii) Density 
$$ho = rac{m}{V}$$
 (General ) =  $rac{p_M}{RT}$  (for ideal gas)





(iii) Four speeds,  $v = \sqrt{\frac{ART}{M}} = \sqrt{\frac{Akt}{m}} = \sqrt{\frac{Ap}{\rho}}$ 

Here, m = mass of one gas molecule.

A = 3 for rms speed of gas molecules, =  $\frac{8}{\pi} \approx 2.5$  for average speed of gas molecules = 2 for most probable speed of gas molecules =  $\gamma = \frac{C_p}{C_p}$  for speed of sound in a gas

(iv) 
$$p = \frac{1}{3} \frac{mn}{V} v^2 rms$$

(v)  $p = \frac{2}{3}E$ . Here, E = total translational kinetic energy per unit volume

(vi) f = degree of freedom = 3 for monoatomic gas

= 5 for diatomic and linear polyatomic gas = 6 for nonlinear polyatomic gas

- (a) Vibrational degree of freedom is not taken into consideration.
- (b) Translational degree of freedom for any type of gas is three.

(vii) Total internal energy of a gas is,  $U = \frac{nf}{2}RT$ 

Here, n = total number of gram moles

(viii) 
$$C_V = \frac{dU}{dT}$$
 (where U = internal energy of one mole of a gas =  $\frac{1}{2}$  RT)

$$\therefore \quad C_V = \frac{f}{2}R = \frac{R}{\gamma - 1}$$
(ix)  $C_p = C_V + R = \left(1 + \frac{f}{2}\right)R = \left(\frac{\gamma}{\gamma - 1}\right)R$ 
(x)  $\gamma = \frac{C_p}{C_v} = 1 + \frac{2}{f}$ 

(xi) Internal energy of 1 mole in one degree of freedom of nay gas is  $\frac{1}{2}RT$ 

(xii) Translational kinetic energy of 1 mole of monoatomic gas is zero of dia or linear polyatomic gas is  $\frac{2}{3}RT$  or RT, of nonlinear polyatomic gas is  $\frac{3}{2}RT$ .

## 9. THERMODYNAMICS

9.1 Gas laws

(a) **Boyle's law** is applied when T = constant,  $p \propto \frac{1}{V}$ 

(b) **Charle's law**  $p = constant or, process is isobaric, V \propto T$ 

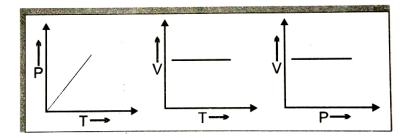
(c) Pressure law or Gay Lussac's law Is applied when V = constant or process is isochoric,  $p \propto T$ 

**9.2 First law of thermodynamics** It is a law of conservation of energy given by,  $Q = \Delta U + W$ 

**PROCESS:** 

(i) Isochoric process:

Since change in volume is zero therefore, Dw = 0, Dv = 0

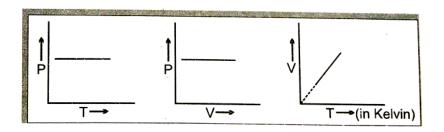


$$\Delta U = n \frac{f}{2} R \Delta T, \Delta Q = \Delta U = n \frac{f}{2} R \Delta T$$

(ii) Isobaric Process: Pressure remains constant in isobaric process

 $\therefore \quad P = constant \implies \frac{V}{T} = constant$ 

Indicator diagram of isobaric process:



$$\Delta W = P \Delta V = P(V_{final} - V_{initial}) = nR(T_{final} - T_{initial})$$
$$\Delta W = n\frac{f}{2}R\Delta T, \Delta Q = \Delta U + \Delta W$$
$$\Delta Q = n\frac{f}{2}R\Delta T + P[V_f - V_i] = n\frac{f}{2}R\Delta T + nR\Delta T$$

Above expression gives an idea that to increase temperature by  $\Delta T$  in isobaric process heat required is more than is isochoric process.

## (iii) Cyclic Process:

In the cyclic process initial and final states are same therefore initial state = final state

Work done = Area enclosed under P-V diagram.

If the process on P-V curve is clockwise, then net work done is (+ve) and vice-versa.

## (iv) Free Expansion

 $\Delta Q = 0, \Delta U = 0$  and  $\Delta W = 0$ . Temperature in the free expansion remains constant.

### **10. MOLAR HEAT CAPACITY**

C = heat required to raise temperature of 1 mole of any substance by 1°C or 1

 $\mathsf{K.} = \frac{Q}{n\Delta T}$ 

Molar heat capacity of solids and liquid is almost constant.

In case of gases C is process dependent. It varies from O to  $\infty$ .

In isothermal process C =  $\propto as \Delta T = 0$ 

In adiabatic process C = 0 as Q = 0

 $C_P$  (molar heat capacity of isobaric process and  $C_V$  (molar heat capacity of isochoric process) are commonly used. In a general process  $pV^x$ 

= constant, molar heat capacity is given by,

$$\mathsf{C} = \frac{R}{\gamma - 1} + \frac{R}{1 - x}$$

## **11. MIXTURE OF NON RACTIVE GASES**

- (a)  $n = n_1 + n_2$  (b)  $p = p_1 + p_2$
- (c)  $U = U_1 + U_2$  (d)  $\Delta U = \Delta U_1 + \Delta U_2$

(e) 
$$C_{v} = \frac{n_{1}Cv_{1} + n_{2}Cv_{2}}{n_{1} + n_{2}}$$
 (f)  $C_{p} = \frac{n_{1}C_{p1} + n_{2}C_{p2}}{n_{1} + n_{2}} = C_{v} + R$ 

(g) 
$$\gamma = \frac{c_p}{c_v} \text{ or } \frac{n}{\gamma - 1} = \frac{n_1}{y_1 - 1} + \frac{n_2}{y_2 - 1}$$
 (h)  $M = \frac{n_1 M_1 + n_2 M_2}{n_1 + n_2}$ 



## JEE FORMULA NOTES

**DEPTH Notes with Revision** 

## PHYSICS

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## OPTICS

## **1. PROPERTIES OF LIGHT**

(i) Speed of light in vacuum, denoted by c, is equal to  $3 \times 10^8$  m/s approximately

(ii) Light is electromagnetic wave (proposed by Maxwell). It consists of varying electric field and magnetic field.

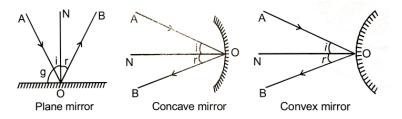
(iii) Light carries energy and momentum.

(iv) The formula  $v = f\lambda$  is applicable to light.

## 2. REFLECTION

When a ray of light is incident at a point on the surface, the surface throws partly or wholly the incident energy back into the medium of incidence. This phenomenon is called reflection.

Surfaces that cause reflection are known as mirror or reflectors. Mirrors can be plane or curved.



## 2.1 Law of reflection

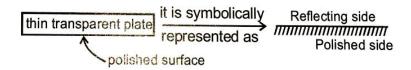
(i) The incident ray, the reflected ray and the normal to the reflecting surface at the point of incidence, all lie in the same plane. (ii) The angle of incidence is equal to the angle of reflection, i.e.,  $\angle i = \angle r$ 

(ii) The angle of incidence is equal to the angle of reflection, i.e.,  $\Sigma t = \Sigma t$ 

These laws hold good for all reflecting surfaces either plane or curved.

## 3. PLANE MIRROR

Plane mirror is formed by polishing one surface of a plane thin glass plate. It is also said to be silvered on one side.



## PLANE MIRROR

A beam of parallel rays of light , incident on a plane mirror will get reflected as a beam of parallel reflected rays. *Formation of image by a plane mirror.* 

From the argument of similar triangles

OM = /M

i.e., perpendicular distance of the object from the mirror = perpendicular distance of the image from the mirror

## Steps to draw the image:

- (i) Drop a perpendicular on the mirror and extend it on the back side of the mirror.
- (ii) Image always lie on this extended line
- (iii) To exactly locate the image,

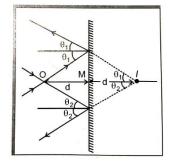
Use the concept:

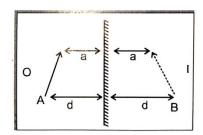
Perpendicular distance of the object form the mirror is equals to the perpendicular

distance from the mirror of the image.

## 3.1 Image of an extended linear object:

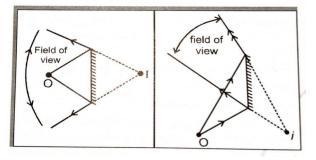
Draw the images of the extreme points and join them with a straight line





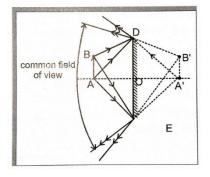
## **3.2 Field of view:**

Are in which reflected rays exists is called field of view. It is the area from which an observer can see the image of an object. If the observer is outside this area he will not be able to see the image although the image will be there.



Most of the problems in optics involving geometry can be solved by using similar triangles.

## 3.3 Field of view of extended linear object



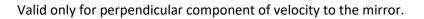
Common field of view of extreme points of the object will be the field of view of extended linear object.

## 3.4 Relation between velocity of object and image:

$$\Rightarrow v_{mG} = \frac{v_{iG} + v_{oG}}{2}$$

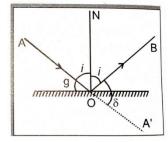
Here:

 $v_{iG}$  = velocity of image with respect to ground  $v_{oG}$  = velocity of object with respect to ground.  $v_{mG}$  = velocity of mirror with respect to ground.



## 3.5 Deviation produced by a Plane mirror

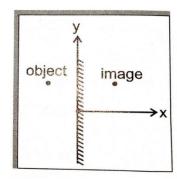
Deviation is defined as the angle between directions of the incident ray d the reflected ray (or, the emergent ray). It is generally denoted by  $\delta$ . Here,  $\angle A'OB = \delta = \angle AOA' - \angle AOB = 180^\circ - 2i$ Or,  $\delta = 180^\circ - 2i$ 

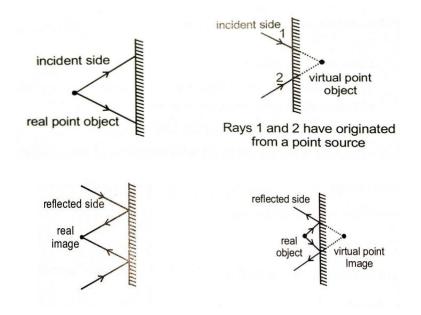


## 3.6 Real or virtual image/Object

## **Object and Image**

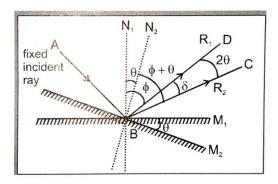
Object is defined as point of intersection of incident rays. Image is defined as point of intersection of reflected rays (in case of reflection) or refracted rays (in case of refraction).





## 4. ROTATION OF MIRROR

For a fixed incident light ray, if the mirror be rotated through an angle  $\theta$  (about an axis which lies in the plane of mirror and perpendicular to the plane of incidence), the reflected ray turns through an angle  $2\theta$  in same sense.

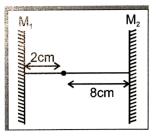


## 5. IMAGES FORMED BY TWO PLANEE MIRRORS

If rays after getting reflected from one mirror strike second mirror, the image formed by first mirror will function as an object for second mirror, and this process will continue for every successive reflection.

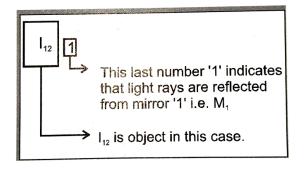
## 5.1 Images due to parallel plane mirrors:

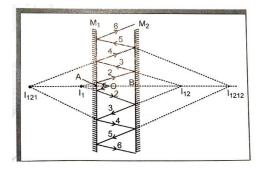
Ex. Figure shows a point object placed between two parallel mirrors. Its distance form  $M_1$  is 2 cm and that form  $M_2$  IS 8cm. Find the distance of images from the two mirrors considering reflection on mirror  $M_1$  first.



## Sol.

To understand how images are formed see the following figure and table. You will require to know what symbols like  $I_{121}$  stands for. See the following diagram.

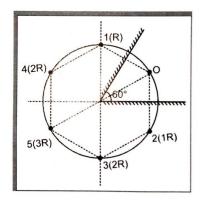




Incident rays	Ref.by	Ref. rays	Object	Image	Object distance	Image distance
Rays 1	M <sub>1</sub>	Rays 2	0	11	AO=2cm	Al <sub>1</sub> =2cm
Rays 2	M <sub>2</sub>	Rays 3	11	I <sub>12</sub>	Bl <sub>1</sub> =12cm	BI <sub>12</sub> =12cm
Rays 3	M <sub>1</sub>	Rays 4	I <sub>12</sub>	I <sub>121</sub>	Al <sub>12</sub> =22cm	Al <sub>121</sub> =22cm
Rays 4	M <sub>2</sub>	Rays 5	I <sub>121</sub>	I <sub>1212</sub>	BI121=32cm	BI1212=32cm

Similarly images will be formed by the rays striking mirror  $M_2$  first. Total number of images  $= \infty$ .

## 5.2 Circle concept



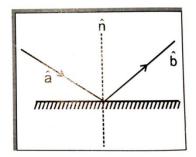
All the images formed will li on a circle whose centre is the intersection point of the mirror and radius equal to distance of object from the intersection point.

## 6. NUMBER OF IMAGES FORMED BY TWO INCLIND MIRRORS.

(i) if  $\frac{360^{\circ}}{\theta}$  = even number.; number of image  $= \frac{360^{\circ}}{\theta} - 1$ (ii) if  $\frac{360^{\circ}}{\theta}$  = odd number; number of image  $= \frac{360^{\circ}}{\theta} - 1$ , If the object is placed on the angle bisector. (iii) if  $\frac{360^{\circ}}{\theta}$  = odd number; number of image  $= \frac{360^{\circ}}{\theta}$ , If the object is not placed on the angle bisector. (iv) if  $\frac{360^{\circ}}{\theta} \neq$  integer, then the number of image = nearest even integer.

## **VECTOR – FORM**

- $\hat{a} = Unit \ vector \ along \ teh \ incident \ ray$
- $\hat{n} = \text{Unit normal vector}$
- $\hat{b} =$  Unit vector along the reflected Ray
- $\widehat{b} = \widehat{a} 2(\widehat{a}.\widehat{n})\widehat{n}$

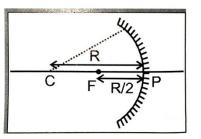


## 7. SPHERICAL MIRROR

## 7.1 RELATION BETWEEN u, v AND R FOR SPHERICAL MIRRORS

Where R is the radius of the Curvature of the mirror

 $\frac{1}{u} + \frac{1}{v} = \frac{2}{R}$  $\frac{1}{f} = \frac{1}{u} + \frac{2}{v}$ 



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## **IMPORTANT POINT**

Above formula is only valid for paraxial rays
 u, v and f should be put along with sign

## 7.2 MAGNIFICATION:

7.2.1 Transverse Magnification

 $\Delta ABO \sim \Delta A'B'O$ 

$$\mathbf{x} = \frac{h_i}{v} = \frac{h_o}{u} \Rightarrow m = \frac{h_i}{h_o} = -\frac{v}{u}$$

- The above formula is valid for both concave and convex mirror.
- Above the optical axis is considered positive and below to be negative
- $h_i, h_o$ , and u should be put with sign.

# $\begin{array}{c|c} & & & \\ & & \\ A' & h_0 & & \\ A & C & f & \\ \hline & h_i & & \\ & & \\ & & \\ B' & & \\ & & \\ & & \\ \end{array}$

## 7.2.2 Longitudinal Magnification

$$\frac{1}{V} + \frac{1}{u} = \frac{1}{f}$$

By differentiating

$$\implies \quad \frac{dv}{v^2} - \frac{du}{u^2} = 0 \implies \quad \frac{dv}{du} = -\frac{v^2}{u^2}$$

Longitudinal magnification when the size of object is quite less with respect to its distance from the pole.

Above formula is valid only when the length of object is very small as compared to the distance of object from the pole.

 $dv \rightarrow \text{length of image}$ 

 $du \rightarrow \text{length of object}$ 

- $u \rightarrow object distance from the pole.$
- $v \rightarrow$  Image distance from the pole.

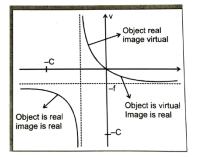
## FOR CONCAVE MIRROR

S.No	Position of object	Details of images
1.	At ∞	At F, real, inverted  m  << 1
2.	Between C and $\infty$	Beetween F and C, real inverted,  m  < 1
3.	At C	At C, real, inverted  m  = 1
4.	Between F and C	Between C and $_\infty$ , real, inverted, $ m  > 1$
5.	At F	At infinity, real, inverted,  m  > > 1
6.	Between F and P	Behind the mirror, virtual, erect  m  > 1

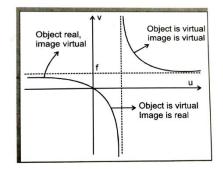
## FOR CONCAVE MIRROR

S.No	Position of object	Details of images		
1.	At infinity	At F, virtual, erect,  m  << 1		
2.	In front of mirror	Beetween P and F, virtual, erect,  m < 1		

u – v curve for spherical mirror



## FOR CONCAVE MIRROR



## FOR CONVEX MIRROR

- 7.3 Velocity in Spherical Mirror: Velocity of image
- (a) Object moving along principle axis:

$$V_{IM} = \frac{v^2}{u^2} (V_{OM})$$

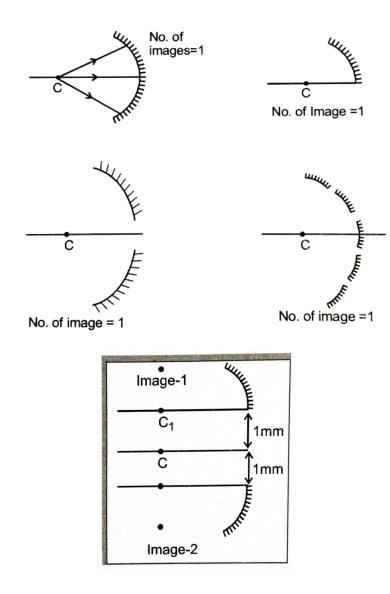
(b) Object moving perpendicular to principal axis

$$\frac{dh_i}{dt} = -\frac{v}{u}\frac{dh_o}{dt}$$

(c) Object moving parallel to Principal axis:

$$v_{y} = \frac{dh_{i}}{dt} = -h_{o}\left[\frac{dv}{dt} \cdot \frac{1}{u} - \frac{v}{u^{2}}\frac{du}{dt}\right]$$

## 8. CUTTING OF MIRRORS



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## 9. REFRACTION OF LIGHT

 $\mu = \frac{c}{v} = \frac{\text{speed of light in vaccum}}{\text{speed of light in medium}}$ 

## 9.1 Laws of Refraction:

(a) The incident ray, the normal to any refracting surface at the point of incidence and the refracted ray all lie in the same plane called the plane of incidence or plane of refraction.

(b) 
$$\frac{\sin i}{\sin r} = Constant$$
 for any pair of media

And for light of a given wavelength. This is known as *Snell's* Law.

Also, 
$$\frac{\sin i}{\sin r} = \frac{n_2}{n_1} = \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2}$$

For applying in problems remember

 $n_1 sin i = n_1 sin r$ 

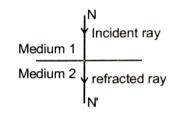
 $\frac{n_2}{n_1} = {}^1n_2 =$  Refractive Index of the second medium with respect to the first medium.

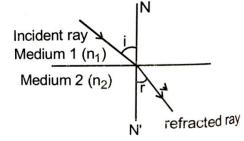
c = speed of light in air (or vaccum ) = 3 × 10<sup>8</sup> m/s.

*i* & r should be taken from normal.

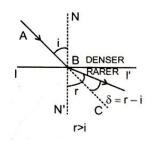
## Special cases:

 Normal incidence : i = 0 from snell's law: r = 0

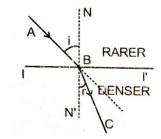




• When light moves from denser to rarer medium it bends away from normal.

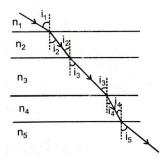


• When light moves from rarer to denser medium it bends towards the normal.



## 9.2 Plane Refraction:

Prove that  $n_1 \sin i_1 = n_2 \sin i_2 = n_3 \sin i_3 = n_4 \sin i_4$ = (**Remember this ).** Also Prove that if  $n_1 = n_4$  then Light rays in medium  $n_1$  and in medium  $n_4$  are parallel.

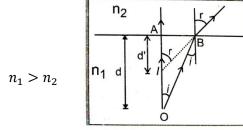


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## **10.** Apparent Depth and Normal Shift

Case I : When the object is in denser medium and the observer is in rarer medium (near normal incidence)

$$\frac{n_2}{n_1} = \frac{d\prime}{d} = \frac{apparent \, depth}{Real \, depth}$$

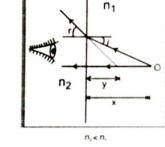


- 1. The above formula is valid only for paraxial rays.
- 2. Distance should be taken from surface.
- 3.  $n_2$  is the reflective index of the medium, where ray is going and  $n_1$  from where ray is coming

10.1 Velocity of the image in case of plane refraction:

$$\frac{n_2}{n_1} = \frac{y}{x} \qquad \implies \qquad y = \frac{n_2}{n_1} \cdot x$$

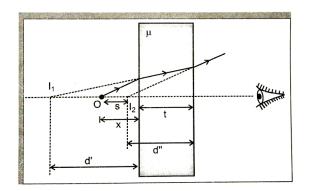
$$\frac{dy}{dt} = \frac{n_2}{n_1} \frac{dx}{dt} \qquad \Longrightarrow \qquad V_{IS} = \frac{n_2}{n_1} V_{OS}$$



## **11. REFRACTION THROUGH A GLASS SLAB**

When a light ray passes through a glass slab having parallel faces, it gets refracted twice before finally emerging out of it.

11.1 Apparent shift due to slab when object is seen normally through the slab

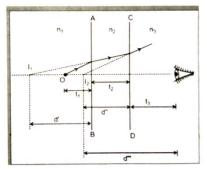


$$S = t \left[ 1 - \frac{\mu_{surrounding}}{\mu_{slab}} \right]$$

## Important points

- 1. Rays should be paraxial
- 2. Medium on both side of the slab should be same.
- 3. Shift coms out from the object
- 4. Shift is independent of the distance of the object form the slab.
- 5. If shift comes out +ve then shift is towards the direction of incident rays and vice versa.

## **11.2** Apparent distance between object and observer when both are in different medium.



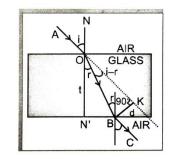
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$$d^{\prime\prime\prime} = n_3 \left[ \frac{t_1}{n_1} + \frac{t_2}{n_2} + \frac{t_3}{n_3} \right]$$

If object and observer are in same medium then shift formula should be used and if both are in different medium then the above formula of apparent distance should be used.

## **11.3 LATERAL SHIFT**

$$d\frac{t}{cosr}\sin(i-r)$$



## **12. CRITICAL ANGLE AND TOTAL INTERNAL REFLECTION**

Critical angle is the angle mad in denser medium for which the angle of refraction. In rarer medium is 90°. When angle in denser medium is more then critical is 90°.

When angle in denser medium is more then critical angle the light ray reflects back in denser medium following the laws of reflection and the interface behaves like a perfectly reflecting mirror. In the figure.

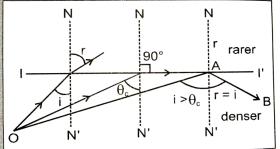
$$\therefore \qquad \theta_c = \sin^{-1} \frac{n_r}{n_d}$$

## 12.1 Conditions of T.I.R.:

(a) light is incident on the interface from denser medium.

(b) Angle of incidence should be greater than the critical angle (i > c).





## 13. PRISM

- (a) PQ and PR are refracting surfaces.
- (b) ∠QPR = A is called refracting angle or the angle of prism (also called Apex angle.)
- (c)  $\delta = angle of deviation$
- (d) For refraction of a monochromatic(single wave length) ray of light through a prism;

$$\delta = (i+e) - (r_1 + r_2)$$

And 
$$r_1 + r_2 = A$$

$$\delta = i + e - A.$$

## Note

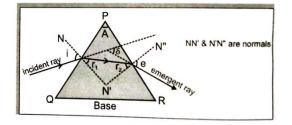
- I. If ray crosses two surface which are inclined to each other then we use the concept of prism.
- **II.** If ray crosses two plain parallel surfaces then we use concept of slab.

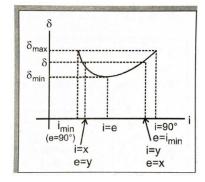
## **13.1** Graph between $\angle \delta$ and $\angle i$

(1) Variation of  $\delta$  versus I

For one  $\delta$  (except  $\delta$  min) there are two values of angle of incidence. If I and e are interchanged then we get the same value of  $\delta$ because of reversibility principle of light.

- (2) There is one and only one angle of incidence for which the angle of deviation is minimum.
- (3) Right hand side part of the graph is more tilted then the left hand side.





## 13.2 Minimum Deviation and Condition for Minimum Deviation:

The condition for minimum deviation is I = e and  $r_1 = r_2$  .... (19)

## 13.3 Relation Between Refractive index and the angle of Minimum Deviation

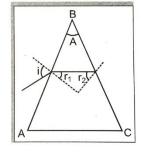
If surrounding medium has refractive index =  $n_s$ 

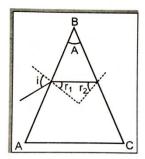
then  $\frac{n_p}{n_s} = \frac{sin(\frac{A+\delta_m}{2})}{sin\frac{A}{2}}$ 

## 13.4 Condition for Prism:

(a) Relative between prism angle A & critical angle C such that ray will always show T I R at BC:

For this 
$$(r_2)_{min} > C$$
 ..... (i)  
For  $(r_2)_{min}$ ,  $r_1$  should be maximum and  
for  $(r_2)_{max} \implies i_{max} = 90^{\circ}$   
 $(r_1)_{max} = C$   
 $(r_2)_{max} = A - C$   
Now from eq. (i)  $A - C > C$   
 $A > 2C$   
i.e.  $A > 2C$ , all rays are reflected back from the second surface.





(b) The relation A & C such that ray will always cross surface BC.

For this  $(r_2)_{max} < C$   $(A - r_1)_{max} < C$   $A - (r_1)_{min} < C$   $(r_1)_{min} = 0$  when  $i_{min} = 0$ From eq. (2) A - 0 < CA < C

i.e. If  $A \le C$ , no rays are reflected back from the second surface i.e. all rays are refracted from second surface.

Rankers JEE | Rankers JEE Advanced | Rankers NTSE and Foundation |Rankers Offline Coaching |Rankers Consulting Services YouTube – Rankers JEE (c) If 2C ≥ A > C, some rays are reflected back from the second surface and some rays are refracted from second surface, depending on the angle of incidence. δ is maximum for two values of i ⇒ i<sub>min</sub>(corresponding to e = 90°) and I = 90° (corresponding to e<sub>min</sub>). For i<sub>min</sub>: n<sub>s</sub> sin i<sub>min</sub> = n<sub>p</sub> sin (A – C) If i < i<sub>min</sub> then T.I.R. takes place at second refracting surface PR.

## **13.5** Dispersive power

**Dispersive power** ( $\omega$ ) of the medium of the material of prism is given by:

$$\omega = \frac{n_v - n_r}{n_y - 1}$$

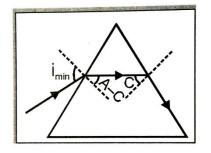
Dispersion without average deviation and average deviation without dispersion

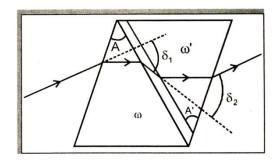
Dispersion without average deviation

$$(\mu_y - 1)A = (\mu'_y - 1)A'$$
$$\delta_V - \delta_r = (\mu_y - 1)A(\omega - \omega')$$

Average Deviation without Dispersion.

$$\frac{(\mu_{y}-1)A'}{(\mu_{y}-1)A} = \frac{\omega}{\omega'}$$
$$\delta = (\mu_{y}-1)A\left(1 - \frac{\omega}{\omega'}\right)$$



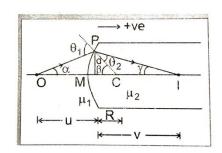


## **14. REFRACTION FROM A SPHERICAL SURFACE**

 $\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$ 

Important point for above formula

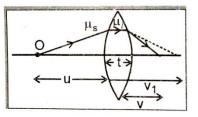
- Above formula is valid only for paraxial ray.
- V,v,R should be put along with sign
- $\mu_2$  is r.i. of medium in which rays is going and  $\mu_1$ sit he r.i. of medium from which rays are coming.



## **15. REFRACTION THROUGH THIN LENSES**

## 15.1 Lens Maker formula

1	$\frac{1}{-} =$	$\left(\frac{\mu_l}{\mu_s}-\right)$	1)	1	_ 1]
v	u _	$\setminus \mu_s$	<u>・</u> ノ	$R_1$	$R_2$

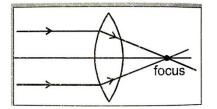


## Important points for the above formula:

- (1) Rays should be paraxial
- (2) V, u,  $R_1$  and  $R_2$  should be put with the sign.
- (3)  $R_1$  is the radius of curvature of the surface on which the ray strikes first.
- (4) Lens should be thin.
- (5) Medium on both sides of the lens should be same.

## **15.2 Focus**

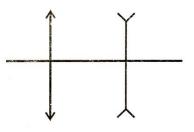
$$\frac{1}{f} = \left(\frac{\mu_{\iota}}{\mu_{s}} - 1\right) \left[\frac{1}{R_{1}} - \frac{1}{R_{2}}\right]$$



Substituting in the lens maker formula:

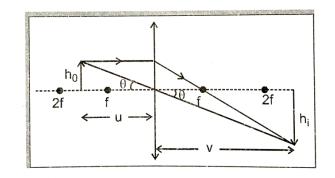
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$
 (lens formula)

> Focal length of lens depends on surrounding medium.

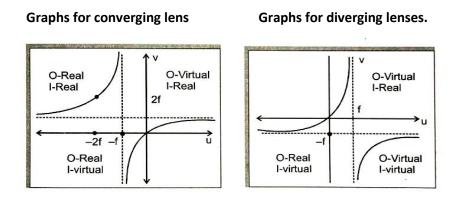


> If f = +ve implies converging and if f = -ve implies diverging lens.

## 15.3 Transverse Magnification



$$\mathsf{m} = \frac{h_i}{h_0} = \frac{v}{u}$$

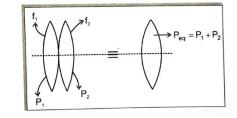


15.4 Velocity of the image formed by a lens

$$v_{IL} = \frac{v^2}{u^2} v_{OL}$$

## 15.5 Combination of Lens

$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2}$$



## Important points:

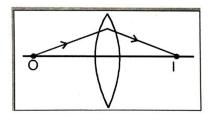
- (1) Rays should be paraxial
- (2) Lens should be kept in contact
- (3) Lenses should be kept in contact
- (4)  $f_1, f_2, f_3, \dots$  should be put with sign.
- (5)  $f_1, f_2, f_3, \dots$  are the focal length of lenses in the surrounding medium.
- (6) If  $f_{eq}$  = +ve then system will behaves as converging system.
  - If  $f_{eq} = -$  ve then system will behaves as diverging system.

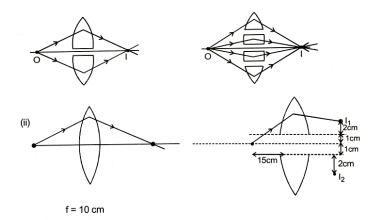
## 16. CUTTING OF LENS.

## 16.1 Parallel Cutting

No. of images in all the cases =1

∴ Principle axis does not shift





## 16.2 Power of lens.

Power = 
$$\frac{1}{f}(diopter)$$

Where  $f \rightarrow meter$  and

f should be put with sign.

Power of converging lens = +ve

Power of diverging lens = -ve

## 16.3 Power of Mirror

Power = 
$$\frac{1}{f}(diopter)$$

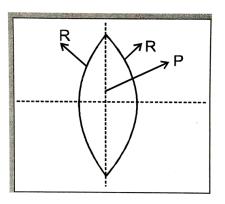
Where  $f \rightarrow meter$  and f

f should be put with sign.

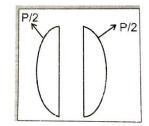
Power of converging mirror = +ve

Power of diverging mirror = -ve

## 16.4 Perpendicular cutting

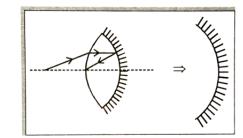


 $\frac{1}{f} = (\mu - 1)\left(\frac{1}{R} - \frac{1}{R}\right) \Rightarrow \frac{1}{f} = (\mu - 1)(\mu - 1)\frac{2}{R}$  $\frac{1}{f} = (\mu - 1)\left(\frac{1}{R} - 0\right) = \frac{(\mu - 1)}{R}$ 

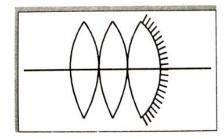


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## **17. SILVERGING OF LENS.**



$$\boldsymbol{P}_{eq} = 2\boldsymbol{P}_{\iota} + \boldsymbol{P}_{m} \implies -\frac{1}{f_{eq}} = \frac{1}{f_{\iota}} - \frac{1}{f_{m}}$$



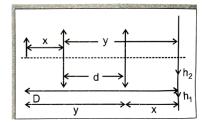
$$\implies \quad \frac{1}{f_{eq}} = \frac{1}{f_m} - \frac{2}{f_\iota} \qquad \quad \frac{1}{f_{eq}} = \frac{1}{f_m} - 2\left[\frac{1}{f_{eq1}}\right]$$

#### Important points:

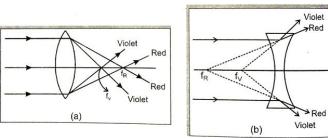
- 1. Rays should be paraxial
- 2. Lenses should be thin
- 3. All the lenses should be in contact.
- 4.  $f_{\iota}$ , f<sub>m</sub> should be put along with the sign.
- 5. If  $f_{eq} = -ve \Longrightarrow concave$   $f_{eq} = +ve \Longrightarrow convex$ ,
  - If  $f_{eq} = \infty \implies$  plane mirror

#### **18. Displacement Method**

$$h_0 = \sqrt{h_1 h_2}$$
$$h = \frac{D^2 - d^2}{4D}$$



#### **19. Chromatic Aberration and Achromatism**



**Condition for Achromatism** 

 $\frac{\omega_1}{f_1} + \frac{\omega_2}{f_2} = \mathbf{0}$ 



## JEE FORMULA NOTES

### **DEPTH Notes with Revision**

# PHYSICS

#### WAVE OPTICS

#### 1. WAVE FRONT

- Wave front is a locus of particles having same phase.
- Direction of propagation of wave is perpendicular to wave front.
- Every particle of a wave front act as a new source & is known as secondary wavelet.

#### **Coherent source**

If the phase difference due to two source at a particular point remains constant with time, then the two sources are considered as coherent source.

#### 2. INTERFERENCE:

$$\Rightarrow A_{net}^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \emptyset$$
  

$$\therefore I_{net} = I_1 + I_2 + 2\sqrt{I_1I_2} \cos \phi \quad (as \ I \propto A^2)$$
  
For  $I_{net}$  to be maximum  
 $\cos \phi = 1 \Rightarrow \phi = 2n\pi$   
Where  $n = \{0, 1, 2, 3, 4, 5 \dots ...\}$   
 $\frac{2\pi}{\lambda} \Delta x = 2n\pi \Rightarrow \Delta x = n\lambda$   
For constructive interference  
 $I_{net} = (\sqrt{I_1} + \sqrt{I_2})^2$   
When  $I_1 = I_1 = I$   
 $I_{net} = 4I$   
 $I_{net} = A_1 + A_2$ 

For  $I_{net}$  to be minimum,  $\cos\Delta\phi = -1$   $\Delta\phi = (2n+1)\pi$  where n = {0,1,2,3,4,5....}  $\frac{2\pi}{\lambda}\Delta x = (2n+1)\pi \Rightarrow \Delta x = (2n+1)\frac{\lambda}{2}$ 

For destructive interfence

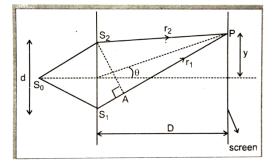
$$I_{net} = \left(\sqrt{I_1} - \sqrt{I_2}\right)^2$$

If 
$$I_1 = I_2$$
  $I_{net} = 0$   $A_{net} = A_1 - A_2$ 

3. YOUNG'S DOUBLE SLIT EXPTERIMENT (Y.D.S.E.) :

Path difference  $\Delta p = S_1 P - S_2 P$ 

$$= \sqrt{\left(y + \frac{d}{2}\right)^{2} + D^{2}}$$
$$-\sqrt{\left(y - \frac{d}{2}\right)^{2} + D^{2}} \qquad \dots \dots (1)$$



#### Approximation I :

For D>>d, we can approximate rays  $\hat{r_1}$  and  $\hat{r_2}$  as being approximately parallel, at angle  $\theta$  to the principle axis. Now,  $S_1P - S_2P = S_1A = S_1S_2sin\theta$  $\Rightarrow$  path difference = d sin  $\theta$  .....(2)

#### **Approximation II :**

Further if  $\theta$  is small, i.e., Y<<D, sin  $\theta \simeq \tan \theta = \frac{y}{D}$ 

and hence, path difference 
$$=\frac{dy}{D}$$
 ..... (3)

for maxima

$$\Delta p = \frac{d.y}{D} = n\lambda$$

for minima

$$\Delta p = \pm \frac{\lambda}{2}$$
,  $\pm \frac{3\lambda}{2} \pm \frac{5\lambda}{2}$ 

4. FRINGE WIDTH :

$$\beta = \frac{\lambda D}{d}$$

**Note** : As vertical distance y is related to  $\theta = \frac{y}{D}$  so  $\Delta \theta = \frac{\Delta y}{D}$  which is referred as angular fringe width  $B_{\theta} = \frac{\beta}{D} = \frac{\lambda}{d}$ 

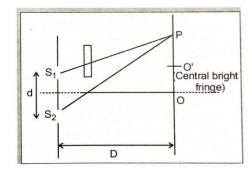
#### 5. ON INTRODUCTION FO A GLASS SLAB IN THE PATH OF THE LIGHT COMING OUT OF THE SLITS -

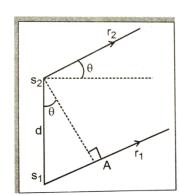
for central bright fringe;

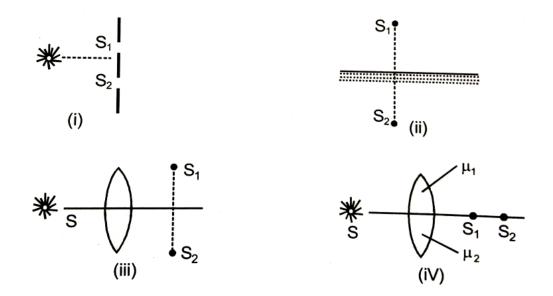
 $\Delta p = 0$ 

$$\Rightarrow \quad \frac{yd}{D} = t(\mu - 1)$$

A single source is split in two coherent sources to obtain Sustained interference in light. This can be done in following different ways.









## JEE FORMULA NOTES

### **DEPTH Notes with Revision**

# PHYSICS

#### **ALTERNATING CURRNT**

#### 1. Summary

AC source connected with	ф		Z	Phasor Diagram
Pure Resistor	0	V <sub>R</sub> is in same phase with i <sub>R</sub>	R	$\rightarrow V_m$
Pure Inductor	π/2	$V_L$ leads $i_L$	ΧĻ	V <sub>m</sub> ↑ J <sub>m</sub>
Pure Capacitor	π/2	$V_{C}$ leads i <sub>C</sub>	x <sub>c</sub>	$\downarrow$

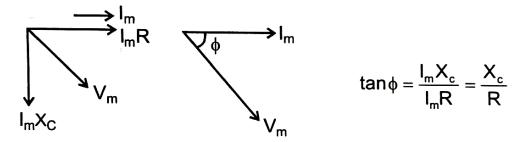
2. RC series circuit with an ac source:

Let 
$$i = I_m \sin(\omega t + \emptyset)$$
  
 $\Rightarrow V_R = iR = I_m R \sin(\omega t + \emptyset)$   
 $V_c = I_m X_c \sin(\omega t + \emptyset - \frac{\pi}{2}) \Rightarrow V_s = V_R + V_c$   
or  $V_m \sin(\omega t + \emptyset) = I_m R (\omega t + \varphi) + I_m X_c (\omega t + \varphi - \frac{\pi}{2})$   
 $V_m = \sqrt{(I_m R)^2 + (I_m X_c)^2 + 2(I_m R)(I_m X_c) \cos\frac{\pi}{2}}$ 

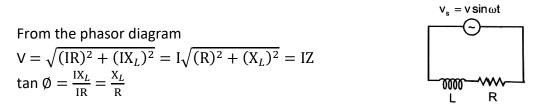
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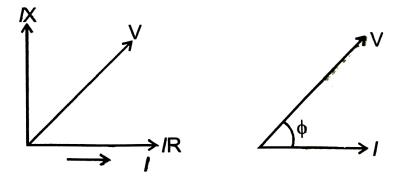
Or 
$$I_m = -\frac{V_m}{\sqrt{R^2 + X_c^2}} \Longrightarrow Z = \sqrt{R^2 + X_c^2}$$

Using phasor diagram also we can find the above result.



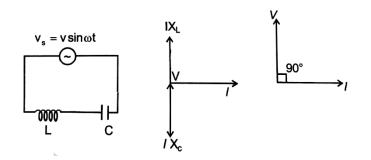
#### 3. LR SERIES CIRCUIT WITH AN AC SOURCE





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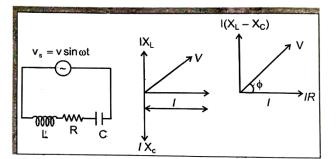
#### 4. LC SERIES CIRCUIT WITH AN AC SOURCE



From the phasor diagram

$$V = I|(X_L - X_C)| = IZ \qquad \phi = 90^{\circ}$$

#### 5. RLC SERIES CIRCUIT WITH AN AC SOURCE



From the phasor diagram

$$V = \sqrt{(IR)^2 + (IX_L - IX_C)^2} = I\sqrt{(R)^2 + (X_L - X_C)^2} = IZ$$

$$\mathbf{Z} = \sqrt{(\mathbf{R})^2 + (\mathbf{X}_L - \mathbf{X}_C)^2}$$

$$\tan \varphi = \frac{I(X_L - X_C)}{IR} = \frac{(X_L - X_C)}{R}$$

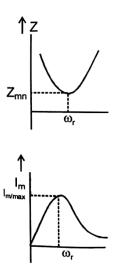
#### 6. **RESONANCE**

Amplitude of current (and therefore  $I_{rms}$  also) in an RLC series circuit is maximum for a given value of  $V_m$  and R, if the impedance of the circuit is minimum, which will be when  $X_L - X_C = 0$ . This condition is called resonance. So at resonance:

$$X_L - X_C = 0$$

or 
$$\omega L = \frac{1}{\omega C}$$

or  $\omega = \frac{1}{\sqrt{\text{LC}}}$ 





## JEE FORMULA NOTES

### **DEPTH Notes with Revision**

# PHYSICS

#### CAPACITANCE

#### 1. CAPACITOR

q∝

$$V$$
 For  $q = CV$ 

$$V = 1, q = C$$

The SI unit is Farad. The practical unit is  $\mu F$  (Micro Farad)

1 Farad = 
$$\frac{1 \text{ Coulomb}}{1 \text{ volt}} = 1 \text{ CV}^{-1}$$

2. Capacitance of an Isolated Sphere

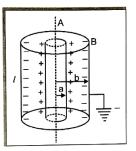
$$C = \frac{q}{v} = 4\pi\varepsilon_0 r$$

3. Calculation of Capacitance

$$\therefore \qquad \mathbf{C} = \frac{q}{V_{ab}} = \frac{q}{-\int_b^a \vec{E}.\vec{d}\vec{r}}$$

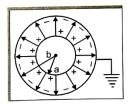
4. Cylindrical Capacitor

$$C = \frac{q}{V} = \frac{2\pi\varepsilon_0 l}{\left(\ln\frac{b}{a}\right)}$$



5. Spherical capacitor

$$C = \frac{Q}{V} = \frac{4\pi\varepsilon_0 ab}{b-a}$$



- **6.** Parallel Plate Capacitor :  $C = \frac{\varepsilon_0 A}{d}$
- 7. Energy Stored in a Charged Capacitor

$$U = \frac{q^2}{2C}$$
  
Putting, q= CV,  $U = \frac{1}{2}CV^2$ 

Putting , C=
$$\frac{q}{V}$$
, U =  $\frac{1}{2}qV$ 

#### 8. Heat Generated:

- (1) Work done by battery
  - W = QV Q = charge flow the battery V = EMF of battery
- (2) W = +Ve (When Battery discharging)W = -Ve (When Battery charging)
- (3) : Q = CV (C = equivalent capacitance)So  $W = CV \times V = CV^2$

Now energy on the capacitor =  $\frac{1}{2}$  CV<sup>2</sup>

: Energy dissipated in form of heat (due to resistance)

Heat = Work done by battery – {final energy of capacitor – initial energy of capacitor}

#### 9. Distribution of Charges on connecting two charged capacitors:

(a) Common potential :

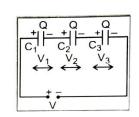
$$V = \frac{Q_1 + Q_2}{C_1 + C_2} = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{\text{Total charge}}{\text{Total capacitance}} v$$

(b) Heat loss during redistribution:

$$\Delta H = U_i - U_f = \frac{1}{2} \frac{C_1 C_2}{C_1 + C_2} (V_1 - V_2)^2$$

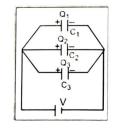
#### **10.** Capacitors in Series

 $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$ 



**11.** Capacitors in Parallel

 $C = C_1 + C_2 + C_3$ 



#### 12. R- C CIRCUIT

#### Note:

•

At time t = 0 (initial state) capacitor will behave as a short circuit wire.

At time t =  $\infty$  (Final state or Steady state) capacitor will behave as a open circuit wire.

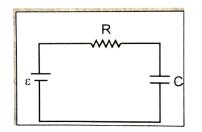
#### 12.1 Charging of a condenser :

$$q = q_0 \left[ 1 - e^{(t/RC)} \right]$$

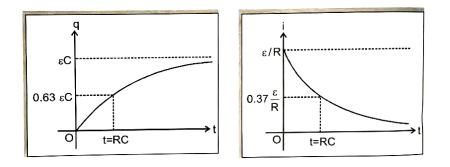
Where  $q_0 = maximum$  final value fo charge at  $t = \infty$ 

If 
$$t = RC = \tau$$
 then  
 $q = q_0 \left[ 1 - e^{(t/RC)} \right] = q_0 \left[ 1 - \frac{1}{e} \right]$   
or  $q = q_0 (1 - 0.37) = 0.63 q_0$ 

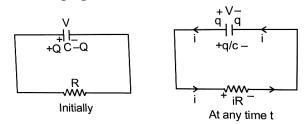
$$q = q_0(1 - 0.37) = 0.6$$
  
= 63% of q<sub>0</sub>



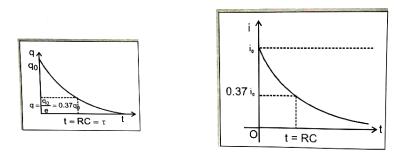
- Time t = RC is known as time constant.
- The potential difference across the condenser at any instant of time is given by  $V = V_0 \big[ 1 e^{(t/RC)} \big] \text{volt} \qquad I = I_0 \big[ e^{-(t/RC)} \big] \text{ampere}$



#### **12.2** Discharging of a condenser :



The quantity of charge on the condenser at any instant of time t is given by  $q = q_0 e^{-(t/RC)}$ i.e. the charge falls exponentially.  $i = -\frac{dq}{dt} = \frac{Q}{RC} e^{-t/RC}$ 

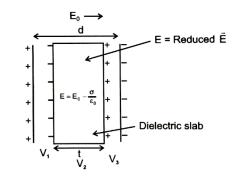




 $C = \frac{q}{v}$ 

$$=\frac{q}{\varepsilon_0 A \left(d-t+\frac{t}{K_D}\right)}$$

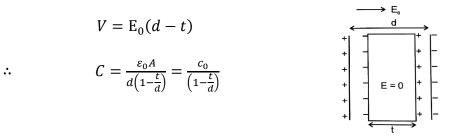
$$=\frac{\varepsilon_0 A}{d-t+\frac{t}{K_D}}$$



Capacitance of parallel plate capacitor

with dielectric slab between plates

14. Capacitance of a Parallel Plate Capacitor with Conducting Slab between Plates



15. Introduction of a Dielectric slab of dielectric constant K between the plates

#### (a) When the battery is disconnected

- (i) Charge remain constant , i.e.,  $q = q_0$ , as in an isolated system charge is conserved.
- (ii) Capacity increases, i.e.,  $C = KC_0$ , as by the presence of a dielectric capacity becomes K times.
- (iii) Potential difference between the plates decreases, i.e.,  $V = \left(\frac{V_0}{\kappa}\right)$ , as

$$V = \frac{q}{c} = \frac{q_0}{KC_0} = \frac{V_0}{K} [:: q = q_0 \text{ and } C = KC_0]$$

(iv) Field between the plates decreases,

$$i.e., \mathrm{E} = \frac{E_0}{K}$$
, as

$$\mathbf{E} = \frac{V}{d} = \frac{V_0}{Kd} = \frac{E_0}{K} \left[ \text{as } \mathbf{V} = \frac{V_0}{K} \right] \text{ and } \mathbf{E}_0 = \frac{V_0}{d}$$

(v) Energy stored in the capacitor decreases i.e.

$$U = \left(\frac{U_0}{K}\right), \text{ as}$$
$$U = \frac{q^2}{2C} = \frac{q_0^2}{2KC_0} = \frac{U_0}{K} \quad (\text{as } q = q_0 \text{ and } C = KC_0)$$

#### (b) When the battery remains connected (potential is held constant)

- (i) Potential difference remains constant, i.e.,  $V = V_0$ , as battery is a source of constant potential difference.
- (ii) Capacity increases, i.e.,  $C = KC_0$ , as by presence of a dielectric capacity becomes K times.
- (iii) Charge on capacitor increases, i.e.,  $q = Kq_0$ , as

$$q = CV = (KC_0)V = Kq_0[: \quad q_0 = C_0V]$$

(iv) Electric field remains unchanged, i.e.,  $E = E_0$ , as  $E = \frac{V}{d} = \frac{V_0}{d} = E_0$ 

$$\left[\text{as } V = V_0 \text{ and } \frac{V_0}{d} = E_0\right]$$

(v) Energy stored in the capacitor increases, i.e.,

U = KU<sub>0</sub>, as  
U = 
$$\frac{1}{2}$$
cv<sup>2</sup> =  $\frac{1}{2}$ (KC<sub>0</sub>)(V<sub>0</sub>)<sup>2</sup> = KU<sub>0</sub>  
[as C = KC<sub>0</sub> and U<sub>0</sub> =  $\frac{1}{2}$ C<sub>0</sub>V<sub>0</sub><sup>2</sup>]



## JEE FORMULA NOTES

### **DEPTH Notes with Revision**

# PHYSICS

#### **CURRENT ELECTRICITY**

#### 1. ELECTRIC CURRENT

$$I = \lim_{\Delta t \to 0} \frac{\Delta q}{\Delta t} = \frac{dq}{dt}$$

#### 2. ELECTRIC CURRENT IN A CONDUCTOR

 $I = nAev_d$ 

$$\mathbf{v}_d = \frac{\lambda}{\tau}$$

$$\mathbf{v}_d = \frac{\frac{1}{2} \left(\frac{eE}{m}\right) \tau^2}{\tau} = \frac{1}{2} \frac{eE}{m} \tau$$

$v_d = drift velocity$	E = electric field
e = electronic charge	m = mass of electron
au = relaxation time	$\lambda =$ mean free path.

#### 3. CURRENT DENSITY

$$\vec{J} = \frac{di}{ds}\vec{n} \qquad \qquad \int di = \int \vec{J}.\,d\vec{s}$$

So,  $di = \vec{j} \cdot d\vec{s}$ 

#### 4. ELECTRICAL RESISTANCE

$$i = neAv_d = neA\left(\frac{eE}{2m}\right)\tau = \left(\frac{ne^2\tau}{2m}\right)AE$$
$$i = \left(\frac{ne^2\tau}{2m}\right)\left(\frac{A}{\iota}\right)V = \left(\frac{A}{\rho\iota}\right)V = \frac{V}{R} \implies V = IR$$
$$V = I \times \frac{\rho\iota}{A}$$

$$E = \frac{V}{\iota} = \frac{l\rho}{A} \implies E = Jp \ J = current density$$

 $\rho = \frac{2m}{ne^2\tau} = \frac{1}{\sigma}, \sigma$  is called conductivity

#### 5. DEPENDENCE OF RESISTANCE ON VARIOUS FACTORS

$$\mathbf{R} = \frac{\rho\iota}{A} = \frac{2m}{ne^2\tau} \cdot \frac{\iota}{A}$$

#### Various cases

(a) On stretching wire (volume constant)

If length of wire is changed then  $\frac{R_1}{R_2} = \frac{\iota_1^2}{\iota_2^2}$ 

- (b) If radius of cross section is changed then  $\frac{R_1}{R_2} = \frac{\iota_2^4}{\iota_1^4}$ , where  $R_1$  and  $R_2$  are initial and final resistance and  $\iota_1$ ,  $\iota_2$  are initial and final lengths. And  $r_1$  and  $r_2$  are the initial and final radii respectively.
- (c) Effect of percentage change in length of wire

$$\frac{R_1}{R_2} = \frac{\iota^2 \left[1 + \frac{x}{100}\right]^2}{\iota^2}$$

Where  $\iota$  is original length and x is % increment If x is quite small (say < 5%) then % change in R is

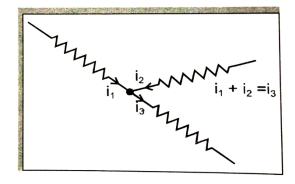
$$\frac{R_2 - R_1}{R_1} \times 100 = \left\{ \left(1 + \frac{x}{100}\right)^2 - 1 \right\} \times 100 = 2x\%$$

#### 6. TEMPERATURE DEPENDDENCE OF RESISTIVITY AND RESISTANCE

$$\begin{split} \rho(T) &= \rho_0 [1 + \alpha (T - T_0)] \\ R(T) &= R_0 [1 + \alpha (T - T_0)] \\ \text{The } \rho - T \text{ equation written above can be derived from the relation } \rho &= \rho_0 e^{\alpha (T - T_0)} \end{split}$$

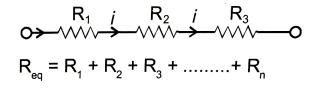
#### 7. KIRCHHOFF'S CURRENT LAWS

- (a) The sum of the currents that flow into a junction is equal to the sum of the currents that flow out of the junction.
- (b) The sum of the emf's around a loop is equal to the sum of the IR potential drops around the loops.
  In writing ∑ IR = 0, then current into a node (or junction) is taken to be positive. In applying Kirchhoff's voltage law (∑E = ∑IR), if there are more than one source when the direction do not agree, the voltage of source is taken as positive, if it is in the direction of assumed current.



#### 8. **RESISTANCE IN SERIES**

When the resistance (or any type of elements) are connected end to end then they are said to be in series. The current through each element is same.



#### 9. RESISTANCE IN PARALLEL

A parallel circuit of resistor is one in which the same voltage is applied across all the components, in a parallel grouping of resistors  $R_1$ ,  $R_2$ ,  $R_3$ 

$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3} \qquad \qquad \frac{V}{R_{eq}} = \frac{1}{R_1} + \frac{2}{R_2} + \frac{3}{R_3}$$

Note :

#### In parallel combination

(a) Potential difference across each resistor is same

**(b)** 
$$I = I_1 + I_2 + I_3 + \dots + I_n$$

(c) Effective resistance (R) then

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots \frac{1}{R_n}.$$

( $R_{eq}$  is less than each resistor)

(d) Current in different resistors is inversely proportional to the resistance.

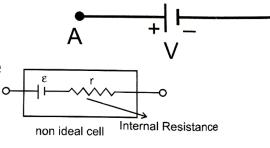
$$\begin{split} I_1: I_2: & \dots : I_n = \frac{1}{R_1}: \frac{1}{R_2}: \frac{1}{R_3}: \dots : \frac{1}{R_n} \\ I_1 = \frac{G_1}{G_1 + G_2 + \dots + G_n} \ \text{I}, I_2 = \frac{G_2}{G_1 + G_2 + \dots + G_n} \ \text{I}, \text{etc} \\ \text{Where } G = \frac{1}{R} = \text{conductance of a resistor, [Its unit is } \Omega^{-1}] \end{split}$$

#### **10. ELECTROMOTIVE FORCE (E.M.F.) AND POTENTIAL DIFFERENCE ACROSS A BATTERY.**

#### (a) Representation for battery

Ideal cell: Cell in which there is no heating effect.

**Non ideal cell:** Cell in which there is heating effect inside due to opposition to the current flow internally.

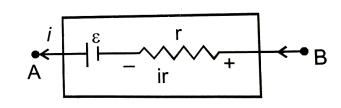


#### (b) Battery acting as a source (or battery is discharging)

 $V_A - V_B = \varepsilon - ir$ 

 $V_A - V_B \Rightarrow$  it is also called terminal voltage

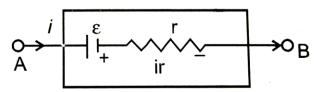
The rate at which the chemical energy of the cell is consumed =  $\varepsilon i$ The rate of which heat is generated inside the battery or cell =  $i^2r$ Electric power output =  $\varepsilon i - i^2r = (\varepsilon - ir)i$ 



B

#### (c) Battery acting as a load (or battery charging )

 $V_A - V_B = \varepsilon + ir$ The rate at which chemical energy stored in the cell=  $\varepsilon$ thermal power generated inside the cell=  $i^2r$  electric power input =  $\varepsilon i + i^2r = (\varepsilon + ir)i$ =  $(V_A - V_B)i$ 



(d) Electromotive force of a cell is equal to potential difference between its terminals when no current is passing through the circuit.

When cell in open circuit

u = i = 0 as resistance of open circuit is infinite ( $\infty$ )

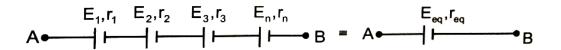
So,

 $V = \varepsilon$ , so open circuit terminal potential difference is equal to emf of the cell.

(e) Short circuiting: Two points, in an electric circuit directly connected by a conducting wire are called short circuited, under such condition both points are at same potential.

#### **11. GROUPING OF CELLS**

(a) Cells in series



Equivalent EMF

$$\mathbf{E}_{eq} = \mathbf{E}_1 + \mathbf{E}_2 + \dots + \mathbf{E}_n$$

[write EMF's with polarity]

Equivalent internal resistance

$$r_{eq} = r_1 + r_2 + r_3 + r_4 + \dots + r_n$$

In n cells each of emf E are arranged in series and if r is internal resistance of each cell, then total emf = Ne

So current in the circuit I =  $\frac{nE}{R+nr}$ 

If nr  $\ll$  R then I =  $\frac{nE}{R} \rightarrow$  Series combination is advantageous If nr  $\ll$  R then I =  $\frac{E}{r} \rightarrow$  Series combination is not advantageous

#### (b) Cells in parallel

$$E_{eq} = \frac{\varepsilon_1 / r_1 + \varepsilon_2 / r_2 + \dots + \varepsilon_n / r_n}{1 / r_1 + 1 / r_2 + \dots + 1 / r_n}$$
$$\frac{1}{r_{eq}} = \frac{1}{r_1} + \frac{1}{r_2} + \dots + \frac{1}{r_n}$$

If m cells each of emf E and internal resistance r be connected in parallel and if this combination is connected to an external resistance then the emf of the circuit = E.

Internal resistance of the circuit  $=\frac{r}{m}$  and  $I = \frac{E}{R + \frac{r}{m}} = \frac{mE}{mR + r}$ 

If mR<< r; I =  $\frac{mE}{r} \rightarrow$  Parallel combination is advantageous If Mr>> r; I =  $\frac{E}{R} \rightarrow$  Parallel combination is not advantageous

#### (c) Cells is multiple Arc

n = number of rows m = number of cells in each row Current I =  $\frac{mE}{R + \frac{mr}{n}}$ For maximum current nR = mr

#### **12. ELECTRICAL POWER**

$$Power = \frac{V.dq}{dt} = VI \qquad P = I^2 R = VI = \frac{V^2}{R}$$

$$W = VIt = I^2Rt = VI = \frac{V^2}{R}t$$
  $P = I^2Rt$  Joule  $= \frac{I^2Rt}{4.2}$  calorie

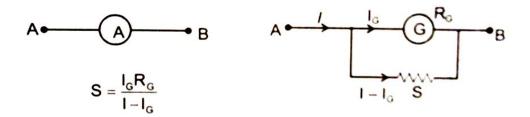
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#### **13. GALVANOMETER**

BINA sin $\theta = C \phi$	
Here I ∝ Ø	
B = magnetic field	A = area of the coil
l = current	C = torsoinal constant
N = number of turns	Ø = angle rotated by coil

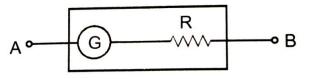
#### **14. AMMETER**

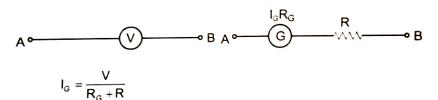
A shunt (small resistance) is connected is parallel with galvanometer to convert it into ammeter.



#### **15. VOLTMETER**

A high resistance is put in series with galvanometer. It is used to measure potential difference across a resistor in a circuit.





#### **16. POTENTIOMETER**

Potential gradient (x)  $\rightarrow$  potential difference per unit length of wire

$$\mathbf{x} = \frac{\mathbf{V}_1 - \mathbf{V}_B}{\mathbf{L}} = \frac{\mathbf{\varepsilon}}{\mathbf{R} + \mathbf{r}} \cdot \frac{\mathbf{R}}{\mathbf{L}}$$

Application of potentiometer

- (a) To find emf of unknown cell and compare emf of two cells
  - $\frac{\varepsilon_1}{\varepsilon_2} = \frac{\iota_1}{\iota_2}$
- (b) To find current if resistance is known

$$I = \frac{x\iota_1}{R_1}$$

(c) To find the internal resistance of a cell

$$r' = \left[ \tfrac{\iota_1 - \iota_2}{\iota_2} \right] R$$

17. METER BRIDGE (USED TO MEASURE UNKNOWN RESISTANCE)

$$x = \frac{100 - \iota}{\iota} R$$



## JEE FORMULA NOTES

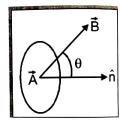
### **DEPTH Notes with Revision**

# PHYSICS

## E.M.I

#### 1. MAGNETIC FLUX

Consider a closed curve enclosing an area A (as shown in the figure). Let there be a uniform magnetic field  $\vec{B}$  in that region. The magnetic flux through the area  $\vec{A}$  is given by  $\phi = \int \vec{B} \cdot d\vec{A} \implies \phi = \vec{B} \cdot \vec{A} = BA \cos \theta$ Unit  $\rightarrow$  weber (Wb).



#### 2. FARADAY'S LAW OF ELECTROMAGNETIC INDUCTION

Whenever the flux of magnetic field through the area bounded by a closed conducting loop. The emf is given by

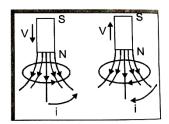
 $\varepsilon = -\frac{d\phi}{dt}$  where  $\phi = \int \vec{B} \cdot d\vec{A}$ 

the flux of magnetic field through the area. If resistance of loop is R then

$$i = \frac{\varepsilon}{R} = -\frac{1}{R}\frac{d\phi}{dt}$$

#### 3. LENZ'S LAW

According to lenz's law of the flux associated with any loop changes than the induced current flows in such a fashion that it tries to oppose the cause which has produced it.



#### 4. Induced emf generates:

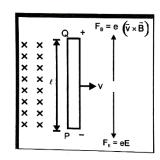
(i) By changing the magnetic field

(ii) By changing the area

(iii) By changing the angle between Area vector & magnetic field.

#### 5. Motional Emf

at equilibrium:-  $|q(\vec{v} \times \vec{B})| = |q\vec{E}|$   $\vec{E} = \vec{v} \times \vec{B}$   $\int dE = -\vec{E} \cdot d\vec{l}$   $E = \int (\vec{v} \times \vec{B}) \cdot d\vec{l}$ So emf developed across the ends of the rod moving  $\perp$  to magnetic field with velocity  $\perp$  to the rod is  $\varepsilon = vBl$ 



6. Induced emf in a rotating rod:

$$\int dE = \int_0^t B\omega x dx$$

$$V_A - V_B = \frac{B\omega l^2}{2}$$

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×	×	×	-! <sub>x</sub> -	×	→×	×
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#### 7. INDUCED ELECTRIC FIELD

This electric field is produced by the changing magnetic field and not by charged particles. The electric produced by the changing magnetic field is nonelectrostatic and nonconservative in nature. We cannot define a potential corresponding to this field. We call it induced electric field. The lines of induced electric field are closed curves. There are no starting and terminating points of the field lines.

If  $\vec{E}$  be the induced electric field, the force on the charge q placed in the field of

 $q\vec{E}$ . The work done per unit charge as the charge moves through  $d\vec{l}$  is E.

 $d\vec{l}$ . The emf developed in the loop is, therefore,

$$\varepsilon = \oint \vec{E} . d\vec{l}$$

Using Faraday's law of induction,

$$\varepsilon = -\frac{d\phi}{dy}$$
  
Or  $\oint \vec{E} \cdot d\vec{l} = -\frac{d\phi}{dt}$  .....(6)

The presence of a conducting loop is not necessary to have an induced electric field. As long as  $\vec{B}$  keeps changing, the induced electric field is present. If a loop is there, the free electrons start drifting and consequently an induced current results.

#### 8. SELF INDUCTION:

If current in the coil changes by  $\Delta I$  in a time interval  $\Delta t$ , the average emf induced in the coil is given as

$$\varepsilon = -\frac{\Delta(N\emptyset)}{\Delta t} = \frac{\Delta(LI)}{\Delta t} = -\frac{L\Delta I}{\Delta t}$$
  
The instantaneous emf is given as  
$$\varepsilon = -\frac{d(N\emptyset)}{dt} = \frac{d(LI)}{dt} = -\frac{LdI}{dt}$$
  
S.I unit of inductance is wb/amp or Henry (H)

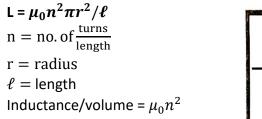
L – self inductance is +ve quantity.

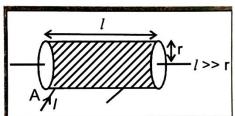
L depends on :

(1) Geometry of loop

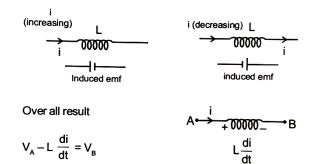
(2) Medium in which it is kept. L does not depend upon current. L is a scaler quantity.

#### 8.1 Self Inductance of solenoid





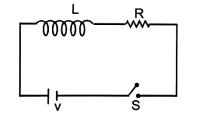
#### 9. INDUCTOR



Energy stored in inductor

#### 10. L – R CIRCUIT

- at t = 0 inductor behaves as open switch.
- at t =  $\infty$  inductor behaves as plane wire.

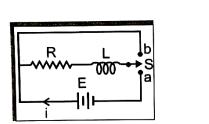


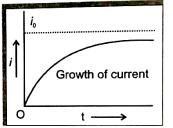
 $U = \frac{1}{2}Li^2$ 

#### **10.1 Growth of Current**

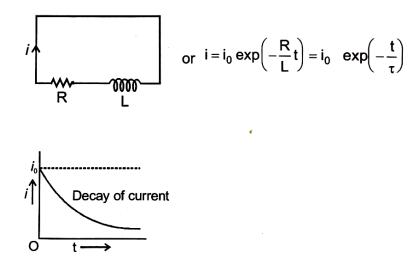
The maximum current in the circuit  $i_0 = \frac{E}{R}$ .

So 
$$i = i_0 \left\{ 1 - \exp\left(-\frac{R}{L}t\right) \right\}$$





10.2 Decay of Current



#### **11. MUTUAL INDUCTANCE**

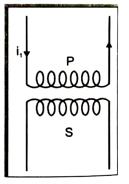
Let the current through the primary coil at any instant be  $i_1$ . Then the magnetic flux  $\phi_2$  in the secondary at any time will

be proportional to  $i_1 i. e.$  ,  $\emptyset_2 \propto i_1$ 

Therefore the induced e.m.f. in secondary

when  $i_1$  changes is given by

$$\varepsilon - \frac{d\phi_2}{dt} i.e., \ \varepsilon \propto -\frac{di_1}{dt}$$
$$\therefore \qquad \varepsilon = -M \frac{di_1}{dt} = -\frac{dMi_1}{dt} \Longrightarrow \phi_2 = M i_1$$



M = Mutal inductance

Unit of Mutual inductance is Henry (H)

#### **12. COMBINATION OF INDUCTORS**

(i) Series combination

 $\mathbf{L}_{eq} = \mathbf{L}_1 + \mathbf{L}_2 + \dots$ 

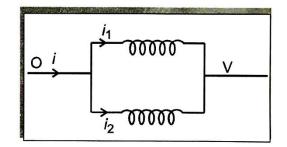
Parallel Combination of Inductor

$$i = i_1 + i_2$$

$$\implies \frac{di}{dt} = \frac{di_1}{dt} + \frac{di_2}{dt}$$

$$\frac{v}{L_{eq}} = \frac{v}{L_1} + \frac{v}{L_2}$$

$$\frac{v}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$$





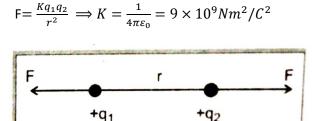
## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

### ELECTROSTATICS

#### 1. COULOMB'S LAW :



This force F acts along the line joining the two charges and is repulsive if  $q_1$  and  $q_2$  are of same sign and is attractive if they are of opposite sign.

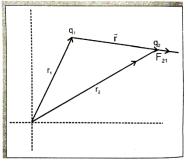
#### 1.1 Vector forms of Coulomb's law

 $(F_{21}: \text{force on } q_2 \text{ due to } q_1)$  $\vec{F}_{21} = \frac{kq_1q_2}{r^2} \hat{r} = \frac{kq_1q_2}{r^3} \vec{r}$  $\vec{F}_{21} = \frac{kq_1q_2}{[\vec{r}_2 - \vec{r}_1]^3} (\vec{r}_2 - \vec{r}_1)$ 

- Head of  $\vec{r}$  points at that position where force has to be calculated
- $\vec{r}_2 \& \vec{r}_1$  depend on origin but  $\vec{r}$  does not.
- $q_1$  and  $q_2$  should be put along with sign.

#### 1.2 Coulomb's law in a medium:

$$\begin{split} F_{med} &= \frac{1}{4\pi\epsilon_0\varepsilon_r} \frac{q_1q_2}{r^2} \\ or & F_{med} &= \frac{F_{air}}{\epsilon_r} \text{ as } \epsilon_r > 1 \qquad \implies F_{med} < F_{air} \end{split}$$



#### 2. ELECTRIC FIELD:

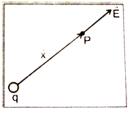
If a charge  $q_0$  placed at a point in electric field, experienced a net force  $\vec{F}$  on it, then electric field strength at that point can be

- or  $E = \frac{\vec{F}}{q_0}$  .....(1)  $[q_0 \rightarrow test \ charge]$
- (a) Electric Field Strength due to Point Charge:

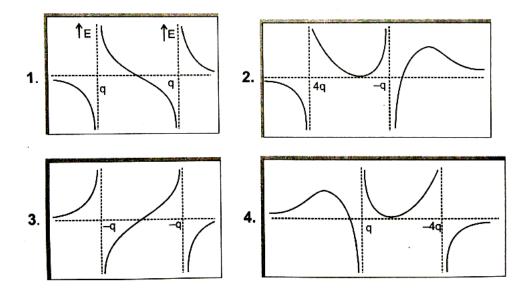
$$E = \frac{Kq}{x^2}$$

(b) Vector Form of Electric field due to Point Charge:

$$\vec{E} = \frac{Kq}{x^3} \cdot \vec{x}$$



#### 2.1 Graph of electric field due to binary charge configuration

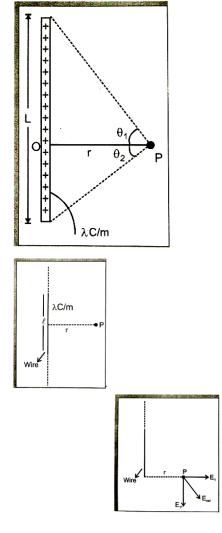


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#### 2.2 Electric field Strength at a General Point due to a Uniformly Charged Rod:

- In ||- direction  $E_x = \frac{KQ}{Lr} (\cos\theta_2 \cos\theta_1)$  $= \frac{k\lambda}{r} (\cos\theta_2 - \cos\theta_1)$ In  $\bot$ - direction  $E_y = \frac{KQ}{Lr} (\sin\theta_1 + \sin\theta_2)$  $= \frac{k\lambda}{r} (\sin\theta_1 + \sin\theta_2)$ 
  - r is the perpendicular distance of the point from the wire
  - $\theta_1$  and  $\theta_2$  should be taken in opposite sense
- **2.3** Electric field due to infinite wire

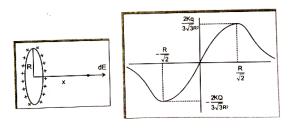
 $(\iota \gg r)$ 



2.4 Electric field due to semi infinite wire

$$E_{net}$$
 at  $P = \frac{\sqrt{2}k\lambda}{r}$ 

2.5 Electric field due to Uniformly Charged Ring:

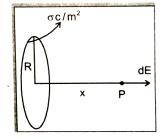


$$E_P = \frac{KQx}{(R^2 + x^2)^{3/2}}$$
 (along the axis)

 $E = \frac{KQ}{x^2}$ 

2.6 Electric field Strength due to a Uniformly Surface Charged Disc:

$$E = \frac{\sigma}{2\varepsilon_0} \left[ 1 - \frac{x}{\sqrt{x^2 + R^2}} \right] [along the axis]$$
  
Case (i) : If x>>R



Case (ii) : If x<<R

$$E = \frac{\sigma}{2\varepsilon_0} [1 - 0] = \frac{\sigma}{2\varepsilon_0}$$

i.e. behavior of the disc is like infinite sheet.

2.7 Electric Field Strength due to a Uniformly charged Hollow Hemispherical Cup:

$$E_0 = rac{\sigma}{4 \, arepsilon_0}$$
 (along the axis)

#### 3. ELECTROSTATIC POTENTIAL ENERGY:

3.1 Interaction Energy of a System of Two Charged Particles:

$$q_1$$
  $r$   $q_2$ 

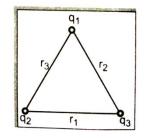
$$W = \frac{\kappa q_1 q_2}{r} = U$$
 [Interaction energy]

If the two charges here are of opposite sign, the potential energy will be negative as As

$$U = -\frac{\kappa q_1 q_2}{r} =$$

**3.2 Potential Energy for a System of charged Particles:** 

$$U = \frac{Kq_1q_2}{r_3} + \frac{Kq_1q_3}{r_2} + \frac{Kq_2q_3}{r_1}$$

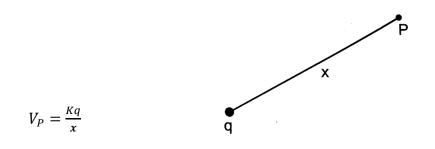


#### 4. ELECTRIC POTENTIAL:

If at a point in electric field charge  $q_0$  has potential energy U, then electric potential at that point can be given as

$$V = \frac{U}{q_0}$$
 joule/coulomb

(a) Electric Potential due to a Point Charge in its Surrounding:



(b) Electric Potential due to a Charge Rod :

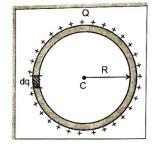
$$V = \frac{KQ}{R} \ln\left(\frac{r+L}{r}\right)$$

·	>	x	→
dx Q <u>++++++</u> ₩ L	++++ >	r	P

(c) Electric Potential due to a Charged Ring :

Case I : At its centre

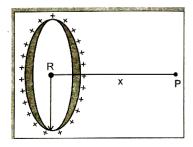
$$V = \frac{KQ}{R}$$

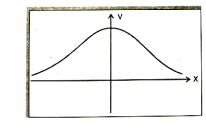


Case II : At a Point on Axis of Ring

$$V_P = \frac{KQ}{\sqrt{R^2 + x^2}}$$

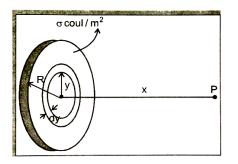
Graph





(d) Electric Potential due to a Uniformly Charged Disc :

$$V_P = \frac{\sigma}{2\varepsilon_0} \left[ \sqrt{x^2 + R^2} - x \right]$$



5. RELATION BETWEEN ELECTRIC FIELD INTENSITY AND ELECTRIC POTENTIAL :

(a) For uniform electric field :

$$V_B - V_A = -\vec{E}.\vec{AB}$$

#### (b) Non uniform electric field

$$E = -\left[\hat{\iota}\frac{\partial}{\partial x} + \hat{j}\frac{\partial}{\partial y} + \hat{k}\frac{\partial}{\partial z}\right]V = -\nabla V = -grad V$$

- Area under E x curve gives negative of change in potential.
- Negative of slope of V x curve gives the electric field at that point.

#### 6. ELECTRIC LINES OF FORCE

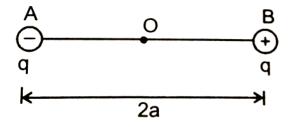
- Electric lines of forces originate from +ve charge or infinite and terminate on -ve charge or infinity
- If density of lines is high then electric field intensity will also high and vice versa.
- Tangent at any point on the electric field line will give u direction of force or electric field that's why these lines are known as electric lines of forces.
- Two electric field lines never cut each other because at the point at intersection there is two position direction of electric field which is not possible.
- Electric field lines does not exist in closed loop because electrostatic force is a conservation force
- No. of lines originating or terminating is directly proportional to the magnitude of charge.

#### 7. EQUIPOTENTIAL SURFACES :

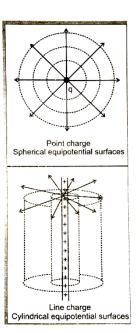
- **1.** Equipotential surface is the locus of points where potential of all the points is same.
- Potential difference between any two points of the same equipotential surface is zero that's why work done by electric field on a charge moving from one point to another point on same equipotential surface is zero.
- **3.** E.f lines is always perpendicular to the equipotential surface.
- **4.** If we take a particle from one equipotential surface to another equipotential surface then there is work done due to electric forces.
- **5.** Electric field lines move from higher equipotential surface to lower equipotential surface.

#### 8. ELEECTRIC DIPOLE

Electric dipole moment  $\vec{P} = q. 2\vec{a}$ , Vector quantity SI unit Cm



9.(a) Electric Field on Axial Line of an Electric Dipole



$$E = \frac{1}{4\pi\varepsilon_0} \frac{2qr}{(r^2 - a^2)^2}$$
  
When  $a \ll r$ ,  $E_{axial} = \frac{1}{4\pi\varepsilon_0} \frac{2p}{r^3}$   
 $E_{axial}$  is along the direction of dipole moment

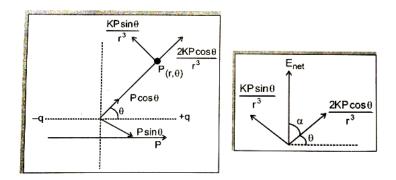
#### 9.(b) Electric Field on Equatorial Line of an Electric Dipole

$$E = \frac{1}{4\pi\varepsilon_0} \frac{q \times 2a}{(r^2 + a^2)^{3/2}} \qquad \text{When } a \ll r. E_{equiatoral} = \frac{1}{4\pi\varepsilon_0} \frac{P}{r^3}$$

 $E_{equiatoral}$  is along the negative direction of dipole moment .

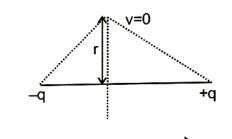
• Remembers, when a is very small, dipole is known as 'point dipoler'.

#### 9.(c) Electric field at a general Point due to a dipole



$$E_{net} = \sqrt{\left(\frac{2KP\cos\theta}{r^3}\right)^2 + \sqrt{\left(\frac{2KP\sin\theta}{r^3}\right)^2} = \frac{kP}{r^3}\sqrt{1+3\cos^2\theta}}$$
$$\tan\alpha = \frac{\tan\theta}{2}$$

- 9.(d) Electric potential due to a dipole.
- 1. At an axial point
  - $V_{net} = \frac{kp}{r^2}$  (As P = 2aq)



p

Pcosθ

Psinθ

α

2. At a point on perpendicular bisector



Potential at P due to dipole =  $\frac{kpcos\theta}{r^2}$ 

-q

#### 10. Dipole in a Uniform External Electric Field

A System of equal and opposite charges separated by a small distance is called a dipole.

(a) In vector form, 
$$\vec{\tau} \times \vec{E}$$
  
(b) $U = -pEcos\theta$  At  $\theta = 0^{\circ}, U = U_{min}$   
At  $\theta = 180^{\circ}, U = U_{max}$ 

$$U = -\vec{p}.\vec{E}$$
  
(C) Dipole Moment,  $p = q \times 2a \ cm$   
 $\vec{p} = q \times 2a \ \hat{p}$ 



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

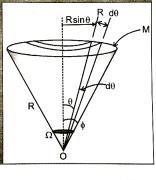
### **ELECTROSTATICS-2**

#### 1. ELECTRIC FLUX

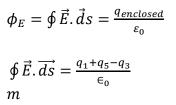
 $Flux = \emptyset = \int \vec{E} \cdot \vec{dA}, \qquad If \vec{E} is cosntant, \emptyset = \vec{E} \cdot \vec{A}$ 

- Basically flux is the count of number of lines of electric field crossing an area.
- For open surface we choose one direction as a area vector & stick to it for the whole problem
- 2. Relation in Half Angle of cone and Solid Angle of Vertex:

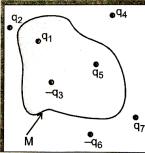
$$\begin{aligned} \Omega &= 2\pi (1 - cos\phi) \\ \Omega &= \text{solid angle } \phi = \text{half angle of cone} \end{aligned}$$







[Gauss's Law]

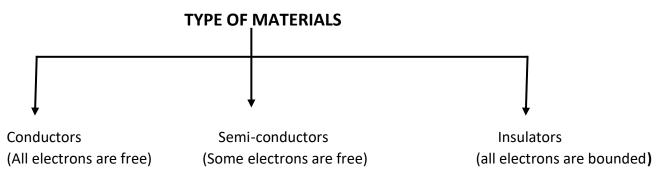


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- (a) Electric field near a thin flat sheet of charge  $E = \frac{\sigma}{2\varepsilon_0}$ , where  $\sigma$  = surface charge density
- (b) Electric field near a conductor of any shape

$$E = \frac{\sigma}{\varepsilon_0}$$

4. CONDUCTOR



(i) Conductors are materials which contains large number of free electrons which can move freely inside the conductor.

(ii) In electrostatics conductors are always equipotential surfaces

(iii) Charge always resides on outer surface of conductor.

(iv) If there is a cavity inside the conductor having no charge then charge will always reside only on outer surface of conductor.

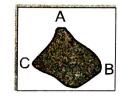
(v) Electric field is always perpendicular to conducting surface.

(vi) Electric lines of force never enter into conductors.

(vii) Electric field intensity near the conducting surface is given by formula

$$\vec{E} = \frac{\sigma}{\varepsilon_0} \hat{n}$$

 $\sigma$  is the local charge density.



$$\overrightarrow{E_A} = \frac{\sigma_A}{\varepsilon_0} \hat{n} \text{ and } \overrightarrow{E_c} = \frac{\sigma_c}{\varepsilon_0} \hat{n}$$

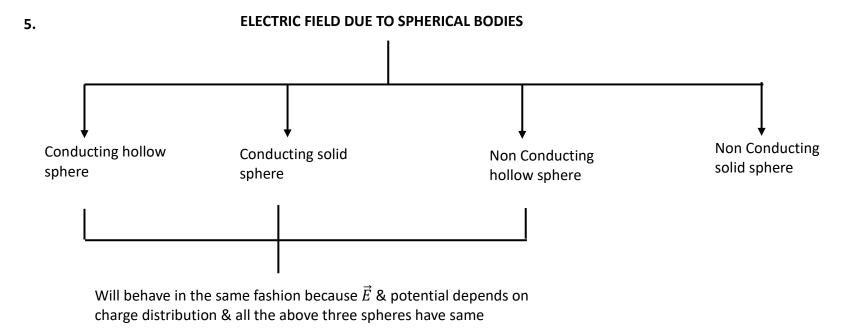
(viii) When a conductor is grounded its potential becomes zero.

(ix) When an isolated conductor is grounded then its charge becomes zero.

(x) When two conductors are connected there will be charge flow till their potential becomes equal.

(xi) Electric pressure : Electric pressure at the surface of a conductor is given by formula  $P = \frac{\sigma^2}{2\varepsilon_0}$  where  $\sigma$  is the local surface charge density.

V = 0



(a) Electric field due to a charged spherical shell of radius R

Inside 
$$= 0$$
,

Outside = 
$$\frac{q}{4\pi\varepsilon_0 r}$$

(b) Potential due to a charged spherical shell of radius R

Inside = 
$$\frac{q}{4\pi\varepsilon_0 R}$$
,

Outside =  $\frac{q}{4\pi\varepsilon_0 r}$ 

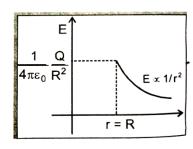
(c) Electric field due to a solid sphere of charge density ho

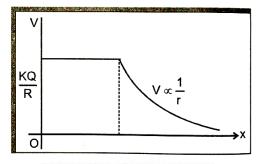
Inside = 
$$\frac{KQr}{R^3}$$
, Outside =  $\frac{Q}{4\pi\varepsilon_0 r^2}$ 

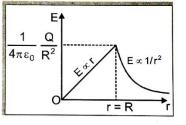
- r is distance of point from origin.
- (d) Potential due to a solid sphere of charged density  $\rho$ , and charge Q:-

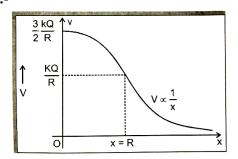
inside = 
$$\frac{KQ}{2R^3}[3R^2 - r^2]$$
  
Outside =  $\frac{KQ}{r}$   
At the centre =  $\frac{3}{2}\frac{KQ}{R}$ 

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r = distance of point from the centre of sphere.

(e) Self energy of a Hollow, conducting, solid conducting & hollow non conducting sphere.

$$U = \frac{KQ^2}{2R}$$

(f) Self Energy of a Uniformly Charged Non-conducting Sphere:

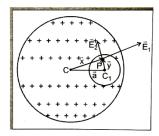
$$U_{self} = \frac{3}{5} \frac{KQ^2}{R}$$

#### 6. CHARGE INDUCTION IN METAL CAVITIES:

- (1) Whenever a charge is placed inside a metal cavity, an equal and opposite charge is induced on the inner surface of cavity.
- (2) A similar charge is induced on the outer surface of body with surface charge density inversely proportional to radius of curvature of body.
- (3) When the charge inside is displaced, the induced charge distribution on inner surface of body changes in such a way that its centre of charge can be assumed to be at the point charge so as to nullify the electric field in outer region.
- (4) Due to movement in the point charge inside the body The charge distribution on outer surface of body does not change.
- (5) If another charge is brought to the body from outside, it will only affect the outer distribution of charges no on the charge distribution inside the cavity.

#### (a) Electric Field Inside a Cavity of Non-conducting Charged Body:



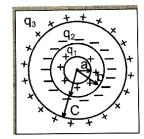


#### 7. Potential due to concentric spheres

(i) At a point r > c

$$V = \frac{1}{4\pi\varepsilon_0} \frac{q_1 - q_2 + q_3}{r}$$

(ii) At a point b < r < c



$$V = \frac{1}{4\pi\varepsilon_0} \frac{q_1 - q_2}{r} + \frac{1}{4\pi\varepsilon_0} \frac{q_3}{c}$$

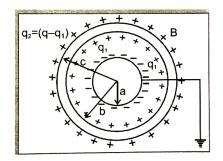
(iii) At a point a < r < b

$$V = \frac{1}{4\pi\varepsilon_0} \frac{q_1}{r} - \frac{1}{4\pi\varepsilon_0} \frac{q_2}{b} + \frac{1}{4\pi\varepsilon_0} \frac{q_3}{c}$$

(iv) At a point r < a

$$V = \frac{1}{4\pi\varepsilon_0} \left[ \frac{q_1}{a} - \frac{q_2}{b} + \frac{q_3}{c} \right]$$

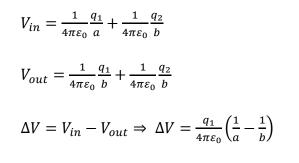
- 8. Potential difference between the two concentric spheres when one of them is earthed
  - (i)  $V = \frac{1}{4\pi\varepsilon_0} q \left[\frac{1}{a} \frac{1}{b}\right]$ (ii)  $V = \frac{1}{4\pi\varepsilon_0} q_1 \left[\frac{1}{a} - \frac{1}{b}\right]$  $\frac{q_2}{c} = q_1 \left[\frac{1}{a} - \frac{1}{b}\right] \qquad \dots \dots \dots (i)$

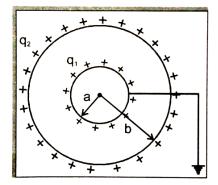


 $q_1 + q_2 = q$  ...... (ii)

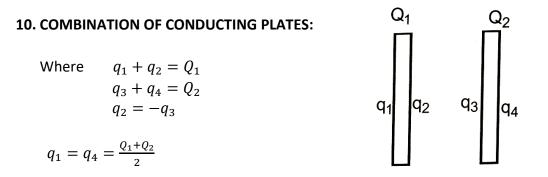
Solving (i) and (ii) we can get  $q_1$  and  $q_2$ 

#### 9. POTENTIAL DIFFERENCE BETWEEN TWO CONCENTRIC UNIFORMLY CHARGED METALLIC SPHERES.



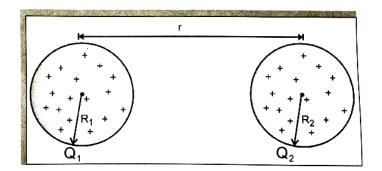


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#### **11. TOTAL ELECTROSTATIC ENERGY OF A SYSTEM OF CHARGES:**

Total electrostatic potential energy of system of charges can be given as  $U = \sum$  self energy of all charged bodies  $+\sum$  interaction energy of all pairs of charged bodies.



 $\mathbf{U} = \mathbf{U}_{self} + \mathbf{U}_{interaction}$ 

$$U = \frac{3KQ_1^2}{5R_1} + \frac{3KQ_2^2}{5R_2} + \frac{KQ_1Q_2}{r}$$



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

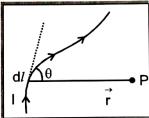
# PHYSICS

### MAGNETISM

#### 1. BIOT SAVART LAW

It states that the magnetic field strength (dB) produced due to a current element (of current I and length dI) at a point having position vector  $\vec{r}$  relative to current element is

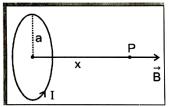
 $d\vec{B} = \frac{\mu_0}{4\pi} \frac{I\vec{dl} \times \vec{r}}{r^3}$   $\mu_0 = \text{permeability of free space} = 4\pi \times 10^{-7}$ Where  $\theta$  is the angle between current element  $I\vec{dl}$  and position vector  $\vec{r}$ . The direction of magnetic field  $d\vec{B}$ is perpendicular to plane containing  $I\vec{dl}$  and  $\vec{r}$ .



#### 2. MAGNETIC FIELD DUE TO A CIRCUIT COIL

The magnetic field due to current carrying circular coil of N-turns, radius a, carrying current I at a distance x from the centre of coil is

$$B = \frac{\mu_0 N I a^2}{2(a^2 + x^2)^{3/2}}$$
 along the axis  
At centre x = 0  
$$\therefore B_C = \frac{\mu_0 N I}{2a}$$



In general the field produced by a circle arc subtending an angle  $\boldsymbol{\theta}$  at centre

$$B_{C} = \frac{\mu_{0}I}{2a} \cdot \frac{\theta}{2\pi} \quad (\theta \text{ in radian})$$



#### 3. AMPERE'S CIRCULITAL LAW

It states that the line integral of magnetic field induction along a closed path is equal to  $\mu_0$  – times the current enclosed by the path i.e.,

$$\oint \vec{\mathbf{B}} d\vec{l} = \mu_0 \mathbf{I}$$

#### 4. MAGNETIC FIELD DUE TO A STRAIGHT CONDUCTOR CARRYING A CURRENT

The magnetic field due to a straight current carrying wire of finite length is

$$\mathbf{B} = \frac{\mu_0 \mathbf{I}}{4\pi \mathbf{R}} (\sin \phi_1 + \sin \phi_2)$$

The direction of magnetic field is given by right hand grip rule. Special cases : If the wire infinitely long. then  $\phi_1 = \pi/2$ ,  $\phi_2 = \pi/2$ 

$$\mathbf{B} = \frac{\mu_0 \mathbf{I}}{2\pi \mathbf{R}}$$

If point is near one end of a long wire,

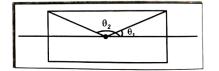
$$\left( \phi_1 = \frac{\pi}{2}, \phi_1 = 0 \right)$$
 then  $B = \frac{\mu_0 I}{4\pi R}$ 

5. If point is near one end due to a Solenoid

$$\mathbf{B} = \frac{\mu_0 n i}{2} \left[ \cos \theta_2 - \cos \theta_1 \right]$$

(i) At the axis of a long solenoid

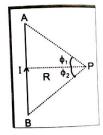
$$\begin{aligned} \theta_1 &= 0, \\ B &= \mu_0 n I \end{aligned} \qquad \qquad \theta_2 &= \pi \end{aligned}$$



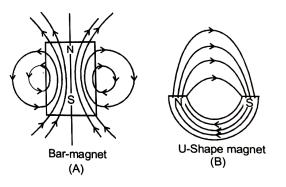
where  $n=number\ of\ turns\ per\ metre\ length.$  Magnetic field at on end of solenoid

$$B_{end} = \frac{\mu_0 nI}{2}$$

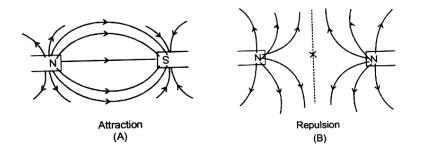
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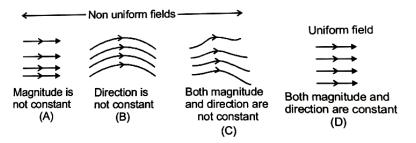
#### 6. MAGNETIC LINES AND THEIR CHARACTERISTICS



- (i) Outside a magnet, field are from north to south pole while inside from south to north, i.e., magnetic lines are closed curves i.e. they appear to converge or diverge at poles.
- (ii) The number of magnetic lines of field originating or terminating on a pole is proportional to its strength.
- (iii) Magnetic lines of field can never intersect each other because if they intersect at a point, intensity at that point will have two directions which is absurd.
- (iv) Magnetic lines of field have a tendency to contract longitudinally like a stretched elastic string (producing attraction between similar poles)



(v) Number of lines of field per unit area, normal to the area at a point, represents the magnitude of field at that point. So crowded lines represent a strong field while distant lines represent weak field. Further, if the lines of force are equidistant and straight the field is uniform otherwise not

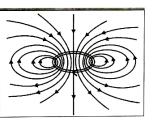


7. As monopoles do not exist, the total magnetic flux linked with a closed surface is always zero, i.e.,

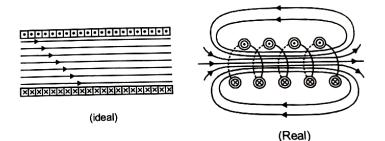
 $\oint \vec{B}. \vec{ds} = \mu_0(0) = 0$ This law is called Gauss's law for magnetism.

8. MAGNETIC FIELD LINE DUE TO SOME IMPORTANT STRUCTURE
(a) Straight current carrying wire
(b) Circular coil





#### (c) Solenoid



#### 9. MAGNETIC FIELD DUE TO A TOROID (ENDLESS SOLENOID)

Magnetic field within the turns of toroid

Where r is average radius.

Magnetic field outside the toroid is zero.

#### **10. FORCE ON A CHARGED PARTICLE IN MAGNETIC FIELD**

The force on a charged moving with velocity  $\vec{v}$  and  $\vec{B}$  in a uniform magnetic field  $\vec{B}$  is given by  $\vec{F}_m = q(\vec{v} \times \vec{B})$ The direction of this force is perpendicular to both  $\vec{v}$  and  $\vec{B}$ When  $\vec{v}$  is parallel to  $\vec{B}$ , then  $\vec{F}_m = 0$ 

 $\mathbf{B} = \frac{\mu_0 NI}{2\pi r}$ 

When  $\vec{v}$  is perpendicular to  $\vec{B}$ , Then  $\vec{F}_m$  is maximum,  $(F_m) = qvB$ .

#### 11. FORCE ON A CHARGED PARTICLE IN SIMULTANEOUS ELECTRIC AND MAGNETIC FIELD

The total force on a charged particle moving in simultaneous electric field  $\vec{E}$  and magnetic field  $\vec{B}$  is given by  $\vec{F} = q(\vec{E} \times \vec{v} \times \vec{B})$ 

This is called Lorentz force.

#### **12. PATH OF CHARGED PARTICLE IN MAGNETIC FIELD.**

- (i) If  $\vec{v}$  is parallel to the direction of  $\vec{B}$ , then magnetic force = zero. So the path of particle is an undelfected straight line.
- (ii) If  $\vec{v}$  is perpendicular to  $\vec{B}$ , then magnetic field provides necessary centripetal force for **Circular path**, the radius r of path is given by

$$\frac{mv^2}{r} = qvB \implies r = \frac{mv}{qB}$$
If E is kinetic energy of particle  $r = \frac{\sqrt{2mE}}{qB}$ 
If V is accelerating potential in volt,  $E = qV$ 

$$\therefore r = \frac{\sqrt{2mE}}{qB} = \frac{1}{B}\sqrt{\frac{2mV}{q}}$$

Time period of path

$$=\frac{2\pi m}{qB}$$

(iii) If a particle's velocity  $\vec{v}$  is oblique to magnetic field  $\vec{B}$ , then the particle follows a helical path of radius

$$r = \frac{mv \sin\theta}{qB} = \frac{mv_{\perp}}{qB}$$
  
Time period  $T = \frac{2\pi m}{qB}$  and pitch  $p = v'T = v\cos\theta \frac{2\pi m}{qB}$ 

Т

Where v' is a component of velocity parallel to the direction of magnetic field.

#### 13. Simultaneous Electric and Magnetic Fields

If a particle of charge q enters in a region of simultaneous electric and magnetic field of strength  $\vec{E}$  and  $\vec{B}$  respectively. Then the net force on charged particle is

$$\vec{F} = \vec{F}_e + \vec{F}_m = q\vec{E} + q\vec{v} \times \vec{B}$$
 i.e.,  $\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$ 

#### 14. Velocity Filter

If electric and magnetic fields are mutually perpendicular and a charged particle enters this region with velocity  $\vec{v}$  which is perpendicular to both electric and magnetic fields, then it may happen that the electric and magnetic forces are equal and opposite and charged particle with given velocity v remain undeflected in both fields. In such a condition.

$$qE = qvB \Longrightarrow v = \frac{E}{B}$$

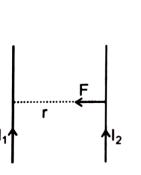
This arrangement is called velocity filter or velocity selector.

#### **15.** Magnetic Force on a Current Carrying Conductor or Length $\vec{l}$ is given by

$$\vec{F}_m = I\vec{l} \times \vec{B}$$
  
where the direction of  $\vec{l}$  is along the direction of current.  
Magnitude of force  
 $F_m = IlB \sin\theta$   
Direction of force  $\vec{F}$  is normal to  $\vec{l}$  and  $\vec{B}$  given by rule of vector product. If  $\theta = 0$   
(i.e.,  $\vec{l}$  is parallel to  $\vec{B}$ ), then magnetic force is zero.

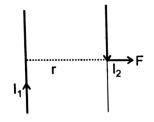
#### **16. FORCE BETWEEN PARALLEL CURRENT CARRYING CONDUCTORS**

Parallel currents attract while antiparallel currents repel. The magnetic force per unit length on either current carrying conductor at separation 'r' given by  $f = \frac{F}{l} = \frac{\mu_0 I_1 I_2}{2\pi r} \text{ newton/metre}$ 



#### **17. DEFINITION OF AMPERE IN S.I. SYSTEM**

One ampere is the current which when flowing in each of the two parallel wires in vacuum at separation 1 m exert a force of  $\frac{\mu_0}{2\pi} = 2 \times 10^{-7} N/m$  on either wire.



#### 18. TORQUE EXPERIENCED BY A CURRENT LOOP (OF AREA $\vec{A}$ )

Carrying current l in a uniform magnetic field  $\vec{B}$  is given by

$$\vec{\tau} = \text{NI}\vec{A} \times \vec{B} = \vec{M} \times \vec{B}$$

Where  $\vec{M} = NI\vec{A}$  is magnetic moment of loop. The unit of magnetic moment in S.I. system is ampere ×  $metre^2(Am^2)$ 

#### **19. POTENTIAL ENERGY OF A CURRENT LOOP IN A MAGNETIC FIELD**

When a current loop of magnetic moment M is placed in a magnetic field, the potential energy of dipole is:

 $U = -\vec{M}.\vec{B} = -MB\cos\theta$ 

(i) When  $\theta = 0$ , U = -MB (minimum or stable equilibrium position)

(ii) When  $\theta = \pi$ , U = +MB (maximum or unstable equilibrium position)

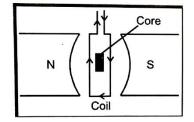
(iii) When  $\theta = \frac{\pi}{2}$ , potential energy is zero.

#### **20. MOVING COIL GALVANOMETER**

A moving coil galvanometer consists of a rectangular coil placed in a uniform magnetic field produced by cylindrical pole pieces to make the magnetic field radial. Torque on coil  $\tau = N I AB$  where N is number of turns. A is area of coil. If k is torsional rigidity of material of suspension wire, then for deflection  $\theta$ , torque  $\tau = k\theta$ 

: For equilibrium

NIAB =  $k \theta$ 



$$\implies \theta = \frac{NAB}{k}I$$

Clearly deflection in galvanometer is directly proportional to current, so the scale of galvanometer is linear.

#### **21. SENSITIVITY OF GALVANOMETER :**

#### 21.1 Current sensitivity :

It is defined on the deflection of coil per unit potential difference across its ends

i.e., 
$$S_v = \frac{\theta}{V} = \frac{\text{NAB}}{\text{kR}}$$

where R is resistance of galvanometer.

Clearly for greater sensitivity number of turns N, area A and magnetic field strength B should be large and torsional rigidity k of suspension should be small.

#### 22. MAGNETIC DIPOLE MOMENT OF A CURRENT LOOP AND REVOLVING ELECTRON

Magnetic dipole moment of a magnet,  $M = 2lamp - m^2$  where m is pole strength.

2l is separation between poles. Magnetic dipole moment of a current loop.

$$M = \frac{e}{2m_e} Lamp - m^2$$

•21•	
m +	m

m

#### 23. Magnetic field intensity due to a magnetic dipole

Magnetic field intensity at a general point having polar coordinates (r,  $\theta$ ) due to a short magnet is given by

$$B = \frac{\mu_0}{4\pi r^3} \sqrt{1 + 3 \cos^2 \theta}$$
Special Cases
(i) At axial point  $\theta = 0$ ,  $B_{axis} = \frac{\mu_0}{4\pi} \frac{2M}{r^3}$ 
(ii) At equation point  $\theta = 90^\circ$   $B_{eqn.} = \frac{\mu_0}{4\pi} \frac{M}{r^3}$ 



## JEE FORMULA NOTES

## **DEPTH Notes with Revision**

# PHYSICS

### **MODERN PHYSICS**

#### **De Broglie Waves**

$$\lambda = \frac{h}{P} = \frac{h}{mv}$$

#### **Photoelectric Effect**

#### (a) Photons

Electromagnetic wave energy is emitted and absorbed in package of definite size called photons. The energy E of photon is proportional to wave frequency f.

i.e. 
$$E \propto f$$
 or  $E = hf = \frac{hc}{\lambda}$ 

where h is called the Plank's constant

$$(h = 6.63 \times 10^{-34} \text{ Js})$$

C is speed of light in vaccum, and

 $\boldsymbol{\lambda}$  is the wavelength of light in vacuum.

The expression can be simplified in the following form for practical applications.

$$E(eV) = \frac{12400}{\lambda(Å)}$$

The momentum p of a photon of energy E is given by  $p = \frac{E}{c}$  where c is the speed of light. Thee direction of momentum is the direction of propagation of light.

#### (b) Einstein's photoelectric equation

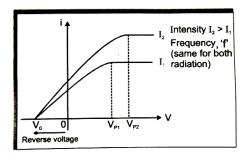
The maximum kinetic energy of the photoelectron is given by

$$\frac{1}{2}mv_{max}^2 = hf - W$$

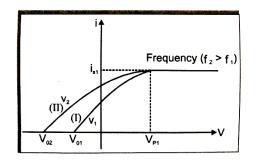
Where f is the frequency of the incident photon, and W is the work function of metal surface.  $W = hf_0$ 

where  $f_0$  is the threshold frequency.

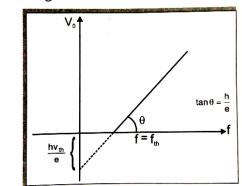
- (i) Photocurrent I is directly proportional to intensity of incident radiation and there is no threashold intensity provided of intensity provided the frequency is greater than the threshold frequency.
- (ii) The figure shows variation of potential V of the anode with respect to the cathode for a constant light frequency. The stopping potential independent of light intensity I.



(iii) The figure shows the variation of photocurrent i as a function of the potential V of the anode with respect to cathode for two different light frequencies  $f_1$  and  $f_2$  (>  $f_1$ ) with the same intensity. The stopping potential increases linearly with frequency.



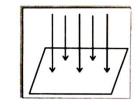
(iv) The figure shows that the maximum kinetic energy  $\frac{1}{2}mv_{max}^2$  of ejected electron is directly proportional to the frequency f of the incident light if it is greater than the threshold frequency.



#### FORCE DUE TO RADIATION (PHOTON)

 $\frac{1}{2}mv_{max}^2 = eV_0 = h(f - f_{th})$ 

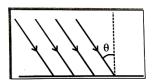
(A) Case (I): a = 1, r = 0pressure  $\frac{F}{A} = \frac{IA}{cA} = \frac{I}{C}$ 



Case (II) : When r = 1, a = 0Pressure  $P = \frac{F}{A} = \frac{2IA}{cA} = \frac{2I}{C}$ 

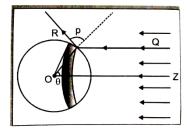
#### Case (III) : When 0 < r < 1 a + r = 1 Now pressure P = $\frac{IA}{C}(1 + r) \times \frac{1}{c}(1 + r)$

(B) Case-I 
$$a = 1, r = 0$$
  
Pressure  $= \frac{F\cos\theta}{A}P = \frac{IA\cos^2\theta}{cA} = \frac{I}{c}\cos^2\theta$   
Case-II When  $r = 1, a = 0$   
Pressure  $= \frac{2IA\cos^2\theta}{cA}$ ,  $P = \frac{2I\cos^2\theta}{c}$   
Case-III  $0 < r < 1$ ,  $a + r = 1$   
Pressure  
 $= \frac{I\cos^2\theta}{c}(1 - r) + \frac{I\cos^2\theta}{c}2r = \frac{I\cos^2\theta}{c}(1 + r)$ 



(C) Pressure 
$$=\frac{\pi r^2 l}{c}$$

Note that integration is done only for the hemisphere that faces the incident beam



#### ATOMIC LINE SPECTRA

In 1885, Balmer discovered a formula for the wavelength of certain spectral lines observed coming from excited hydrogen.

$$\frac{1}{\lambda} = R_{\infty} \left[ \frac{1}{2^2} - \frac{1}{n^2} \right]$$
 for n = 3, 4, 5 .....

Where,  $R_{\infty} = 1.097 \times 10^{-7} m^{-1}$  is called the **Rydberg constant.** Later on other similar formulae were also discovered for hydrogen atoms. These are

Lyman Series,

$$\frac{1}{\lambda} = R_{\infty} \left[ \frac{1}{1^2} - \frac{1}{n^2} \right]$$
 for n = 2, 3, 4 .....

**Paschen Series** 

$$\frac{1}{\lambda} = R_{\infty} \left[ \frac{1}{3^2} - \frac{1}{n^2} \right]$$
 for n = 4, 5, 6 .....

**Brackett Series** 

$$\frac{1}{\lambda} = R_{\infty} \left[ \frac{1}{4^2} - \frac{1}{n^2} \right]$$
 for n = 5, 6, 7 .....

#### The Bohr Model

- (a) The electrons move in circular orbits and the centripetal force is provided by the Coulomb force of attraction between then nucleus and electron.
- (b) Only certain orbits are allowed in which the angular momentum of the electron is an integral multiple of  $\frac{h}{2\pi}$

That is,  $mvr = \frac{nh}{2\pi}$  where  $n = 1, 2, 3, \dots$ 

- (c) Energy is emitted or absorbed when the electron jumps from one level to another. For a transition from a higher orbit to a lower orbit, the photon is emitted and the energy difference is hf, where f is the frequency of the photon.
- (d) Photon absorption causes a transition of the electron to a higher orbit but only if the energy and frequency are just appropriate.

#### **Bohr's Formulae**

(a) The radius of the nth orbit is defined as

$$r_n = 0.53 \frac{n^2}{z} \text{\AA}$$

(b) The speed of electron in n th orbit is

 $v_n = \frac{z}{n} \left(\frac{c}{137}\right)$ Where c = 3 × 10<sup>8</sup> ms<sup>-1</sup> is the speed of light. Or  $v_n = \frac{2.19 \times 10^6 \text{ Z}}{n} \text{ ms}^{-1}$ 

The speed of electron is independent of its mass.

(c) The total energy of an atom is the sum total of kinetic and potential. If the electron is in the n th shell, then

$$E = -13.6 \frac{Z^2}{n^2} (eV)$$
 or  $E = K + U = -K = \frac{U}{2}$ 

And the total energy is directly proportional to the mass of the electron.

If the potential energy is assumed to be zero at n = 1, then the total energy of the atom will be

$$E = -\frac{13.6Z^2}{n^2} + 27.2Z^2$$
 or  $E = \left(2 - \frac{1}{n^2}\right) 13.6Z^2$ 

(d) The wavelength of photon emitted when electron jumps from  $n = n_2$  to  $n = n_1$  is given by

$$\frac{1}{\lambda} = \frac{\Delta E}{hc} = \frac{E_2 - E_1}{hc} = \frac{13.6Z^2}{hc} \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$
  
or  $\frac{1}{\lambda} = R_{\infty} Z^2 \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$ 

If the nucleus of atom is not considered to be stationary, then equations for radius energy and wavelength may be modified as

$$r_{n} = 0.53 \frac{n^{2}}{Z} \left(1 + \frac{m}{M}\right) \text{\AA}$$
$$E_{n} = -13.6 \frac{Z^{2}}{n^{2}} \left(\frac{M}{m+M}\right) eV$$
$$\frac{1}{\lambda} = \frac{R_{\infty}}{1 + \frac{m}{M}} Z^{2} \left[\frac{1}{n_{1}^{2}} - \frac{1}{n_{2}^{2}}\right] m^{-1}$$

where m is the mass of electron, and M is the mass of nucleus.

#### Note:

(i) Total number of emission lines from some excited state  $n_1$  to another energy state

$$n_2(< n_1)$$
 is given by  $\frac{(n_1-n_2)(n_1-n_2+1)}{2}$ 

For example total number of lines from  $n_1 = n$  to  $n_2 = 1$  are  $\frac{n(n-1)}{2}$ 

(ii) As the principal quantum number n is increased in hydrogen and hydrogen like atoms, some quantities are decreased and some are increased. The table given below show which quantities

are increased and which are decreased.

Increased	Decreased	
Radius	Speed	
Potential energy	Kinetic energy	
Total energy	Angualr speed	
Time period		
Angular momentum		

#### X-Rays

X-rays are highly penetrating electromagnetic radiations of wavelength of the order of 1 Å

That is,  $\lambda_{min} = \frac{hc}{1/2mv^2} = \frac{hc}{eV}$ 

The cut-off wavelength is independent of the target material. It depends only on the kinetic energy of the electron beam .

The characteristic spectrum depends only on the target material, and it is independent of the kinetic energy of the electron beam.

The figure shows the variation of intensity I of X-rays as a function of their wavelength  $\lambda$ . The graphs shows a minimum wavelength  $\lambda_{min}$  (called out-off wavelength) but there is no maximum wavelength. The graph shows two basic feature.

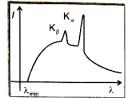
- (a) A continuous curve with  $\lambda_{min}$  shows continuous spectrum of X-rays (b) Two sharp peak of high intensity show characteristic spectrum.
- (c) Variation of *I* versus  $\lambda$  the kinetic energy of the electron beam is increased from K<sub>1</sub> to K<sub>2</sub> keeping the same target. It is observed that cutoff wavelength of continuous spectrum decreases ( $\lambda_2 < \lambda_1$ ) but the characteristics spectrum remains unchanged.
- (d) Variation of *I* versus  $\lambda$  The target material is changed ( $Z_2 > Z_1$ ) but the kinetic energy of the electron beam remains unchanged. It is observed that the cut-off wavelength remains same but the characteristics spectrum is the unique property of the target material.

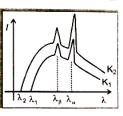
Moseley's Law 
$$\sqrt{f} = a(Z - b)$$
$$\frac{1}{\lambda} = R_{\infty}(Z - 1)^{2} \left[1 - \frac{1}{n^{2}}\right]$$
$$n = 2, 3, 4 \dots$$

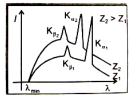
#### Radioactivity

(a) After n half-lives,

(i) Number of nuclei left = 
$$N_0 \left(\frac{1}{2}\right)^n$$
 (ii) fraction of nuclei left =  $\left(\frac{1}{2}\right)^n$  and







(iii) Percentage of nuclei left =  $100 \left(\frac{1}{2}\right)^n$ 

- (b) Number of nuclei decayed after time t,
  - $= N_0 N$  $= N_0 N_0 e^{-\lambda t} = N_0 (1 e^{-\lambda t})$

The corresponding graphs is as shown in figure.

(c) Probability of a nucleus for survival after time t,

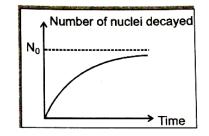
P(survival) = 
$$\frac{N}{N_0} = \frac{N_0 e^{-\lambda t}}{N_0} = e^{-\lambda t}$$

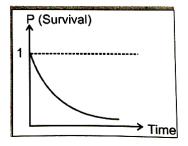
The corresponding graph is shown in figure.

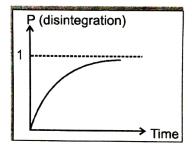
(d) Probability of a nucleus to disintegrate in time t is,

P (disintegration) =  $1 - P(survival) = 1 - e^{-\lambda t}$ 

The corresponding graph is as shown.







(e) Half-life and mean life are related to each other by the relation.

$$t_{1/2} = 0.693 t_{av}$$
 or  $t_{av} = 1.44 t_{1/2}$ 

(f) As we said in point number (2), Number of nuclei decayed in time t are

$$N_0(1-e^{-\lambda t})$$
 So, to avoid it we can use.

$$\Delta N = \frac{\lambda N}{\Delta t}$$

Where,  $\Delta N$  are the number of nuclei decayed in time  $\Delta t$ , at the instant when total number of Nuclei are N. But this can be applied only when  $\Delta t \ll t_{1/2}$ .

(g) In same interval of time, equal percentage (or fraction) of nuclei are decayed (or left undecayed).